

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 1: Boolean Retrieval Handout version

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(compiled on 2024-06-19 19:15:23)

Take-away

- Basic information about the course, teachers, evaluation, exercises
- Boolean Retrieval: Design and data structures of a simple information retrieval system
- What topics will be covered in this class (overview)?

Overview

- 1 Introduction
- 2 History of information retrieval
- 3 Boolean model
- 4 Inverted index
- 5 Processing queries
- 6 Query optimization
- 7 Course overview and agenda

Start with why (Simon Sinek)

Information retrieval (IR) is **finding** material (**usually documents**) of an **unstructured** nature (usually text) that satisfies an **information need** from within **large collections** (usually stored on computers).

Why important? Why you? Why now?

Information handling on Faculty of informatics in information age. . .

Prerequisites

Curiosity about how Information Retrieval works.

But seriously, based on Manning *et al.* IIR textbook (available in MU libraries):

- Chapters 1–5 benefit from basic course on algorithms and data structures.
- Chapters 6–7 need in addition linear algebra, vectors and dot products.
- For Chapters 11–13 basic probability notions are needed.
- Chapters 18–21 demand course in linear algebra, notions of matrix rank, eigenvalues and eigenvectors.

PV211 course design I

- proactive rather than reactive learning
- diversity is stability, e.g. welcomed
- learning by doing/programming
- skillful rather than bag of facts
- Stanford (TEX, Google, ...) inspired

PV211 course design II

- Mentoring rather than 'ex cathedra' lectures: "The *flipped classroom* is a pedagogical model in which the typical lecture and homework elements of a course are reversed."
- Questions are welcome—on PV211 IS discussion forum *before* lectures, and also *during* lectures.
- Respect to the individual learning speed and knowledge.
- Student [soft skills and programming] activities (answering in discussion forums) are *explicitly welcomed*.
- Richness of materials available in advance: MOOC (Massive open online course) becoming widespread, parts of IIR Stanford courses being available, together with other freely available teaching materials, including the whole IIR book, Google Colab notebooks,

Teachers

- Petr Sojka, sojka@fi.muni.cz
- Consulting hours Spring 2024:
Thursday 8:45–9:30 A502 or by appointment by email.
- Room C523 (or C522), fifth floor, Botanická 68a.
- Course web page:
<https://www.fi.muni.cz/~sojka/PV211/>
- Teaching assistants (TA):
Mgr. Marek Toma 485275@mail.muni.cz,
Ing. Martin Fajčík ifajcik@fit.vutbr.cz,
Santosh Kesiraju, Ph.D. kesiraju@fit.vutbr.cz
Mgr. Michal Štefánik, stefanik.m@mail.muni.cz
RNDr. Vít Starý Novotný, Ph.D. witiko@mail.muni.cz,
Mgr. Šárka Ščavnická, 527352@mail.muni.cz
All TAs are ready for consultations after their teaching hours
or by appointment.

Course Evaluations

Classification is based on points you could get

a) **48 pts** for projects done during the term:

- **10 pts** for the first project
- **6 pts** for giving a peer review
- **26 pts** for the second project
- **6 pts** for the peer review

and

b) **52 pts** for the final exam (multiple-choice test):

- **20 pts** for exercises, similar to those practiced at seminars
- **32 pts** for classical multiple-choice test

Projects evaluation and peer review evaluation I

Until 19. 3. 23:59 (resp. 7. 5. 23:59), your tasks awarded up to **10 pts** resp. **26 pts** will be the following:

Functional implementation of Information Retrieval system:

Individually implement a ranked unsupervised (resp. supervised) retrieval system for Cranfield (resp. ARQMath3) collection.

Readability: Document your code and stick to an organized, consistent, human-readable coding style.

Reaching a minimal score: reach at least 22% (resp. 10%) mean average precision (MAP) score and record it in your Jupyter notebook or in the public leaderboard.

Innovativeness & creativity: Upload an `.ipynb` file with your Jupyter notebook to the homework vault in IS MU.

Projects evaluation and peer review evaluation II

For detailed instructions and an example solution, see the Google Colaboratory document linked from the interactive course syllabus in IS MU.

You will be instructed on the first practical on which institutional computational resources (Jupyter Hub, Google Colab, Deepnote, . . .) you will have at your disposal for solving projects.

Peer review evaluation

For each project, test and fill in a questionnaire about 3 solutions of your peers, including feedback with ideas for further improvements. Between 20. 3. and 26. 3., (resp. 8. 5. and 14. 5.) your task awarded up to $3 \times 2 = \mathbf{6\ pts}$ will be to review the term projects of three of your colleagues. **0.5 pts** will be awarded for handing in a review of your colleague's term project. **1.5 pts** will be awarded for reviewing the completion of tasks in your colleague's term project.

Bonus points motivation I

- You can get extra 10/9/8/.../1/0 point(s) for the 1st/2nd/3rd/.../... 10/11th place in the first project assignment.
- You can get extra 20/18/16/.../2/0 point(s) for the 1st/2nd/3rd/.../... 10/11th place in the second project assignment.
- *In addition*, one can get additional *premium* points based on activities during lectures, practicals (good answers), projects (PV211-utils pull requests), in IS discussion forum, or negotiated related (Kaggle) projects.

Summary of course grading I

Classification scale lower bounds for passing z/k are 48/53 points and E–A grading will be adjusted based on ECTS suggestion in IS (E/D/C/B/A \approx **58/66/74/82/90 pts** . Dates of [final] exams will be announced via IS.muni.cz (at least three terms, probably four).

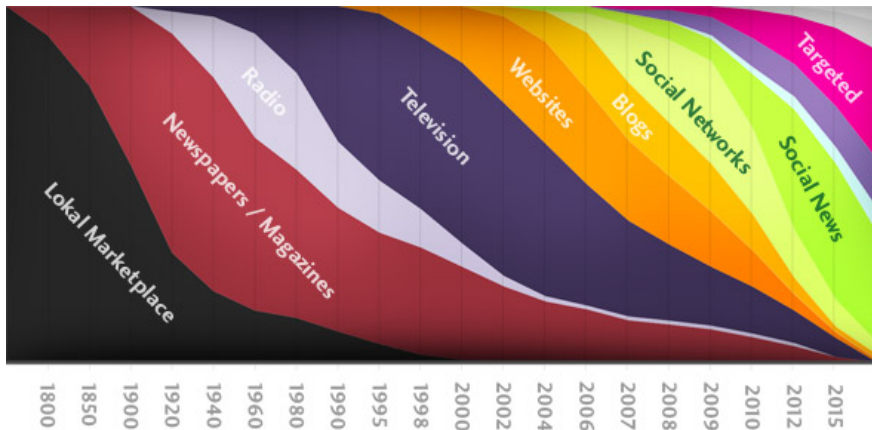
| week/ deadline | pts | description |
|----------------------|-------|--|
| 1–4/ 19. 3. 23:59 | 10 | first assignment project (Cranfield) |
| 5/ 26. 3. 23:59 | 6 | peer review of Cranfield TFIDF |
| 6–11/ 7. 5. 23:59 | 20 | second assignment project (ARQMath3) |
| 6–11/ 7. 5. 23:59 | 6 | for justification and explanation of your solution and code of second assignment |
| 12/ 14. 5. 23:59 | 6 | peer review of explained second project |
| 14+ / exam part 1 | 20 | open exercises, similar to those practiced at seminars |
| 14+ / exam part 2 | 32 | classical multiple-choice test testing understanding of topics taught |
| 1–14+ / extra points | X | extra activities during term or negotiated related projects |
| 14+ / total points | 100+X | points for ECTS gradings |

Can we proceed [Y/N]?

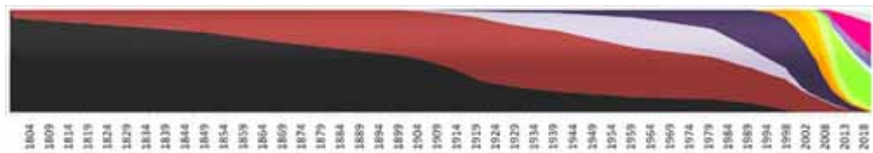
Questions?

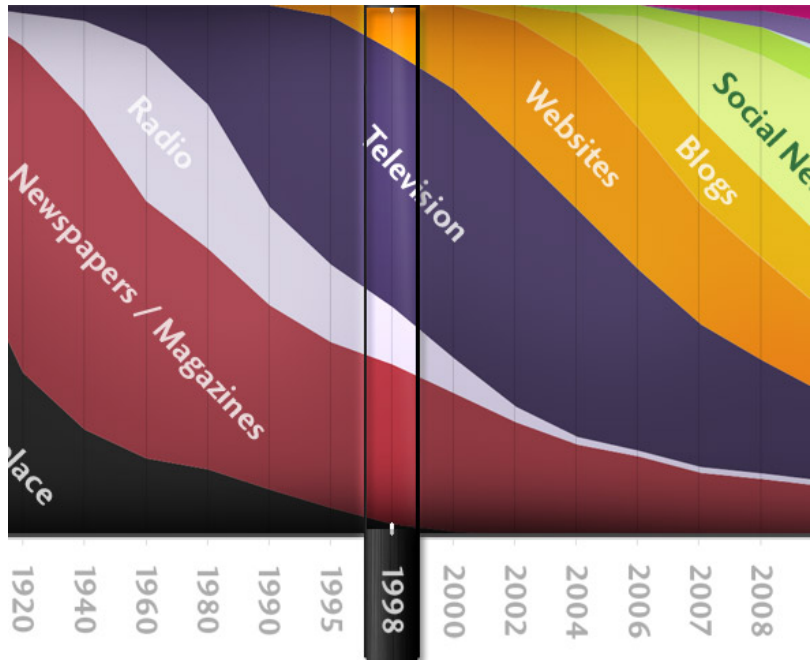
Python? Jupyter Notebook, Jupyter Hub? Google Colab?
Deepnote project? Bc./Mgr./Ph.D.? Mandatory course
z/k/zk? Erasmus? Nationalities: CZ?, SK?, EN=C2 (mother
tongue)?, other? 2 programming projects?/challenges?
Student peer reviews? Mikolov? Řehůřek? Materna?
Jurových? Discord discussion forum with anonymous posts?!

