IIR 18: Latent Semantic Indexing
Handout version

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#### Overview

- Latent semantic indexing
- 2 Dimensionality reduction
- String in the string of the
- Clustering

- Latent Semantic Indexing (LSI) / Singular Value Decomposition: The math
- SVD used for dimensionality reduction
- LSI: SVD in information retrieval
- LSI as clustering
- gensim: Topic modelling for humans (practical use of LSI etal.)

#### Recall: Term-document matrix

Latent semantic indexing

	Anthony	Julius	The	Hamlet	Othello	Macbeth
	and	Caesar	Tempest			
	Cleopatra					
anthony	5.25	3.18	0.0	0.0	0.0	0.35
brutus	1.21	6.10	0.0	1.0	0.0	0.0
caesar	8.59	2.54	0.0	1.51	0.25	0.0
calpurnia	0.0	1.54	0.0	0.0	0.0	0.0
cleopatra	2.85	0.0	0.0	0.0	0.0	0.0
mercy	1.51	0.0	1.90	0.12	5.25	0.88
worser	1.37	0.0	0.11	4.15	0.25	1.95

This matrix is the basis for computing the similarity between documents and queries.

Today: Can we transform this matrix, so that we get a better measure of similarity between documents and queries?

#### Latent semantic indexing: Overview

- We will decompose the term-document matrix into a product of matrices.
- The particular decomposition we'll use: singular value decomposition (SVD).
- SVD:  $C = U\Sigma V^T$  (where C = term-document matrix)
- We will then use the SVD to compute a new, improved term-document matrix C'.
- We'll get better similarity values out of C' (compared to C).
- Using SVD for this purpose is called latent semantic indexing or LSL

# Example of $C = U\Sigma V^T$ : The matrix C

C	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$
ship	1	0	1	0	0	0
boat	0	1	0	0	0	0
ocean	1	1	0	0	0	0
wood	1	0	0	1	1	0
tree	0	0	0	1	0	1

This is a standard term-document matrix.

Actually, we use a non-weighted matrix here to simplify the example.

U	1	2	3	4	5
ship	-0.44	-0.30	0.57	0.58	0.25
boat	-0.13	-0.33	-0.59	0.00	0.73
ocean	-0.48	-0.51	-0.37	0.00	-0.61
wood	-0.70	0.35	0.15	-0.58	0.16
tree	-0.26	0.65	-0.41	0.58	-0.09

One row per term, one column per min(M, N) where M is the number of terms and N is the number of documents.

This is an orthonormal matrix: (i) Row vectors have unit length. (ii) Any two distinct row vectors are orthogonal to each other.

Think of the dimensions as "semantic" dimensions that capture distinct topics like politics, sports, economics. 2 = land/water

Each number  $u_{ij}$  in the matrix indicates how strongly related term i is to the topic represented by semantic dimension j.

	1				
1	2.16 0.00 0.00 0.00 0.00	0.00	0.00	0.00	0.00
2	0.00	1.59	0.00	0.00	0.00
3	0.00	0.00	1.28	0.00	0.00
4	0.00	0.00	0.00	1.00	0.00
5	0.00	0.00	0.00	0.00	0.39

This is a square, diagonal matrix of dimensionality  $min(M, N) \times min(M, N)$ .

The diagonal consists of the singular values of C.

The magnitude of the singular value measures the importance of the corresponding semantic dimension.

We'll make use of this by omitting unimportant dimensions.

# Example of $C = U\Sigma V^T$ : The matrix $V^T$

$V^T$	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$
1	-0.75	-0.28	-0.20	-0.45	-0.33	-0.12
2	-0.29	-0.53	-0.19	0.63	0.22	0.41
3	0.28	-0.75	0.45	-0.20	0.12	-0.33
4	0.00	0.00	0.58	0.00	-0.58	0.58
5	-0.53	0.29	0.63	0.19	0.41	-0.22

One column per document, one row per min(M, N) where M is the number of terms and N is the number of documents.

Again: This is an orthonormal matrix: (i) Column vectors have unit length. (ii) Any two distinct column vectors are orthogonal to each other.

These are again the semantic dimensions from matrices U and  $\Sigma$  that capture distinct topics like politics, sports, economics.

Each number  $v_{ij}$  in the matrix indicates how strongly related document i is to the topic represented by semantic dimension

# Example of $C = U\Sigma V^T$ : All four matrices Recall unreduced decomposition $C = U\Sigma V^T$ Exercise: Why can this be viewed as soft clustering?