History of *information retrieval*: gradual changes of channels and technologies



Gradual *speedup* of changes in IR





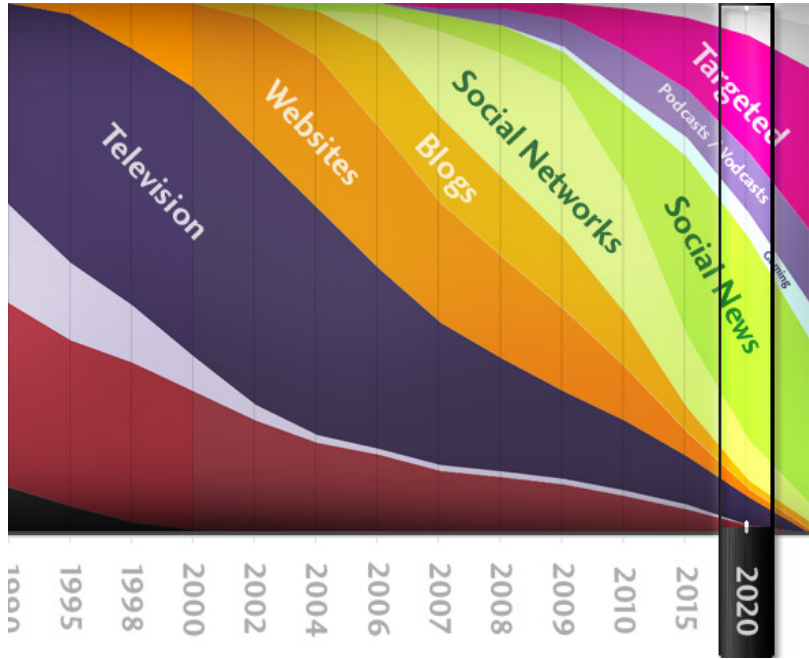
“Google” Circa 1997 (google.stanford.edu)



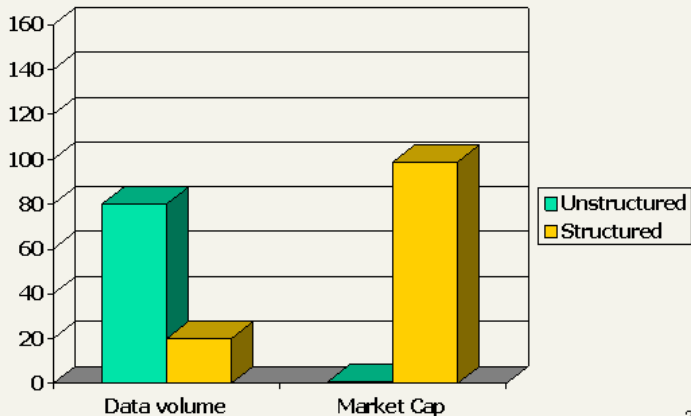
Google

1998: google.stanford.edu

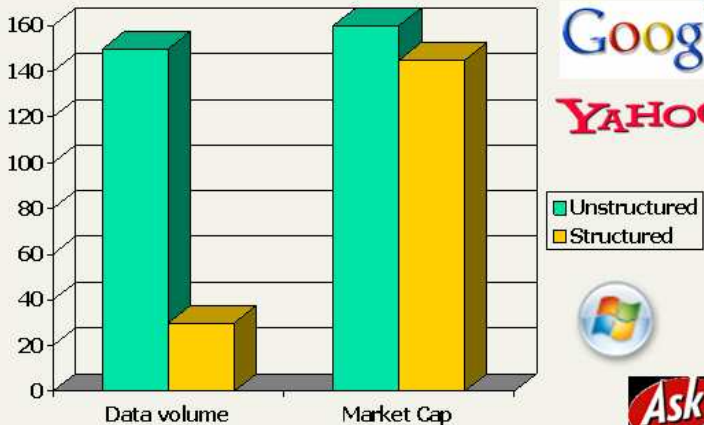
- collaborative project with Stanford faculty ('flipped IS' :-)
- on collected disks in the dormitories
- Google 1998 'Anatomy paper' (Larry Page, Sergey Brin)



Unstructured (text) vs. structured (database) data in 1996



Unstructured (text) vs. structured (database) data in 2006



Google™

YAHOO!



Unstructured (text) versus structured (database) data

in 2016 ?

in 2026 ?

Boolean retrieval

- The Boolean model is arguably the simplest model to base an information retrieval system on.
- Queries are Boolean expressions, e.g., CAESAR AND BRUTUS
- The search engine returns all documents that satisfy the Boolean expression.

Does Google use the Boolean model?

Does Google use the Boolean model?

- On Google, the default interpretation of a query $[w_1 w_2 \dots w_n]$ is w_1 AND w_2 AND \dots AND w_n
- Cases where you get hits that do not contain one of the w_i :
 - anchor text
 - page contains variant of w_i (morphology, spelling correction, synonym)
 - long queries (n large)
 - boolean expression generates very few hits
- Simple Boolean vs. Ranking of result set
 - Simple Boolean retrieval returns matching documents in no particular order.
 - Google (and most well designed Boolean engines) rank the result set – they rank good hits (according to some estimator of relevance) higher than bad hits.

Unstructured data in 1650: collective works of Shakespeare



Unstructured data in 1650

- Which plays of Shakespeare contain the words BRUTUS AND CAESAR, but NOT CALPURNIA?
- One could grep all of Shakespeare's plays for BRUTUS and CAESAR, then strip out lines containing CALPURNIA.
- Why is grep not the solution?
 - Slow (for large collections)
 - grep is line-oriented, IR is document-oriented
 - "NOT CALPURNIA" is non-trivial
 - Other operations (e.g., find the word ROMANS near COUNTRYMAN) not feasible
 - Ranked retrieval (best documents to return) – focus of later lectures, but not this one

Term-document incidence matrix

| | Anthony and Cleopatra | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth | ... |
|-----------|-----------------------------|------------------|----------------|--------|---------|---------|-----|
| ANTHONY | 1 | 1 | 0 | 0 | 0 | 1 | |
| BRUTUS | 1 | 1 | 0 | 1 | 0 | 0 | |
| CAESAR | 1 | 1 | 0 | 1 | 1 | 1 | |
| CALPURNIA | 0 | 1 | 0 | 0 | 0 | 0 | |
| CLEOPATRA | 1 | 0 | 0 | 0 | 0 | 0 | |
| MERCY | 1 | 0 | 1 | 1 | 1 | 1 | |
| WORSER | 1 | 0 | 1 | 1 | 1 | 0 | |

...

Entry is 1 if term occurs. Example: CALPURNIA occurs in *Julius Caesar*.

Entry is 0 if term doesn't occur. Example: CALPURNIA doesn't occur in *The tempest*.

Incidence vectors

- So we have a 0/1 vector for each term.
- To answer the query BRUTUS AND CAESAR AND NOT CALPURNIA:
 - Take the vectors for BRUTUS, CAESAR, and CALPURNIA
 - Complement the vector of CALPURNIA
 - Do a (bitwise) AND on the three vectors
 - $110100 \text{ AND } 110111 \text{ AND } 101111 = 100100$

0/1 vector for BRUTUS

| | Anthony and Cleopatra | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth | ... |
|-----------|-----------------------------|------------------|----------------|--------|---------|---------|-----|
| ANTHONY | 1 | 1 | 0 | 0 | 0 | 1 | |
| BRUTUS | 1 | 1 | 0 | 1 | 0 | 0 | |
| CAESAR | 1 | 1 | 0 | 1 | 1 | 1 | |
| CALPURNIA | 0 | 1 | 0 | 0 | 0 | 0 | |
| CLEOPATRA | 1 | 0 | 0 | 0 | 0 | 0 | |
| MERCY | 1 | 0 | 1 | 1 | 1 | 1 | |
| WORSER | 1 | 0 | 1 | 1 | 1 | 0 | |
| ... | | | | | | | |
| result: | 1 | 0 | 0 | 1 | 0 | 0 | |

Answers to query

Anthony and Cleopatra, Act III, Scene ii

Agrippa [Aside to Domitius Enobarbus]: Why, Enobarbus,
When Antony found Julius **Caesar** dead,
He cried almost to roaring; and he wept
When at Philippi he found **Brutus** slain.

Hamlet, Act III, Scene ii

Lord Polonius: I did enact Julius **Caesar**: I was killed i' the
Capitol; **Brutus** killed me.

Bigger collections

- Consider $N = 10^6$ documents, each with about 1000 tokens
- \Rightarrow total of 10^9 tokens
- On average 6 bytes per token, including spaces and punctuation \Rightarrow size of document collection is about $6 \cdot 10^9 = 6$ GB
- Assume there are $M = 500,000$ distinct terms in the collection
- (Notice that we are making a term/token distinction.)

Can't build the incidence matrix

- $M = 500,000 \times 10^6 =$ half a trillion 0s and 1s.
- But the matrix has no more than one billion 1s.
 - Matrix is extremely sparse.
- What is a better representations?
 - We **only** record the 1s: inverted index!

Inverted index

For each term t , we store a list of all documents that contain t .

BRUTUS →

| | | | | | | | |
|---|---|---|----|----|----|-----|-----|
| 1 | 2 | 4 | 11 | 31 | 45 | 173 | 174 |
|---|---|---|----|----|----|-----|-----|

CAESAR →

| | | | | | | | | |
|---|---|---|---|---|----|----|-----|-----|
| 1 | 2 | 4 | 5 | 6 | 16 | 57 | 132 | ... |
|---|---|---|---|---|----|----|-----|-----|

CALPURNIA →

| | | | |
|---|----|----|-----|
| 2 | 31 | 54 | 101 |
|---|----|----|-----|

⋮

dictionary

postings

Inverted index construction

- 1 Collect the documents to be indexed:

Friends, Romans, countrymen. So let it be with Caesar ...

- 2 Tokenize the text, turning each document into a list of tokens:

Friends Romans countrymen So ...

- 3 Do linguistic preprocessing, producing a list of normalized tokens, which are the indexing terms: friend roman

countryman so ...

- 4 Index the documents that each term occurs in by creating an inverted index, consisting of a dictionary and postings.

Tokenization and preprocessing

Doc 1. I did enact Julius Caesar: I was killed i' the Capitol; Brutus killed me.

Doc 2. So let it be with Caesar. The noble Brutus hath told you Caesar was ambitious:



Doc 1. i did enact julius caesar i was killed i' the capitol brutus killed me

Doc 2. so let it be with caesar the noble brutus hath told you caesar was ambitious

Generate postings

Doc 1. i did enact julius caesar i was
killed i' the capitol brutus killed me
Doc 2. so let it be with caesar the
noble brutus hath told you caesar was
ambitious



| term | docID |
|-----------|-------|
| i | 1 |
| did | 1 |
| enact | 1 |
| julius | 1 |
| caesar | 1 |
| i | 1 |
| was | 1 |
| killed | 1 |
| i' | 1 |
| the | 1 |
| capitol | 1 |
| brutus | 1 |
| killed | 1 |
| me | 1 |
| so | 2 |
| let | 2 |
| it | 2 |
| be | 2 |
| with | 2 |
| caesar | 2 |
| the | 2 |
| noble | 2 |
| brutus | 2 |
| hath | 2 |
| told | 2 |
| you | 2 |
| caesar | 2 |
| was | 2 |
| ambitious | 2 |

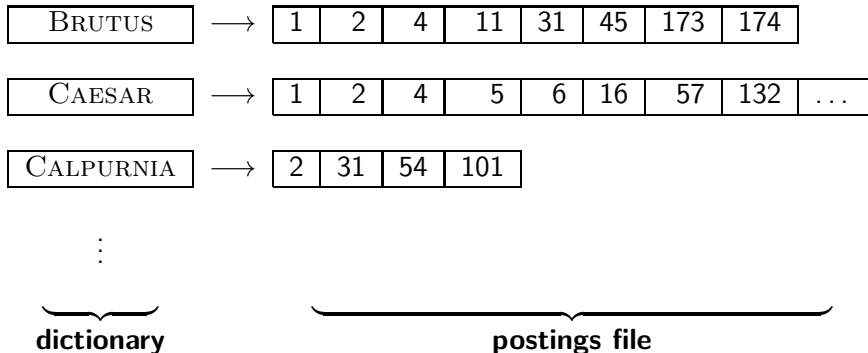
Sort postings

| term | docID | | term | docID |
|-----------|-------|---|-----------|-------|
| i | 1 | | ambitious | 2 |
| did | 1 | | be | 2 |
| enact | 1 | | brutus | 1 |
| julius | 1 | | brutus | 2 |
| caesar | 1 | | capitol | 1 |
| i | 1 | | caesar | 1 |
| was | 1 | | caesar | 2 |
| killed | 1 | | caesar | 2 |
| i' | 1 | | did | 1 |
| the | 1 | | enact | 1 |
| capitol | 1 | | hath | 1 |
| brutus | 1 | | i | 1 |
| killed | 1 | | i | 1 |
| me | 1 | ⇒ | i' | 1 |
| so | 2 | | it | 2 |
| let | 2 | | julius | 1 |
| it | 2 | | killed | 1 |
| be | 2 | | killed | 1 |
| with | 2 | | let | 2 |
| caesar | 2 | | me | 1 |
| the | 2 | | noble | 2 |
| noble | 2 | | so | 2 |
| brutus | 2 | | the | 1 |
| hath | 2 | | the | 2 |
| told | 2 | | told | 2 |
| you | 2 | | you | 2 |
| caesar | 2 | | was | 1 |
| was | 2 | | was | 2 |
| ambitious | 2 | | with | 2 |

Create postings lists, determine document frequency

| term | docID | | term | doc. freq. | → | postings lists |
|-----------|-------|---|-----------|------------|---|----------------|
| ambitious | 2 | | ambitious | 1 | → | 2 |
| be | 2 | | be | 1 | → | 2 |
| brutus | 1 | | brutus | 2 | → | 1 → 2 |
| brutus | 2 | | capitol | 1 | → | 1 |
| capitol | 1 | | caesar | 2 | → | 1 → 2 |
| caesar | 1 | | caesar | 1 | → | 1 |
| caesar | 2 | | did | 1 | → | 1 |
| caesar | 2 | | enact | 1 | → | 1 |
| did | 1 | | hath | 1 | → | 2 |
| enact | 1 | | i | 1 | → | 1 |
| hath | 1 | | i' | 1 | → | 1 |
| i | 1 | ⇒ | it | 1 | → | 2 |
| i | 1 | | julius | 1 | → | 1 |
| i' | 1 | | killed | 1 | → | 1 |
| it | 2 | | let | 1 | → | 2 |
| julius | 1 | | me | 1 | → | 1 |
| killed | 1 | | noble | 1 | → | 2 |
| killed | 1 | | so | 1 | → | 2 |
| let | 1 | | the | 2 | → | 1 → 2 |
| me | 2 | | told | 1 | → | 2 |
| noble | 1 | | you | 1 | → | 2 |
| noble | 2 | | was | 2 | → | 1 → 2 |
| so | 2 | | with | 1 | → | 2 |
| the | 1 | | | | | |
| the | 2 | | | | | |
| told | 2 | | | | | |
| you | 2 | | | | | |
| was | 1 | | | | | |
| was | 2 | | | | | |
| with | 2 | | | | | |

Split the result into dictionary and postings file



Later in this course

- Index construction: how can we create inverted indexes for large collections?
- How much space do we need for dictionary and index?
- Index compression: how can we efficiently store and process indexes for large collections?
- Ranked retrieval: what does the inverted index look like when we want the “best” answer?

Simple conjunctive query (two terms)

- Consider the query: BRUTUS AND CALPURNIA
- To find all matching documents using inverted index:
 - 1 Locate BRUTUS in the dictionary
 - 2 Retrieve its postings list from the postings file
 - 3 Locate CALPURNIA in the dictionary
 - 4 Retrieve its postings list from the postings file
 - 5 Intersect the two postings lists
 - 6 Return intersection to user

Intersecting two postings lists

BRUTUS \longrightarrow 1 \rightarrow 2 \rightarrow 4 \rightarrow 11 \rightarrow 31 \rightarrow 45 \rightarrow 173 \rightarrow 174

CALPURNIA \longrightarrow 2 \rightarrow 31 \rightarrow 54 \rightarrow 101

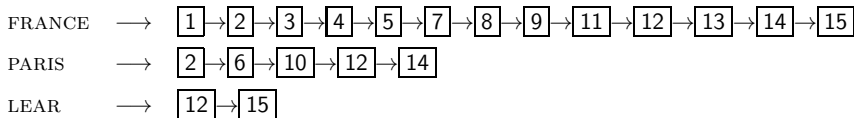
Intersection \implies 2 \rightarrow 31

- This is linear in the length of the postings lists.
- Note: This only works if postings lists are sorted.

Intersecting two postings lists

```
INTERSECT( $p_1, p_2$ )
1  answer  $\leftarrow \langle \rangle$ 
2  while  $p_1 \neq \text{NIL}$  and  $p_2 \neq \text{NIL}$ 
3  do if  $\text{docID}(p_1) = \text{docID}(p_2)$ 
4      then  $\text{ADD}(\text{answer}, \text{docID}(p_1))$ 
5           $p_1 \leftarrow \text{next}(p_1)$ 
6           $p_2 \leftarrow \text{next}(p_2)$ 
7      else if  $\text{docID}(p_1) < \text{docID}(p_2)$ 
8          then  $p_1 \leftarrow \text{next}(p_1)$ 
9          else  $p_2 \leftarrow \text{next}(p_2)$ 
10 return answer
```

Query processing: Exercise



Compute hit list for ((paris AND NOT france) OR lear)

Boolean queries

- The Boolean retrieval model can answer any query that is a Boolean expression.
 - Boolean queries are queries that use AND, OR and NOT to join query terms.
 - Views each document as a [set](#) of terms.
 - Is precise: Document matches condition or not.
- Primary commercial retrieval tool for 3 decades
- Many professional searchers (e.g., lawyers) still like Boolean queries.
 - You know exactly what you are getting.
- Many search systems you use are also Boolean: spotlight, email, intranet, etc.

Commercially successful Boolean retrieval: Westlaw

- Largest commercial legal search service in terms of the number of paying subscribers
- Over half a million subscribers performing millions of searches a day over tens of terabytes of text data
- The service was started in 1975.
- In 2005, Boolean search (called “Terms and Connectors” by Westlaw) was still the default, and used by a large percentage of users . . .
- . . . although ranked retrieval has been available since 1992.

Westlaw: Example queries

Information need: Information on the legal theories involved in preventing the disclosure of trade secrets by employees formerly employed by a competing company

Query: "trade secret" /s disclos! /s prevent /s employe!

Information need: Requirements for disabled people to be able to access a workplace

Query: disab! /p access! /s work-site work-place (employment /3 place)

Information need: Cases about a host's responsibility for drunk guests

Query: host! /p (responsib! liab!) /p (intoxicat! drunk!) /p guest

Westlaw: Comments

- Proximity operators: /3 = within 3 words, /s = within a sentence, /p = within a paragraph
- Space is disjunction, not conjunction! (This was the default in search pre-Google.)
- Long, precise queries: incrementally developed, not like web search
- Why professional searchers often like Boolean search: precision, transparency, control
- When are Boolean queries the best way of searching? Depends on: information need, searcher, document collection,...

Query optimization

- Consider a query that is an AND of n terms, $n > 2$
- For each of the terms, get its postings list, then AND them together
- Example query: BRUTUS AND CALPURNIA AND CAESAR
- What is the best order for processing this query?

Query optimization

- Example query: BRUTUS AND CALPURNIA AND CAESAR
- Simple and effective optimization: **Process in order of increasing frequency**
- Start with the **shortest** postings list, then keep cutting further
- In this example, first CAESAR, then CALPURNIA, then

BRUTUS

BRUTUS → 1 → 2 → 4 → 11 → 31 → 45 → 173 → 174

CALPURNIA → 2 → 31 → 54 → 101

CAESAR → 5 → 31

Optimized intersection algorithm for conjunctive queries

```
INTERSECT( $\langle t_1, \dots, t_n \rangle$ )  
1  terms  $\leftarrow$  SORTBYINCREASINGFREQUENCY( $\langle t_1, \dots, t_n \rangle$ )  
2  result  $\leftarrow$  postings(first(terms))  
3  terms  $\leftarrow$  rest(terms)  
4  while terms  $\neq$  NIL and result  $\neq$  NIL  
5  do result  $\leftarrow$  INTERSECT(result, postings(first(terms)))  
6     terms  $\leftarrow$  rest(terms)  
7  return result
```

More general optimization

- Example query: (MADDING OR CROWD) AND (IGNOBLE OR STRIFE)
- Get frequencies for all terms
- Estimate the size of each OR by the sum of its frequencies (conservative)
- Process in increasing order of OR sizes

Exercise

Recommend a query processing order for: (TANGERINE OR TREES) AND (MARMALADE OR SKIES) AND (KALEIDOSCOPE OR EYES)

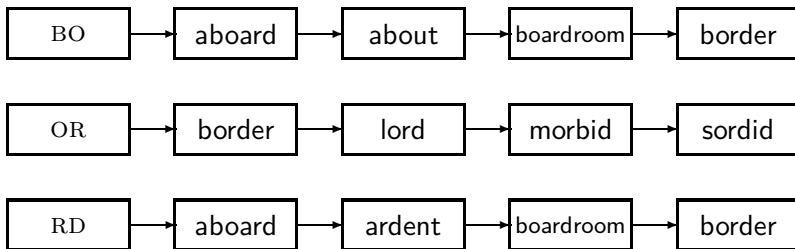
Course overview and agenda

- We are done with Chapter 1 of IIR (IIR 01).
- Plan for the rest of the semester: some 14 of the 21 chapters of IIR (cf. slides from previous years and those planned for this year – comments welcome).
- During weeks 6–9 will probably not be contact lectures but selfstudy from available study materials and recordings from previous years.
- In addition to experts from FI lectures by leading experts are in preparation (probably weeks 5, 10 and 13).
- In what follows: teasers for most chapters – to give you a sense of what will be covered.
- One or two bonus invited lecture(s), and lecture(s) on IR topics researched in research group MIR.fi.muni.cz and on state-of-the art achievements in the area (vector space embeddings, transformers, Neural AI 4 IR, etc.).