С	d	1 (	<i>l</i> <sub>2</sub>	d <sub>3</sub>	$d_4$	$d_5$	$d_6$									
ship	1	C	)	1	0	0	0									
boat	0	1	. (	0	0	0	0									
ocear	n 1	1	. (	0	0	0	0	=								
wood	1	C	) (	0	1	1	0									
tree	0	C	) (	0	1	0	1									
U	İ	1		2	2	3	3	4		5	Σ	1	2	3	4	5
ship	-	0.44	-	-0.30	)	0.57	7	0.58	0.2	5	1	2.16	0.00	0.00	0.00	0.00
boat	-	0.13	-	-0.33	3	-0.59	)	0.00	0.7	3	2	0.00	1.59	0.00	0.00	0.00
ocear	n   –	0.48	-	0.5	1	-0.37	7	0.00	-0.6	1 ×	3	0.00	0.00	1.28	0.00	0.00
wood	I   -	0.70	)	0.35	5	0.15	; -	-0.58	0.1	6	4	0.00	0.00	0.00	1.00	0.00
tree	-	0.26	j	0.65	5	-0.41		0.58	-0.0	9	5	0.00	0.00	0.00	0.00	0.39
$V^T$	'	$d_1$		$d_2$		$d_3$		$d_4$	$d_5$		$d_6$	'				
1	-0.	75	<b>−</b> 0.	28	-(	0.20	-0	.45	-0.33	-0	).12					
2	-0.	29	-0.	53	_(	0.19	0	.63	0.22	C	0.41					
3	0.	28	-0.	75	(	0.45	-0	.20	0.12	-c	0.33					
4	0.	00	0.	00	(	0.58	0	.00	-0.58	C	0.58					
5	_0	53	Ο	29	(	0.63	0	19	0.41	_(	1 22					

LSI is decomposition of C into a representation of the terms, a representation of the documents and a representation of the importance of the "semantic" dimensions.

Latent semantic indexing

- We've decomposed the term-document matrix C into a product of three matrices:  $U\Sigma V^T$ .
- The term matrix U consists of one (row) vector for each term
- The document matrix  $V^T$  consists of one (column) vector for each document
- The singular value matrix  $\Sigma$  diagonal matrix with singular values, reflecting importance of each dimension
- Next: Why are we doing this?

$V^T$	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$
1	-0.75	-0.28	-0.20	-0.45	-0.33	-0.12
2	-0.29	-0.53	-0.19	0.63	0.22	0.41
3	0.28	-0.75	0.45	-0.20	0.12	-0.33
4	0.00	0.00	0.58	0.00	-0.58	0.58
5	-0.53	0.29	0.63	0.19	0.41	-0.22

Verify that the first document has unit length.

Verify that the first two documents are orthogonal.

$$0.75^2 + 0.29^2 + 0.28^2 + 0.00^2 + 0.53^2 = 1.0059$$
  
 $-0.75* -0.28 + -0.29* -0.53 + 0.28* -0.75 + 0.00* 0.00 + -0.53* 0.29 = 0$ 

#### How we use the SVD in LSI

- Key property: Each singular value tells us how important its dimension is.
- By setting less important dimensions to zero, we keep the important information, but get rid of the "details".
- These details may
  - be noise in that case, reduced LSI is a better representation because it is less noisy.
  - make things dissimilar that should be similar again, the reduced LSI representation is a better representation because it represents similarity better.
- Analogy for "fewer details is better"
  - Image of a blue flower
  - Image of a yellow flower
  - Omitting color makes it easier to see the similarity

# Reducing the dimensionality to 2

U		1	2	3	4	5	
ship	-0.4	14 –	-0.30	0.00	0.00	0.00	
boat	-0.1	L3 –	-0.33	0.00	0.00	0.00	
ocear	n -0.4	18 –	-0.51	0.00	0.00	0.00	
wood	-0.7	70	0.35	0.00	0.00	0.00	
tree	-0.2	26	0.65	0.00	0.00	0.00	
$\Sigma_2$	1	2	3	4	5		
1	2.16	0.00	0.00	0.00	0.00	_	
2	0.00	1.59	0.00	0.00	0.00		
3	0.00	0.00	0.00	0.00	0.00		
4	0.00	0.00	0.00	0.00	0.00		
5	0.00	0.00	0.00	0.00	0.00		
$V^T$	$d_1$		$d_2$	$d_3$	$d_4$	$d_5$	$d_6$
1	-0.75	<b>-</b> 0.	.28 –	0.20	-0.45	-0.33	-0.12
2	-0.29	-0.	.53 –	0.19	0.63	0.22	0.41
3	0.00	0.	.00	0.00	0.00	0.00	0.00
4	0.00	0.	.00	0.00	0.00	0.00	0.00
5	0.00	0.	.00	0.00	0.00	0.00	0.00