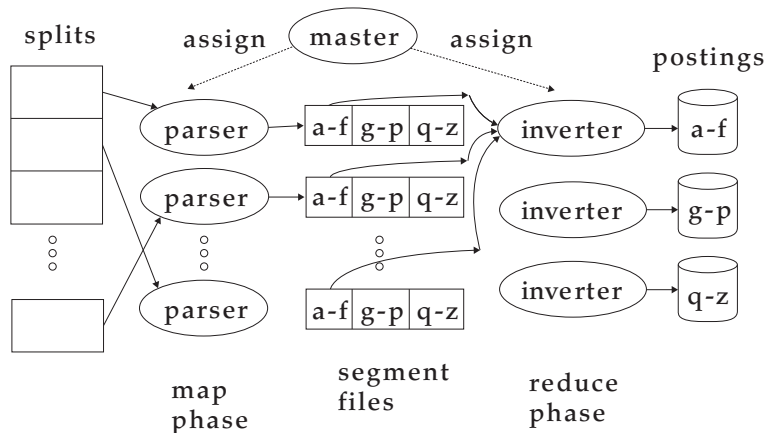
Week 2 – IIR 02: The term vocabulary and postings lists

- Phrase queries: “STANFORD UNIVERSITY”
- Proximity queries: GATES NEAR MICROSOFT
- We need an index that captures **position information** for phrase queries and proximity queries.

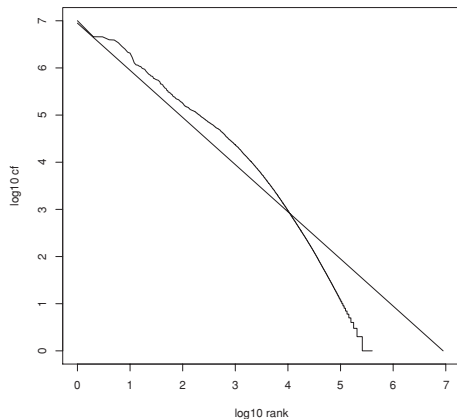
Week 2 – IIR 03: Dictionaries and tolerant retrieval



Week 3 – IIR 04: Index construction



Week 4 – IIR 05: Index compression

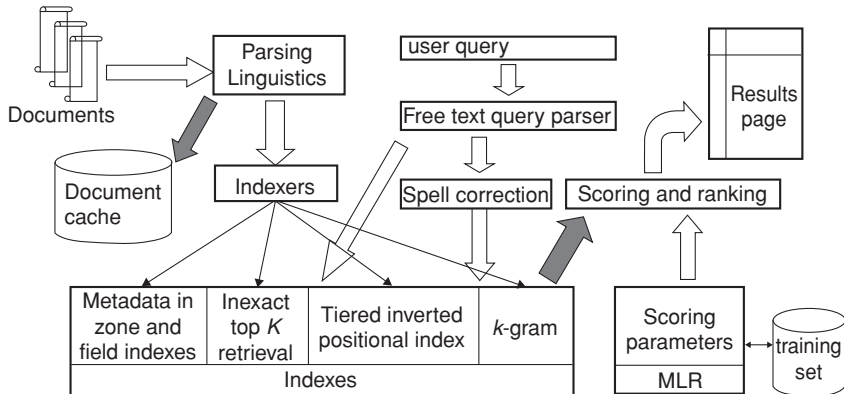


Zipf's law

Week 4 – IIR 06: Scoring, term weighting and the vector space model

- Ranking search results
 - Boolean queries only give inclusion or exclusion of documents.
 - For ranked retrieval, we measure the proximity between the query and each document.
 - One formalism for doing this: [the vector space model](#)
- Key challenge in ranked retrieval: evidence accumulation for a term in a document
 - 1 vs. 0 occurrence of a query term in the document
 - 3 vs. 2 occurrences of a query term in the document
 - Usually: more is better
 - But by how much?
 - Need a scoring function that translates frequency into score or weight

Week 5 – IIR 07: Scoring in a complete search system



Week 5 – IIR 08: Evaluation and dynamic summaries

[Advanced Search](#)

Web [+ Show options...](#)

Results 1 - 11

[Manitoba - Wikipedia, the free encyclopedia](#)

Manitoba's capital and **largest city**, Winnipeg, According to Environment Canada, **Manitoba** ranked first for clearest skies year round, and ranked **second ...**

[Geography](#) - [History](#) - [Demographics](#) - [Economy](#)
en.wikipedia.org/wiki/Manitoba - [Cached](#) - [Similar](#)

[List of cities in Canada - Wikipedia, the free encyclopedia](#)

Cities and towns in **Manitoba**. See also: List of communities in **Manitoba** Dartmouth - formerly the **second largest city** in Nova Scotia, now a Metropolitan ...

en.wikipedia.org/wiki/List_of_cities_in_Canada - [Cached](#) - [Similar](#)

[+ Show more results from en.wikipedia.org](#)

[Canadian Immigration Information - Manitoba](#)

The **largest city** in the province is the capital, Winnipeg, with a population exceeding 706900. The **second largest city** is Brandon. **Manitoba** has received ...

www.canadavisa.com/about-manitoba.html - [Cached](#) - [Similar](#)

[CBC Manitoba | EAL](#)

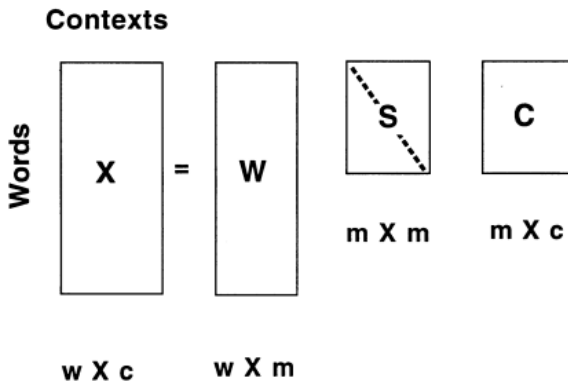
Lesson 57: Brandon - **Manitoba's Second Largest City**. For Teachers; For Students. Step One Open the Lesson: PDF (194kb) PDF WORD (238kb) Microsoft Word ...

www.cbc.ca/manitoba/.../lesson-57-brandon---manitobas-second-largest.html - [Cached](#)

Week 6 – Anatomy of the web-scale IR system

Challenges in Building Large-Scale Information Retrieval Systems
by Jeff Dean, Google Senior Fellow, jeff@google.com

Week 7 – IIR 18: Latent Semantic Indexing



Week 7 – CS276 14: Distributed Word Representations for Information retrieval

Introduction to Information Retrieval

Distributional similarity based representations

- You can get a lot of value by representing a word by means of its neighbors
- “You shall know a word by the company it keeps”
 - (J. R. Firth 1957: 11)
- One of the most successful ideas of modern statistical NLP



...government debt problems turning into **banking** crises as happened in 2009...













...saying that Europe needs unified **banking** regulation to replace the hodgepodge...

...India has just given its **banking** system a shot in the arm...

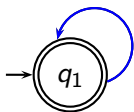
↩ These words will represent *banking* ↗

Week 8 – IIR 09: Relevance feedback & query expansion

[Browse](#)
[Search](#)
[Prev](#)
[Next](#)
[Random](#)

| | | | | | |
|---|---|---|---|--|---|
|  |  |  |  |  |  |
| (144458, 523493) 0.54182 0.231944 0.309876 | (144458, 523835) 0.56319296 0.267304 0.295889 | (144458, 523529) 0.584279 0.280881 0.303398 | (144456, 253569) 0.64501 0.351395 0.293615 | (144456, 253568) 0.630275 0.411745 0.23853 | (144458, 523799) 0.66709197 0.358033 0.309059 |
|  |  |  |  |  |  |
| (144473, 16249) 0.6721 0.393922 0.278178 | (144456, 249634) 0.675018 0.4639 0.211118 | (144456, 253693) 0.676901 0.47645 0.200451 | (144473, 16328) 0.700339 0.309002 0.391337 | (144483, 265264) 0.70170796 0.36176 0.339948 | (144478, 512410) 0.70297 0.469111 0.233859 |

IIR 12: Language models



| w | $P(w q_1)$ | w | $P(w q_1)$ |
|------|------------|-------|------------|
| STOP | 0.2 | toad | 0.01 |
| the | 0.2 | said | 0.03 |
| a | 0.1 | likes | 0.02 |
| frog | 0.01 | that | 0.04 |
| | | ... | ... |

This is a one-state probabilistic finite-state automaton – a **unigram language model** – and the state emission distribution for its one state q_1 .

STOP is not a word, but a special symbol indicating that the automaton stops.

frog said that toad likes frog STOP

$$\begin{aligned}
 P(\text{string}) &= 0.01 \cdot 0.03 \cdot 0.04 \cdot 0.01 \cdot 0.02 \cdot 0.01 \cdot 0.2 \\
 &= 0.00000000000048
 \end{aligned}$$

Week 8 – IIR 13: Text classification & Naive Bayes

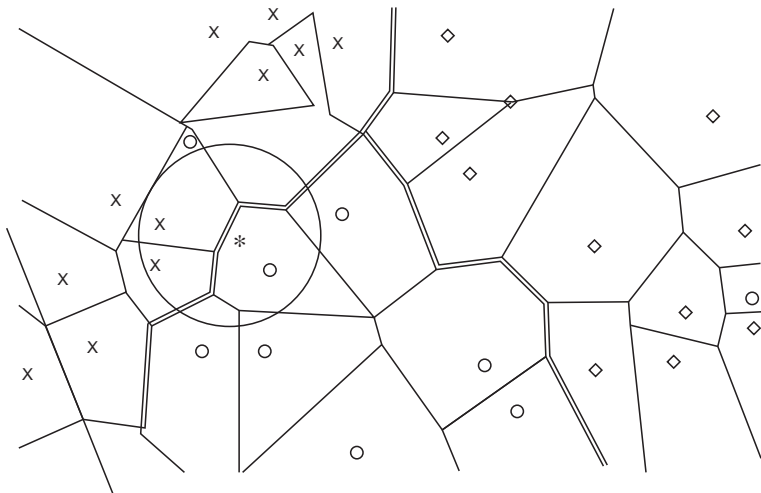
- Text classification = assigning documents automatically to predefined classes
- Examples:
 - Language (English vs. French)
 - Adult content
 - Region

NO week this term IIR 11: Probabilistic information retrieval

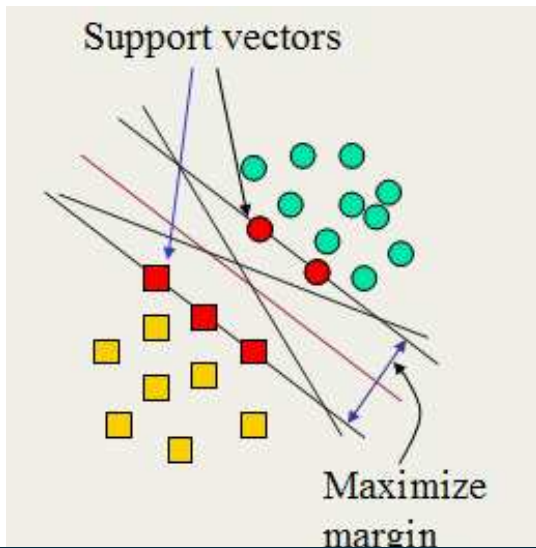
| | document | relevant ($R = 1$) | nonrelevant ($R = 0$) |
|--------------|-----------|----------------------|-------------------------|
| Term present | $x_t = 1$ | p_t | u_t |
| Term absent | $x_t = 0$ | $1 - p_t$ | $1 - u_t$ |

$$O(R|\vec{q}, \vec{x}) = O(R|\vec{q}) \cdot \prod_{t:x_t=q_t=1} \frac{p_t}{u_t} \cdot \prod_{t:x_t=0,q_t=1} \frac{1-p_t}{1-u_t} \quad (1)$$

Week 9 – IIR 14: Vector classification, kNN search



Week 10 – IIR 15: Support vector machines, Learning to rank



Week 11 – IIR 16: Flat clustering

Vivísimo [Advanced Search](#)
[Search](#) [Help](#)

Clustered Results Top 208 results of at least 20,373,974 retrieved for the query **jaguar** ([Details](#))

- ▶ [jaguar](#) (208)
 - ▶ [Cars](#) (74)
 - ▶ [Club](#) (34)
 - ▶ [Cat](#) (23)
 - ▶ [Animal](#) (13)
 - ▶ [Restoration](#) (10)
 - ▶ [Mac OS X](#) (8)
 - ▶ [Jaguar Model](#) (8)
 - ▶ [Request](#) (5)
 - ▶ [Mark Webber](#) (6)
 - ▶ [Maya](#) (5)
 - ▼ [More](#)

Find in clusters:

1. [Jag-lovers - THE source for all Jaguar information](#) [\[new window\]](#) [\[frame\]](#) [\[cache\]](#) [\[preview\]](#) [\[clusters\]](#)
 ... Internet! Serving Enthusiasts since 1993 The Jag-lovers Web Currently with 40661 members The Premier **Jaguar** Cars web resource for all enthusiasts Lists and Forums Jag-lovers originally evolved around its ...
[www.jag-lovers.org](#) - Open Directory 2, Wisenut 8, Ask Jeeves 8, MSN 9, Looksmart 12, MSN Search 18
2. [Jaguar Cars](#) [\[new window\]](#) [\[frame\]](#) [\[cache\]](#) [\[preview\]](#) [\[clusters\]](#)
 [...] redirected to [www.jaguar.com](#)
[www.jaguarcars.com](#) - Looksmart 1, MSN 2, Lycos 3, Wisenut 6, MSN Search 9, MSN 29
3. [http://www.jaguar.com/](#) [\[new window\]](#) [\[frame\]](#) [\[preview\]](#) [\[clusters\]](#)
[www.jaguar.com](#) - MSN 1, Ask Jeeves 1, MSN Search 3, Lycos 9
4. [Apple - Mac OS X](#) [\[new window\]](#) [\[frame\]](#) [\[preview\]](#) [\[clusters\]](#)
 Learn about the new OS X Server, designed for the Internet, digital media and workgroup management. Download a technical factsheet.
[www.apple.com/macosx](#) - Wisenut 1, MSN 3, Looksmart 25

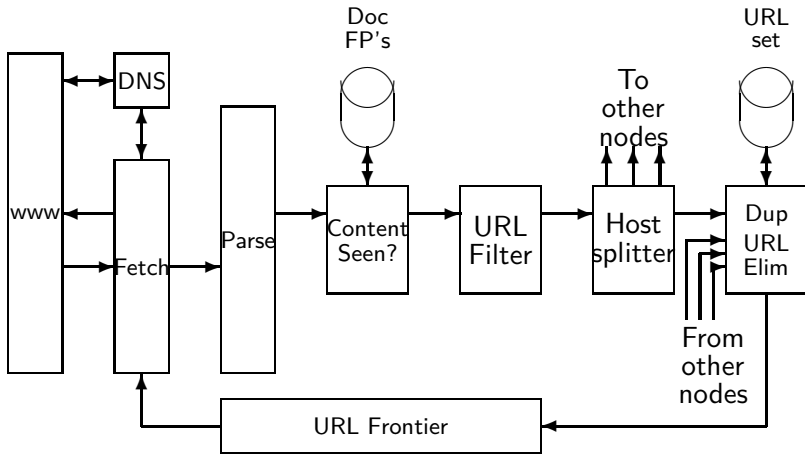
NO week this term – IIR 17: Hierarchical clustering

`http://news.google.com`

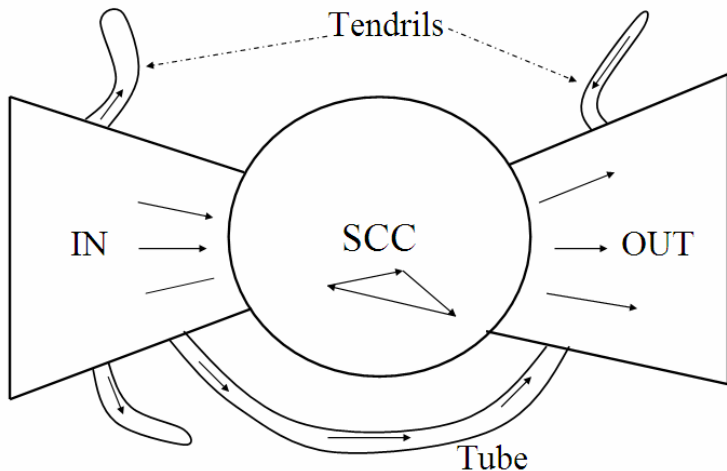
Week 12 – IIR 19: The web and its challenges

- Unusual and diverse documents
- Unusual and diverse users and information needs
- Beyond terms and text: exploit link analysis, user data
- How do web search engines work?
- How can we make them better?

Week 12 – IIR 20: Crawling



Week 13 – IIR 21: Link analysis / PageRank



Week 1 – Week 13: Related research seminars and courses

Seminar FI:PV212 of LEMMA/MIR labs.

- MIR group's solution for ARQMath 2022 @ CLEF2022 tasks: Math information Retrieval Question Answering and Formula searching
- Talks and brainstormings of TA's and FI MU alumni's talks (Řehůřek, Materna, Jurových, . . .)?
- Informatics colloquium related talk(s): Tomáš Mikolov 2019, or in 2017.

MU on Coursera

Take-away

- Basic information about the course, teachers, evaluation, exercises
- Boolean Retrieval: Design and data structures of a simple information retrieval system
- What topics will be covered in this class (overview)?

Resources

- Chapter 1 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - course schedule and overview
 - IIR textbook and other books (Baeta-Yates et al: Modern Information Retrieval, and other passed on during the lecture)
 - Jupyter Hub/ Google Colab/ Deepnote environments with examples

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 2: The term vocabulary and postings lists Handout version

Petr Sojka, Hinrich Schütze et al.

Faculty of Informatics, Masaryk University, Brno
Center for Information and Language Processing, University of Munich

2024-02-28

(compiled on 2024-02-28 13:56:59)

Overview

- 1 Recap
- 2 Documents
- 3 Terms
 - General + Non-English
 - English
- 4 Skip pointers
- 5 Phrase queries

Inverted index

For each term t , we store a list of all documents that contain t .

BRUTUS → 1 | 2 | 4 | 11 | 31 | 45 | 173 | 174

CAESAR → 1 | 2 | 4 | 5 | 6 | 16 | 57 | 132 | ...

CALPURNIA → 2 | 31 | 54 | 101

⋮


dictionary


postings

Westlaw: Example queries

Information need: Information on the legal theories involved in preventing the disclosure of trade secrets by employees formerly employed by a competing company

Query: "trade secret" /s disclos! /s prevent /s employe!

Information need: Requirements for disabled people to be able to access a workplace

Query: disab! /p access! /s work-site work-place (employment /3 place)

Information need: Cases about a host's responsibility for drunk guests

Query: host! /p (responsib! liab!) /p (intoxicat! drunk!) /p guest

Does Google use the Boolean model?

- On Google, the default interpretation of a query $[w_1 w_2 \dots w_n]$ is w_1 AND w_2 AND \dots AND w_n
- Cases where you get hits that do not contain one of the w_i :
 - anchor text
 - page contains variant of w_i (morphology, spelling correction, synonym)
 - long queries (n large)
 - boolean expression generates very few hits
- Simple Boolean vs. Ranking of result set
 - Simple Boolean retrieval returns matching documents in no particular order.
 - Google (and most well designed Boolean engines) rank the result set – they rank good hits (according to some estimator of relevance) higher than bad hits.

Take-away

- Understanding of the basic unit of classical information retrieval systems: **words** and **documents**: What is a document, what is a term?
- Tokenization: how to get from raw text to words (or tokens)
- More complex indexes: skip pointers and phrases

Major steps in inverted index construction

- 1 Collect the documents to be indexed.
- 2 Tokenize the text.
- 3 Do linguistic preprocessing of tokens.
- 4 Index the documents that each term occurs in.

Documents

- Last lecture: Simple Boolean retrieval system
- Our assumptions were:
 - We know what a document is.
 - We can “machine-read” each document.
- This can be complex in reality: “God is in the details.”
(Mies van der Rohe)

Parsing a document

- We need to deal with format and language of each document.
- What format is it in? pdf, word, excel, html, etc.
- What language is it in?
- What character set is in use?
- Each of these is a classification problem, which we will study later in this course (IIR 13).
- Alternative: use heuristics

Format/Language: Complications

- A single index usually contains terms of several languages.
- Sometimes a document or its components contain multiple languages/formats.
 - French email with Spanish pdf attachment
- What is the document unit for indexing?
- A file?
- An email?
- An email with 5 attachments?
- A group of files (ppt or latex in HTML)?
- Upshot: Answering the question “what is a document?” is not trivial and requires some design decisions.
- Also: XML

Definitions

- **Word** – A delimited string of characters as it appears in the text.
- **Term** – A “normalized” word (case, morphology, spelling, etc.); an equivalence class of words.
- **Token** – An instance of a word or term occurring in a document.
- **Type** – The same as term in most cases: an equivalence class of tokens. More informally: what we consider same in the index, e.g. abstraction of a line in the incidence matrix.

Normalization

- Need to “normalize” words in indexed text as well as query terms into the same form.
- Example: We want to match *U.S.A.* and *USA*
- We most commonly implicitly define **equivalence classes** of terms.
- Alternatively: do asymmetric expansion
 - window → window, windows
 - windows → Windows, windows
 - Windows (no expansion)
- More powerful, but less efficient
- Why don't you want to put *window*, *Window*, *windows*, and *Windows* in the same equivalence class?