Actually, we only zero out singular values in  $\Sigma$ . This has the effect of setting the corresponding dimensions in U and  $V^T$  to zero when computing the product C = $U\Sigma V^T$ .

# Reducing the dimensionality to 2

$C_2$	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$					
ship	0.85	0.52	0.28	0.13	0.21	-0.08					
boat	0.36	0.36	0.16	-0.20	-0.02	$-0.18_{-}$	_				
ocean	1.01	0.72	0.36	-0.04	0.16	$-0.21^{-}$	_				
wood	0.97	0.12	0.20	1.03	0.62	0.41					
tree	0.12	-0.39	-0.08	0.90	0.41	0.49					
U	1	1 2	! 3	4	į	$\Sigma_2$	1	2	3	4	5
ship	-0.44	4 -0.30	0.57	0.58	0.25	5 1	2.16	0.00	0.00	0.00	0.00
boat	-0.13	-0.33	-0.59	0.00	0.73	3 × 2	0.00	1.59	0.00	0.00	0.00 ×
ocean	ı   -0.48	-0.51	-0.37	0.00	-0.61	L^ 3	0.00	0.00	0.00	0.00	0.00 ^
wood	-0.70	0.35	0.15	-0.58	0.16	5 4	0.00	0.00	0.00	0.00	0.00
tree	-0.26	0.65	-0.41	0.58	-0.09	5	0.00	0.00	0.00	0.00	0.00
$V^T$	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$					
1	-0.75	-0.28	-0.20	-0.45	-0.33	-0.12					
2	-0.29	-0.53	-0.19	0.63	0.22	0.41					Г
3	0.28	-0.75	0.45	-0.20	0.12	-0.33					L
4	0.00	0.00	0.58	0.00	-0.58	0.58					
5	-0.53	0.29	0.63	0.19	0.41	-0.22					

# Example of $C = U\Sigma V^T$ : All four matrices Recall unreduced decomposition $C = U\Sigma V^T$ Exercise: Why can this be viewed as soft clustering?

С	(	$I_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$									
ship	1		0	1	0	0	0									
boat	(	)	1	0	0	0	0									
ocea	n 1		1	0	0	0	0	=								
wood	1		0	0	1	1	0									
tree	(	) (	0	0	1	0	1									
U	İ		1		2	3	3	4		5	Σ	1	2	3	4	5
ship	-	-0.4	4	-0.3	30	0.57	7	0.58	0.3	25	1	2.16	0.00	0.00	0.00	0.00
boat	-	-0.1	3	-0.3	3	-0.59	)	0.00	0.	73	2	0.00	1.59	0.00	0.00	0.00
ocea	n -	-0.4	8	-0.5	51	-0.37	7	0.00	-0.0	51 ×	3	0.00	0.00	1.28	0.00	0.00
wood	I -	-0.7	0	0.3	35	0.15	; .	-0.58	0.	16	4	0.00	0.00	0.00	1.00	0.00
tree	-	-0.2	6	0.6	55	-0.41	L	0.58	-0.0	09	5	0.00	0.00	0.00	0.00	0.39
$V^T$	'	$d_1$		$d_2$		$d_3$		$d_4$	$d_5$		$d_6$					
1	-0	.75	_	0.28	_	0.20	-0	).45	-0.33	-	0.12					
2	-0	.29	_	0.53	_	0.19	C	0.63	0.22		0.41					
3	0	.28	_	0.75		0.45	-0	.20	0.12	_	0.33					
4	0	.00		0.00		0.58	C	0.00	-0.58		0.58					
5	_^	<b>E3</b>		0.20		0.63	(	10	0.41		າ ວວ					

LSI is decomposition of C into a representation of the terms, a representation of the documents and a representation of the importance of the "semantic" dimensions.