Normalization: Other languages

- Normalization and language detection interact.
- *PETER WILL NICHT MIT.* → MIT = mit
- *He got his PhD from MIT.* → MIT ≠ mit

Recall: Inverted index construction

- Input:

Friends, Romans, countrymen. So let it be with Caesar ...

- Output:

friend roman countryman so ...

- Each token is a candidate for a postings entry.
- What are valid tokens to emit?

Exercises

In June, the dog likes to chase the cat in the barn. – How many word tokens? How many word types?

Why tokenization is difficult – even in English. **Tokenize:** *Mr. O'Neill thinks that the boys' stories about Chile's capital aren't amusing.*

Tokenization problems: One word or two? (or several)

- Hewlett-Packard
- State-of-the-art
- co-education
- the hold-him-back-and-drag-him-away maneuver
- data base
- San Francisco
- Los Angeles-based company
- cheap San Francisco-Los Angeles fares
- York University vs. New York University

Numbers

- 22/02/22
- 2022-02-22
- Feb 22, 2022
- B-52
- 100.2.86.144
- (800) 234-2333
- 800.234.2333
- Older IR systems may not index numbers . . .
- . . . but generally it's a useful feature.
- Google example (1+1)

Chinese: No whitespace

莎拉波娃现在居住在美国东南部的佛罗里达。今年4月9日，莎拉波娃在美国第一大城市纽约度过了18岁生日。生日派对上，莎拉波娃露出了甜美的微笑。

Ambiguous segmentation in Chinese

The two characters can be treated as one word meaning 'monk' or as a sequence of two words meaning 'and' and 'still'.

Other cases of “no whitespace”

- Compounds in Dutch, German, Swedish, Czech (čistokapsonosoplena)
- Computerlinguistik → Computer + Linguistik
- Lebensversicherungsgesellschaftsangestellter
- → leben + versicherung + gesellschaft + angestellter
- Inuit: tusaatsiarunnangittualuujunga (I can't hear very well.)
- Many other languages with segmentation difficulties: Finnish, Urdu, . . .

Japanese

ノーベル平和賞を受賞したワンガリ・マータイさんが名誉会長を務めるMOTTAINAIキャンペーンの一環として、毎日新聞社とマガジンハウスは「私の、もったいない」を募集します。皆様が日ごろ「もったいない」と感じて実践していることや、それにまつわるエピソードを800字以内の文章にまとめ、簡単な写真、イラスト、図などを添えて10月20日までにお送りください。大賞受賞者には、50万円相当の旅行券とエコ製品2点の副賞が贈られます。

4 different “alphabets”: Chinese characters, hiragana syllabary for inflectional endings and function words, katakana syllabary for transcription of foreign words and other uses, and latin. No spaces (as in Chinese).

End user can express query entirely in hiragana!

Arabic script

ك ت ا ب ← كِتَابٌ
un b ā t i k
/kitābun/ ‘*a book*’

Arabic script: Bidirectionality

استقلت الجزائر في سنة 1962 بعد 132 عاما من الاحتلال الفرنسي.

← → ← →

← START

‘Algeria achieved its independence in 1962 after 132 years of French occupation.’

Bidirectionality is not a problem if text is coded in Unicode.

Accents and diacritics

- Accents: résumé vs. resume (simple omission of accent)
- Umlauts: Universität vs. Universitaet (substitution with special letter sequence “ae”)
- Most important criterion: How are users likely to write their queries for these words?
- Even in languages that standardly have accents, users often do not type them. (Polish?)

Case folding

- Reduce all letters to lower case
- Even though case can be semantically meaningful
 - capitalized words in mid-sentence
 - MIT vs. mit
 - Fed vs. fed
 - ...
- It's often best to lowercase everything since users will use lowercase regardless of correct capitalization.

Stop words

- stop words = extremely common words which would appear to be of little value in helping to select documents matching a user need
- Examples: *a, an, and, are, as, at, be, by, for, from, has, he, in, is, it, its, of, on, that, the, to, was, were, will, with*
- Stop word elimination used to be standard in older IR systems.
- But you need stop words for phrase queries, e.g. “King of Denmark”.
- Most web search engines index stop words.

More equivalence classing

- Soundex: IIR 3 (phonetic equivalence, Muller = Mueller)
- Thesauri: IIR 9 (semantic equivalence, car = automobile)

Lemmatization

- Reduce inflectional/variant forms to base form
- Example: *am, are, is* → *be*
- Example: *car, cars, car's, cars'* → *car*
- Example: *the boy's cars are different colors* → *the boy car be different color*
- Lemmatization implies doing “proper” reduction to dictionary headword form (the [lemma](#)).
- Inflectional morphology (*cutting* → *cut*) vs. derivational morphology (*destruction* → *destroy*)

Stemming

- Definition of stemming: Crude heuristic process that **chops off the ends of words** in the hope of achieving what “principled” lemmatization attempts to do with a lot of linguistic knowledge.
- Language dependent
- Often inflectional **and** derivational
- Example for derivational: *automate*, *automatic*, *automation* all reduce to *automat*

Porter algorithm

- Most common algorithm for stemming English
- Results suggest that it is at least as good as other stemming options
- Conventions + 5 phases of reductions
- Phases are applied sequentially
- Each phase consists of a set of commands.
 - Sample command: Delete final *ement* if what remains is longer than 1 character
 - replacement → replac
 - cement → cement
- Sample convention: Of the rules in a compound command, select the one that applies to the longest suffix.

Porter stemmer: A few rules

Rule

SSSES → SS

IES → I

SS → SS

S →

Example

caresses → caress

ponies → poni

caress → caress

cats → cat

Three stemmers: A comparison

Sample text: Such an analysis can reveal features that are not easily visible from the variations in the individual genes and can lead to a picture of expression that is more biologically transparent and accessible to interpretation

Porter stemmer: such an analysi can reveal featur that ar not easili visibl from the variat in the individu gene and can lead to a pictur of express that is more biolog transpar and access to interpret

Lovins stemmer: such an analys can reve featur that ar not eas vis from th vari in th individu gen and can lead to a pictur of expres that is mor biolog transpar and acces to interpres

Paice stemmer: such an analys can rev feat that are not easy vis from the vary in the individ gen and can lead to a pict of express that is mor biolog transp and access to interpret

Does stemming improve effectiveness?

- In general, stemming increases effectiveness for some queries, and decreases effectiveness for others.
- Queries where stemming is likely to help: [tartan sweaters], [sightseeing tour san francisco]
- (equivalence classes: {sweater,sweaters}, {tour,tours})
- Porter Stemmer equivalence class *oper* contains all of *operate operating operates operation operative operatives operational*.
- Queries where stemming hurts: [operational AND research], [operating AND system], [operative AND dentistry]

Exercise: What does Google do?

- Stop words
- Normalization
- Tokenization
- Lowercasing
- Stemming
- Non-latin alphabets
- Umlauts
- Compounds
- Numbers

Recall basic intersection algorithm

BRUTUS \rightarrow 1 \rightarrow 2 \rightarrow 4 \rightarrow 11 \rightarrow 31 \rightarrow 45 \rightarrow 173 \rightarrow 174

CALPURNIA \rightarrow 2 \rightarrow 31 \rightarrow 54 \rightarrow 101

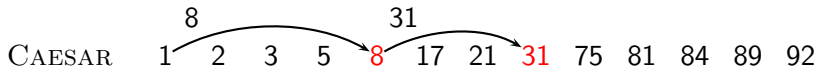
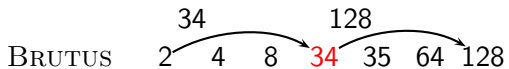
Intersection \Rightarrow 2 \rightarrow 31

- Linear in the length of the postings lists.
- Can we do better?

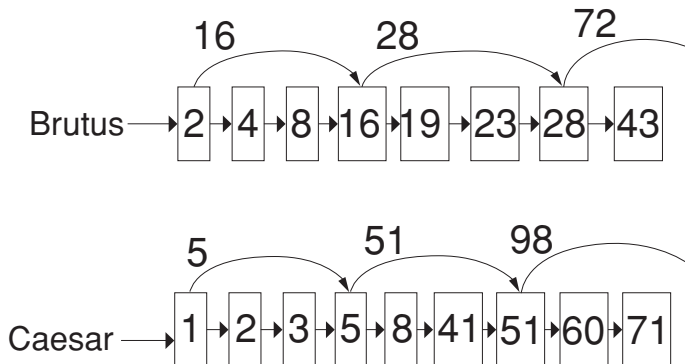
Skip pointers

- Skip pointers allow us to **skip** postings that will not figure in the search results.
- This makes intersecting postings lists more efficient.
- Some postings lists contain several million entries – so efficiency can be an issue even if basic intersection is linear.
- Where do we put skip pointers?
- How do we make sure intersection results are correct?

Basic idea



Skip lists: Larger example



Intersecting with skip pointers

```
INTERSECTWITHSKIPS( $p_1, p_2$ )
1  answer  $\leftarrow \langle \rangle$ 
2  while  $p_1 \neq \text{NIL}$  and  $p_2 \neq \text{NIL}$ 
3  do if  $\text{docID}(p_1) = \text{docID}(p_2)$ 
4      then  $\text{ADD}(\text{answer}, \text{docID}(p_1))$ 
5           $p_1 \leftarrow \text{next}(p_1)$ 
6           $p_2 \leftarrow \text{next}(p_2)$ 
7  else if  $\text{docID}(p_1) < \text{docID}(p_2)$ 
8      then if  $\text{hasSkip}(p_1)$  and  $(\text{docID}(\text{skip}(p_1)) \leq \text{docID}(p_2))$ 
9          then while  $\text{hasSkip}(p_1)$  and  $(\text{docID}(\text{skip}(p_1)) \leq \text{docID}(p_2))$ 
10             do  $p_1 \leftarrow \text{skip}(p_1)$ 
11             else  $p_1 \leftarrow \text{next}(p_1)$ 
12     else if  $\text{hasSkip}(p_2)$  and  $(\text{docID}(\text{skip}(p_2)) \leq \text{docID}(p_1))$ 
13         then while  $\text{hasSkip}(p_2)$  and  $(\text{docID}(\text{skip}(p_2)) \leq \text{docID}(p_1))$ 
14             do  $p_2 \leftarrow \text{skip}(p_2)$ 
15             else  $p_2 \leftarrow \text{next}(p_2)$ 
16 return answer
```

Where do we place skips?

- Tradeoff: number of items skipped vs. frequency skip can be taken
- More skips: Each skip pointer skips only a few items, but we can frequently use it.
- Fewer skips: Each skip pointer skips many items, but we can not use it very often.

Where do we place skips? (cont)

- Simple heuristic: for postings list of length P , use \sqrt{P} evenly-spaced skip pointers.
- This ignores the distribution of query terms.
- Easy if the index is static; harder in a dynamic environment because of updates.
- How much do skip pointers help?
- They used to help a lot.
- With today's fast CPUs, they don't help that much anymore.

Phrase queries

- We want to answer a query such as [Masaryk university] – as a phrase.
- Thus *The president Tomáš Garrigue Masaryk never went to Stanford university* should **not** be a match.
- The concept of phrase query has proven easily understood by users.
- About 10% of web queries are phrase queries.
- Consequence for inverted index: it no longer suffices to store docIDs in postings lists.
- Two ways of extending the inverted index:
 - biword index
 - positional index
 - **Any ideas?**

Biword indexes

- Index every consecutive pair of terms in the text as a phrase.
- For example, *Friends, Romans, Countrymen* would generate two biwords: “*friends romans*” and “*romans countrymen*”
- Each of these biwords is now a vocabulary term.
- Two-word phrases can now easily be answered.

Longer phrase queries

- A long phrase like “*masaryk university brno*” can be represented as the Boolean query “MASARYK UNIVERSITY” AND “UNIVERSITY BRNO”
- We need to do post-filtering of hits to identify subset that actually contains the 3-word phrase.

Issues with biword indexes

- Why are biword indexes rarely used?
- False positives, as noted above
- Index blowup due to very large term vocabulary

Positional indexes

- Positional indexes are a more efficient alternative to biword indexes.
- Postings lists in a **nonpositional** index: each posting is just a docID
- Postings lists in a **positional** index: each posting is a docID and a **list of positions**

Positional indexes: Example

Query: "to₁ be₂ or₃ not₄ to₅ be₆"

TO, 993427:

- 1: ⟨7, 18, 33, 72, 86, 231⟩;
- 2: ⟨1, 17, 74, 222, 255⟩;
- 4: ⟨8, 16, 190, 429, 433⟩;
- 5: ⟨363, 367⟩;
- 7: ⟨13, 23, 191⟩; ...

BE, 178239:

- 1: ⟨17, 25⟩;
- 4: ⟨17, 191, 291, 430, 434⟩;
- 5: ⟨14, 19, 101⟩; ...

Document 4 is a match!

Exercise

Shown below is a portion of a positional index in the format: term: doc1: \langle position1, position2, ... \rangle ; doc2: \langle position1, position2, ... \rangle ; etc.

ANGELS: 2: \langle 36,174,252,651 \rangle ; 4: \langle 12,22,102,432 \rangle ; 7: \langle 17 \rangle ;
FOOLS: 2: \langle 1,17,74,222 \rangle ; 4: \langle 8,78,108,458 \rangle ; 7: \langle 3,13,23,193 \rangle ;
FEAR: 2: \langle 87,704,722,901 \rangle ; 4: \langle 13,43,113,433 \rangle ; 7: \langle 18,328,528 \rangle ;
IN: 2: \langle 3,37,76,444,851 \rangle ; 4: \langle 10,20,110,470,500 \rangle ; 7: \langle 5,15,25,195 \rangle ;
RUSH: 2: \langle 2,66,194,321,702 \rangle ; 4: \langle 9,69,149,429,569 \rangle ; 7: \langle 4,14,404 \rangle ;
TO: 2: \langle 47,86,234,999 \rangle ; 4: \langle 14,24,774,944 \rangle ; 7: \langle 19,319,599,709 \rangle ;
TREAD: 2: \langle 57,94,333 \rangle ; 4: \langle 15,35,155 \rangle ; 7: \langle 20,320 \rangle ;
WHERE: 2: \langle 67,124,393,1001 \rangle ; 4: \langle 11,41,101,421,431 \rangle ; 7: \langle 16,36,736 \rangle ;

Which document(s) if any match each of the following two queries, where each expression within quotes is a phrase query?: “fools rush in”, “fools rush in” AND “angels fear to tread”

Proximity search

- We just saw how to use a positional index for phrase searches.
- We can also use it for proximity search.
- For example: `employment /4 place`
- Find all documents that contain `EMPLOYMENT` and `PLACE` within 4 words of each other.
- *Employment agencies that place healthcare workers are seeing growth* is a hit.
- *Employment agencies that have learned to adapt now place healthcare workers* is not a hit.

Proximity search

- Use the positional index
- Simplest algorithm: look at cross-product of positions of (i) EMPLOYMENT in document and (ii) PLACE in document
- Very inefficient for frequent words, especially stop words
- Note that we want to return the actual matching positions, not just a list of documents.
- This is important for dynamic summaries, etc.

“Proximity” intersection

```

POSITIONALINTERSECT( $p_1, p_2, k$ )
1  answer  $\leftarrow \langle \rangle$ 
2  while  $p_1 \neq \text{NIL}$  and  $p_2 \neq \text{NIL}$ 
3  do if  $\text{docID}(p_1) = \text{docID}(p_2)$ 
4      then  $l \leftarrow \langle \rangle$ 
5           $pp_1 \leftarrow \text{positions}(p_1)$ 
6           $pp_2 \leftarrow \text{positions}(p_2)$ 
7          while  $pp_1 \neq \text{NIL}$ 
8          do while  $pp_2 \neq \text{NIL}$ 
9              do if  $|\text{pos}(pp_1) - \text{pos}(pp_2)| \leq k$ 
10                 then  $\text{ADD}(l, \text{pos}(pp_2))$ 
11                 else if  $\text{pos}(pp_2) > \text{pos}(pp_1)$ 
12                     then break
13                  $pp_2 \leftarrow \text{next}(pp_2)$ 
14                 while  $l \neq \langle \rangle$  and  $|l[0] - \text{pos}(pp_1)| > k$ 
15                     do  $\text{DELETE}(l[0])$ 
16                 for each  $ps \in l$ 
17                     do  $\text{ADD}(\text{answer}, \langle \text{docID}(p_1), \text{pos}(pp_1), ps \rangle)$ 
18                  $pp_1 \leftarrow \text{next}(pp_1)$ 
19                  $p_1 \leftarrow \text{next}(p_1)$ 
20                  $p_2 \leftarrow \text{next}(p_2)$ 
21             else if  $\text{docID}(p_1) < \text{docID}(p_2)$ 
22                 then  $p_1 \leftarrow \text{next}(p_1)$ 
23             else  $p_2 \leftarrow \text{next}(p_2)$ 
24 return answer

```

Combination scheme

- Biword indexes and positional indexes can be profitably combined.
- Many biwords are extremely frequent: Michael Jackson, Britney Spears, etc.
- For these biwords, increased speed compared to positional postings intersection is substantial.
- Combination scheme: Include frequent biwords as vocabulary terms in the index. Do all other phrases by positional intersection.
- Williams et al. (2004) evaluate a more sophisticated mixed indexing scheme. Faster than a positional index, at a cost of 26% more space for index.

“Positional” queries on Google

- For web search engines, positional queries are much more expensive than regular Boolean queries.
- Let's look at the example of phrase queries.
- Why are they more expensive than regular Boolean queries?
- Can you demonstrate on Google that phrase queries are more expensive than Boolean queries?

Take-away

- Understanding of the basic unit of classical information retrieval systems: **words** and **documents**: What is a document, what is a term?
- Tokenization: how to get from raw text to words (or tokens)
- More complex indexes: skip pointers and phrases

Resources

- Chapter 2 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - NLP IR boolean search system example: Sketch Engine: <https://ske.fi.muni.cz>
 - Google query language and preprocessing

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 3: Dictionaries and tolerant retrieval Handout version

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2024-02-28

(compiled on 2024-02-29 18:20:43)

Overview

- 1 Dictionaries
- 2 Wildcard queries
- 3 Edit distance
- 4 Spelling correction
- 5 Soundex

Take-away

- **Tolerant retrieval:** What to do if there is no exact match between query term and document term
- Wildcard queries
- Spelling correction

Inverted index

For each term t , we store a list of all documents that contain t .

BRUTUS → 1 | 2 | 4 | 11 | 31 | 45 | 173 | 174

CAESAR → 1 | 2 | 4 | 5 | 6 | 16 | 57 | 132 | ...

CALPURNIA → 2 | 31 | 54 | 101

⋮

dictionary

postings

Dictionaries

- The dictionary is the data structure for storing the term vocabulary.
- **Term vocabulary**: the **data**
- **Dictionary**: the **data structure** for storing the term vocabulary

Dictionary as array of fixed-width entries

- For each term, we need to store a couple of items:
 - document frequency
 - pointer to postings list
 - ...
- Assume for the time being that we can store this information in a fixed-length entry.
- Assume that we store these entries in an array.

Dictionary as array of fixed-width entries

| term | document frequency | pointer to postings list |
|--------|-----------------------|-----------------------------|
| a | 656,265 | → |
| aachen | 65 | → |
| ... | ... | ... |
| zulu | 221 | → |

space needed: 20 bytes 4 bytes 4 bytes

How do we look up a query term q_i in this array at query time?
That is: which data structure do we use to locate the entry (row)
in the array where q_i is stored?

Data structures for looking up term

- Two main classes of data structures: hashes and trees
- Some IR systems use hashes, some use trees.
- Criteria for when to use hashes vs. trees:
 - Is there a fixed number of terms or will it keep growing?
 - What are the relative frequencies with which various keys will be accessed?
 - How many terms are we likely to have?

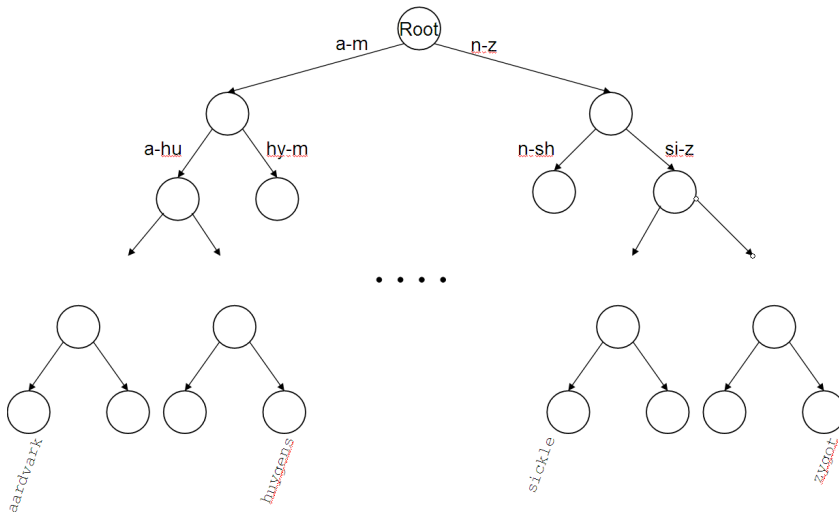
Hashes

- Each vocabulary term is hashed into an integer, its row number in the array.
- At query time: hash query term, locate entry in fixed-width array.
- Pros: Lookup in a hash is faster than lookup in a tree.
 - Lookup time is constant.
- Cons
 - no way to find minor variants (*resume* vs. *résumé*)
 - no prefix search (all terms starting with *automat*)
 - need to rehash everything periodically if vocabulary keeps growing

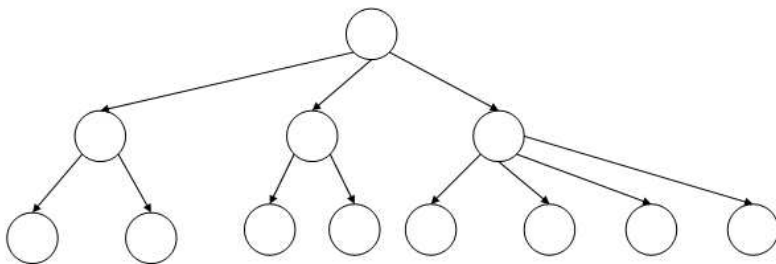
Trees

- Trees solve the prefix problem (find all terms starting with *automat*).
- Simplest tree: binary tree.
- Search is slightly slower than in hashes: $O(\log M)$, where M is the size of the vocabulary.
- $O(\log M)$ only holds for **balanced** trees.
- Rebalancing binary trees is expensive.
- **B-trees** mitigate the rebalancing problem.
- B-tree definition: every internal node has a number of children in the interval $[a, b]$ where a, b are appropriate positive integers, e.g., $[2, 4]$.