# Original matrix C vs. reduced $C_2 = U \Sigma_2 V^T$

C	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$
ship	1	0	1	0	0	0
boat	0	1	0	0	0	0
ocean	1	1	0	0	0	0
wood	1	0	0	1	1	0
tree	0	0	0	1	0	1

$C_2$	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$
ship	0.85	0.52	0.28	0.13	0.21	-0.08
boat	0.36	0.36	0.16	-0.20	-0.02	-0.18
ocean	1.01	0.72	0.36	-0.04	0.16	-0.21
wood	0.97	0.12	0.20	1.03	0.62	0.41
tree	0.12	-0.39	-0.08	0.90	0.41	0.49

We can view  $C_2$  as a twodimensional representation of the matrix C. We have performed a dimensionality reduction to two dimensions.

#### Exercise

C	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$
ship	1	0	1	0	0	0
boat	0	1	0	0	0	0
ocean	1	1	0	0	0	0
wood	1	0	0	1	1	0
tree	0	0	0	1	0	1

$C_2$	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$
				0.13		
				-0.20		
				-0.04		
wood	0.97	0.12	0.20	1.03	0.62	0.41
tree	0.12	-0.39	-0.08	0.90	0.41	0.49

Compute the similarity between  $d_2$  and  $d_3$  for the original matrix and for the reduced matrix.

C	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$		
ship	1	0	1	0	0	0		
boat	0	1	0	0	0	0		
ocean	1	1	0	0	0	0		
wood	1	0	0	1	1	0		
tree	0	0	0	1	0	1		
$C_2$	d	1	$d_2$		$d_3$	$d_4$	$d_5$	$d_6$
$\frac{C_2}{ship}$	0.85		<i>d</i> <sub>2</sub> 0.52		<i>d</i> <sub>3</sub> 0.28	0.13		-0.08
		5					0.21	
ship	0.8	5 5	0.52		0.28	0.13	3 0.21 0 -0.02	-0.08
ship boat	0.85	5 5 1	0.52 0.36		0.28 0.16	0.13 -0.20	3 0.21 0 -0.02 0 0.16	-0.08 $-0.18$
ship boat ocean	0.85 0.36 1.03	5 5 1 7	0.52 0.36 0.72		0.28 0.16 0.36	0.13 $-0.20$ $-0.04$	3 0.21 0 -0.02 1 0.16 3 0.62	-0.08 $-0.18$ $-0.21$

Similarity of  $d_2$  and  $d_3$  in the original space: 0.

Similarity of  $d_2$  and  $d_3$  in the reduced space:  $0.52*0.28+0.36*0.16+0.72*0.36+0.12*0.20+-0.39*-0.08 \approx 0.52$  "boat" and "ship" are semantically similar. The "reduced" similarity measure reflects this.

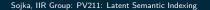
What property of the SVD reduction is responsible for improved similarity?

# Exercise: Compute matrix product

$C_2$	$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$							
ship	0.09	0.16	0.06	-0.19	-0.07	-0.12							
boat	0.10	0.17	0.06	-0.21	-0.07	-0.14	7	??????	_				
ocear	0.15	0.27	0.10	-0.32	-0.11	-0.21	•		_				
wood	-0.10	-0.19	-0.07	0.22	0.08	0.14							
tree	-0.19	-0.34	-0.12	0.41	0.14	0.27							
U		1	2	3	4	5	$\Sigma_2$	1	2	3	4	5	
ship	-0.44	1 -0.3	0 0.5	7 0.5	58 (	0.25	1	0.00	0.00	0.00	0.00	0.00	
boat	-0.13	-0.3	3 - 0.5	9 0.0	00 (	0.73 ×	2	0.00	1.59	0.00	0.00	0.00	×
ocear	-0.48	-0.5	1 - 0.3	7 0.0	-00 - 0	0.61 ^	3	0.00	0.00	0.00	0.00	0.00	^
wood	-0.70	0.3	5 0.1	5 - 0.5	58 (	0.16	4	0.00	0.00	0.00	0.00	0.00	
tree	-0.26	0.6	5 - 0.4	1 0.5	58 –0	0.09	5	0.00	0.00	0.00	0.00	0.00	
$V^T$	$d_1$	$d_2$	$d_3$	$d_4$	(	$d_5$	$d_6$						
1	-0.75	-0.28	-0.20	-0.45	-0.3	33 –0	0.12						
2	-0.29	-0.53	-0.19	0.63	0.2	22 (	0.41						
3	0.28	-0.75	0.45	-0.20	0.1	L2 —	0.33						
4	0.00	0.00	0.58	0.00	-0.5	8 (	0.58						
5	-0.53	0.29	0.63	0.19	0.4	l1 –(	0.22						

#### Why we use LSI in information retrieval

- LSI takes documents that are semantically similar (= talk about the same topics), ...
- ... but are not similar in the vector space (because they use different words) . . .
- ...and re-represents them in a reduced vector space ...
- ...in which they have higher similarity.
- Thus, LSI addresses the problems of synonymy and semantic relatedness.
- Standard vector space: Synonyms contribute nothing to document similarity.
- Desired effect of LSI: Synonyms contribute strongly to document similarity.



#### How LSI addresses synonymy and semantic relatedness

- The dimensionality reduction forces us to omit a lot of "detail".
- We have to map differents words (= different dimensions of the full space) to the same dimension in the reduced space.
- The "cost" of mapping synonyms to the same dimension is much less than the cost of collapsing unrelated words.
- SVD selects the "least costly" mapping (see below).
- Thus, it will map synonyms to the same dimension.
- But it will avoid doing that for unrelated words.

# LSI: Comparison to other approaches

- Recap: Relevance feedback and query expansion are used to increase recall in information retrieval – if query and documents have no terms in common.
  - (or, more commonly, too few terms in common for a high similarity score)
- LSI increases recall and hurts precision.
- Thus, it addresses the same problems as (pseudo) relevance feedback and query expansion . . .
- ... and it has the same problems.

#### **Implementation**

- Compute SVD of term-document matrix
- Reduce the space and compute reduced document representations
- Map the query into the reduced space  $\vec{q}_k = \sum_k^{-1} U_k^T \vec{q}$ .
- This follows from:  $C_k = U_k \Sigma_k V_k^T \Rightarrow \Sigma_k^{-1} U^T C = V_k^T$
- Compute similarity of  $q_k$  with all reduced documents in  $V_k$ .
- Output ranked list of documents as usual
- Exercise: What is the fundamental problem with this approach?

# **Optimality**

- SVD is optimal in the following sense.
- Keeping the k largest singular values and setting all others to zero gives you the optimal approximation of the original matrix C. Eckart-Young theorem
- Optimal: no other matrix of the same rank (= with the same underlying dimensionality) approximates C better.
- Measure of approximation is Frobenius norm:  $||C||_F = \sqrt{\sum_i \sum_j c_{ij}^2}$
- So LSI uses the "best possible" matrix.
- There is only one best possible matrix unique solution (modulo signs).
- Caveat: There is only a tenuous relationship between the Frobenius norm and cosine similarity between documents.

#### Data for graphical illustration of LSI

 $c_1$  Human machine interface for lab abc computer applications

 $c_2$  A survey of user opinion of computer system response time

 $c_3$  The EPS user interface management system

 $c_4$  System and human system engineering testing of EPS

 $c_5$  Relation of user perceived response time to error measurement

 $m_1$  The generation of random binary unordered trees

 $m_2$  The intersection graph of paths in trees

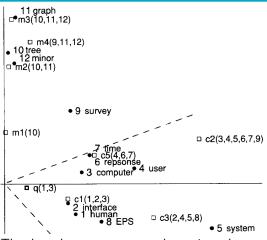
m<sub>3</sub> Graph minors IV Widths of trees and well quasi ordering

 $m_4$  Graph minors A survey

#### The matrix C

	c1	c2	c3	c4	c5	m1	m2	m3	m4
human	1	0	0	1	0	0	0	0	0
interface	1	0	1	0	0	0	0	0	0
computer	1	1	0	0	0	0	0	0	0
user	0	1	1	0	1	0	0	0	0
system	0	1	1	2	0	0	0	0	0
response	0	1	0	0	1	0	0	0	0
time	0	1	0	0	1	0	0	0	0
EPS	0	0	1	1	0	0	0	0	0
survey	0	1	0	0	0	0	0	0	1
trees	0	0	0	0	0	1	1	1	0
graph	0	0	0	0	0	0	1	1	1
minors	0	0	0	0	0	0	0	1	1

# Graphical illustration of LSI: Plot of $C_2$



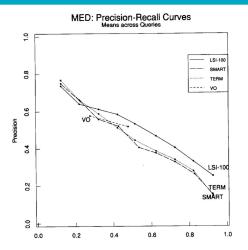
2-dimensional plot of  $C_2$  (scaled dimensions). Circles = terms. Open squares = documents (component terms in parentheses). q = query "human computer interaction".

The dotted cone represents the region whose points are within a cosine of .9 from q . All documents about human-computer documents (c1-c5) are near q, even c3/c5 although they share no terms. None of the graph theory documents (m1-m4) are near q.

#### Exercise

What happens when we rank documents according to cosine similarity in the original vector space? What happens when we rank documents according to cosine similarity in the reduced vector space?

# LSI performs better than vector space on MED collection



 $\mathsf{LSI}\text{-}100 = \mathsf{LSI}$  reduced to 100 dimensions;  $\mathsf{SMART} = \mathsf{SMART}$  implementation of vector space model

# Example of $C = U\Sigma V^T$ : All four matrices Recall unreduced decomposition $C = U\Sigma V^T$ Exercise: Why can this be viewed as soft clustering?

С		$d_1$	$d_2$	$d_3$	$d_4$	$d_5$	$d_6$									
ship		1	0	1	0	0	0									
boat	(	)	1	0	0	0	0									
ocear	n :	1	1	0	0	0	0	=								
wood	1 :	1	0	0	1	1	0									
tree	(	)	0	0	1	0	1									
U	Ì		1		2	3	3	4	. !	5	Σ	1	2	3	4	5
ship		-0.4	4	-0.3	0	0.57	,	0.58	0.2	5	1	2.16	0.00	0.00	0.00	0.00
boat		-0.1	3	-0.3	3	-0.59	)	0.00	0.7	3	2	0.00	1.59	0.00	0.00	0.00
ocear	n -	-0.4	8	-0.5	1	-0.37	,	0.00	-0.6	1 ×	3	0.00	0.00	1.28	0.00	0.00
wood	١ .	-0.7	0	0.3	5	0.15	<b>,</b> -	-0.58	0.1	6	4	0.00	0.00	0.00	1.00	0.00
tree		-0.2	6	0.6	5	-0.41		0.58	-0.09	9	5	0.00	0.00	0.00	0.00	0.39
$V^T$	"	$d_1$		$d_2$		$d_3$		$d_4$	$d_5$		$d_6$					
1	-0	).75	=	-0.28	_	0.20	-0	.45	-0.33	-0	.12					
2	-0	.29	_	-0.53	_	0.19	0	.63	0.22	0	.41					
3	(	0.28	_	-0.75		0.45	-0	.20	0.12	-0	.33					
4	C	0.00		0.00		0.58	0	.00	-0.58	0	.58					
5		153		0.20		0.63	Λ	10	0.41	_0	22					

LSI is decomposition of C into a representation of the terms, a representation of the documents and a representation of the importance of the "semantic" dimensions.

#### Why LSI can be viewed as soft clustering

• Each of the k dimensions of the reduced space is one cluster.

Clustering

- If the value of the LSI representation of document d on dimension k is x, then x is the soft membership of d in topic k.
- This soft membership can be positive or negative.
- Example: Dimension 2 in our SVD decomposition
- This dimension/cluster corresponds to the water/earth dichotomy.
- "ship", "boat", "ocean" have negative values.
- "wood", "tree" have positive values.
- $d_1$ ,  $d_2$ ,  $d_3$  have negative values (most of their terms are water terms).
- $d_4$ ,  $d_5$ ,  $d_6$  have positive values (all of their terms are earth terms).

#### Semantic indexing and clustering with Gensim

Gensim: an open-source vector space modeling and topic modeling toolkit, implemented in the Python programming language

Tutorial examples of topic modelling for humans (LSI): http://radimrehurek.com/gensim/tut2.html

DML-CZ similarity example:

http://dml.cz/handle/10338.dmlcz/500114/SimilarArticles cf. papers similar to famous Otakar Borůvka's paper

Go forth and create masterpieces for semantic indexing applications (by gensim, similarly as others already did ;-)!

# Latent Semantic Indexing (LSI) / Singular Value

- SVD used for dimensionality reduction
- LSI: SVD in information retrieval

Decomposition: The math

- LSI as clustering
- gensim: Topic modelling for humans (practical use of LSI etal.)

#### Resources

- Chapter 18 of IIR
- Resources at https://www.fi.muni.cz/~sojka/PV211/ and http://cislmu.org, materials in MU IS and FI MU library
  - Original paper on latent semantic indexing by Deerwester et al.
  - Paper on probabilistic LSI by Thomas Hofmann
  - Word space: LSI for words