Binary tree



B-tree



Wildcard queries

- mon^* : find all docs containing any term beginning with *mon*
- Easy with B-tree dictionary: retrieve all terms t in the range: $mon \leq t < moo$
- $*mon$: find all docs containing any term ending with *mon*
 - Maintain an additional tree for terms *backwards*.
 - Then retrieve all terms t in the range: $nom \leq t < non$
- Result: A set of terms that are matches for wildcard query.
- Then retrieve documents that contain any of these terms.

Query processing

- At this point, we have an enumeration of all terms in the dictionary that match the wildcard query.
- We still have to look up the postings for each enumerated term.

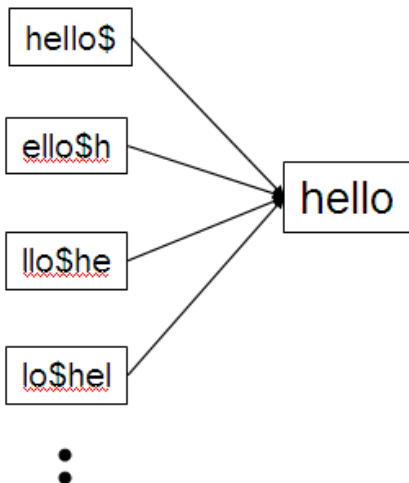
How to handle * in the middle of a term

- Example: m*nchen
- We could look up m* and *nchen in the B-tree and intersect the two term sets.
- Expensive
- Alternative: [permuterm](#) index
- Basic idea: Rotate every wildcard query, so that the * occurs at the end.
- Store each of these rotations in the dictionary, say, in a B-tree

Permuterm index

- For term HELLO: add *hello\$*, *ello\$h*, *llo\$he*, *lo\$hel*, *o\$hell*, and *\$hello* to the B-tree where \$ is a special symbol

Permuterm \rightarrow term mapping



Permuterm index

- For HELLO, we've stored: *hello\$, ello\$h, llo\$he, lo\$hel, o\$hell, \$hello*
- Queries
 - For X, look up X\$
 - For X*, look up \$X*
 - For *X, look up X\$*
 - For *X*, look up X*
 - For X*Y, look up Y\$X*
 - Example: For hel*o, look up o\$hel*
- Permuterm index would better be called a permuterm [tree](#).
- But permuterm index is the more common name.

Processing a lookup in the permuterm index

- Rotate query wildcard to the right
- Use B-tree lookup as before
- Problem: Permuterm more than **quadruples** the size of the dictionary compared to a regular B-tree. (empirical number)

k -gram indexes

- More space-efficient than permuterm index
- Enumerate all character k -grams (sequence of k characters) occurring in a term
- 2-grams are called **bigrams**.
- Example: from *April is the cruelest month* we get the bigrams:
\$a ap pr ri il l\$ \$i is s\$ \$t th he e\$ \$c cr ru ue el le es st t\$ \$m mo on nt th h\$
- \$ is a special word boundary symbol, as before.
- Maintain an inverted index from bigrams to the terms that contain the bigram

Postings list in a 3-gram inverted index



k -gram (bigram, trigram, ...) indexes

- Note that we now have two different types of inverted indexes
- The term-document inverted index for finding documents based on a query consisting of terms
- The k -gram index for finding terms based on a query consisting of k -grams

Processing wildcarded terms in a bigram index

- Query `mon*` can now be run as:
`$m AND mo AND on`
- Gets us all terms with the prefix *mon* . . .
- . . . but also many “false positives” like MOON.
- We must postfilter these terms against query.
- Surviving terms are then looked up in the term-document inverted index.
- *k*-gram index vs. permuterm index
 - *k*-gram index is more space efficient.
 - Permuterm index doesn't require postfiltering.

Exercise

- Google has very limited support for wildcard queries.
- For example, this query doesn't work very well on Google: [gen* universit*]
 - Intention: you are looking for the University of Geneva, but don't know which accents to use for the French words for university and Geneva.
- According to Google search basics, 2010-04-29: "Note that the * operator works only on whole words, not parts of words."
- But this is not entirely true. Try [pythag*] and [m*nchen]
- Exercise: Why doesn't Google fully support wildcard queries?

Processing wildcard queries in the term-document index

- Problem 1: we must potentially execute a large number of Boolean queries.
- Most straightforward semantics: Conjunction of disjunctions
- For [gen* universit*]: geneva university OR geneva université OR genève university OR genève université OR general universities OR ...
- Very expensive
- Problem 2: Users hate to type.
- If abbreviated queries like [pyth* theo*] for [pythagoras' theorem] are allowed, users will use them a lot.
- This would significantly increase the cost of answering queries.
- Somewhat alleviated by Google Suggest

Spelling correction

- Two principal uses
 - Correcting documents being indexed
 - Correcting user queries
- Two different methods for spelling correction
- **Isolated word** spelling correction
 - Check each word on its own for misspelling
 - Will not catch typos resulting in correctly spelled words, e.g.,
*an asteroid that fell **form** the sky*
- **Context-sensitive** spelling correction
 - Look at surrounding words
 - Can correct *form/from* error above

Correcting documents

- We are not interested in interactive spelling correction of documents (e.g., MS Word) in this class.
- In IR, we use document correction primarily for OCR'ed documents. (OCR = optical character recognition)
- The general philosophy in IR is: do **not** change the documents.

Correcting queries

- First: isolated word spelling correction
- Premise 1: There is a list of “correct words” from which the correct spellings come.
- Premise 2: We have a way of computing the **distance** between a misspelled word and a correct word.
- Simple spelling correction algorithm: return the “correct” word that has the smallest distance to the misspelled word.
- Example: *informaton* → *information*
- For the list of correct words, we can use the vocabulary of all words that occur in our collection.
- **Why is this problematic?**

Alternatives to using the term vocabulary

- A standard dictionary (Webster's, OED, etc.)
- An industry-specific dictionary (for specialized IR systems)
- The term vocabulary of the collection, appropriately weighted

Distance between misspelled word and “correct” word

- We will study several alternatives.
- Edit distance and Levenshtein distance
- Weighted edit distance
- k -gram overlap

Edit distance

- The edit distance between string s_1 and string s_2 is the minimum number of basic operations that convert s_1 to s_2 .
- Levenshtein distance: The admissible basic operations are insert, delete, and replace
- Levenshtein distance *dog-do*: 1
- Levenshtein distance *cat-cart*: 1
- Levenshtein distance *cat-cut*: 1
- Levenshtein distance *cat-act*: 2
- Damerau-Levenshtein distance *cat-act*: 1
- Damerau-Levenshtein includes transposition as a fourth possible operation.

Levenshtein distance: Computation

| | | | | | |
|---|---|---|---|---|---|
| | | f | a | s | t |
| | 0 | 1 | 2 | 3 | 4 |
| c | 1 | 1 | 2 | 3 | 4 |
| a | 2 | 2 | 1 | 2 | 3 |
| t | 3 | 3 | 2 | 2 | 2 |
| s | 4 | 4 | 3 | 2 | 3 |

Levenshtein distance: Algorithm

LEVENSHTEINDISTANCE(s_1, s_2)

```
1  for  $i \leftarrow 0$  to  $|s_1|$ 
2  do  $m[i, 0] = i$ 
3  for  $j \leftarrow 0$  to  $|s_2|$ 
4  do  $m[0, j] = j$ 
5  for  $i \leftarrow 1$  to  $|s_1|$ 
6  do for  $j \leftarrow 1$  to  $|s_2|$ 
7      do if  $s_1[i] = s_2[j]$ 
8          then  $m[i, j] = \min\{m[i-1, j]+1, m[i, j-1]+1, m[i-1, j-1]\}$ 
9          else  $m[i, j] = \min\{m[i-1, j]+1, m[i, j-1]+1, m[i-1, j-1]+1\}$ 
10 return  $m[|s_1|, |s_2|]$ 
```

Operations: insert (cost 1), delete (cost 1), replace (cost 1), copy (cost 0)

Levenshtein distance: Algorithm

LEVENSHTEINDISTANCE(s_1, s_2)

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1  for  $i \leftarrow 0$  to  $|s_1|$ 
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10 return  $m[|s_1|, |s_2|]$ 
```

Operations: **insert (cost 1)**, delete (cost 1), replace (cost 1), copy (cost 0)

Levenshtein distance: Algorithm

LEVENSHTEINDISTANCE(s_1, s_2)

```

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10 return  $m[|s_1|, |s_2|]$ 

```

Operations: insert (cost 1), delete (cost 1), replace (cost 1), copy (cost 0)

Levenshtein distance: Algorithm

LEVENSHTEINDISTANCE(s_1, s_2)

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9          else  $m[i, j] = \min\{m[i-1, j]+1, m[i, j-1]+1, m[i-1, j-1]+1\}$ 
10 return  $m[|s_1|, |s_2|]$ 

```

Operations: insert (cost 1), delete (cost 1), **replace (cost 1)**, copy (cost 0)

Levenshtein distance: Algorithm

LEVENSHTEINDISTANCE(s_1, s_2)

```
1  for  $i \leftarrow 0$  to  $|s_1|$ 
2  do  $m[i, 0] = i$ 
3  for  $j \leftarrow 0$  to  $|s_2|$ 
4  do  $m[0, j] = j$ 
5  for  $i \leftarrow 1$  to  $|s_1|$ 
6  do for  $j \leftarrow 1$  to  $|s_2|$ 
7      do if  $s_1[i] = s_2[j]$ 
8          then  $m[i, j] = \min\{m[i - 1, j] + 1, m[i, j - 1] + 1, m[i - 1, j - 1]\}$ 
9          else  $m[i, j] = \min\{m[i - 1, j] + 1, m[i, j - 1] + 1, m[i - 1, j - 1] + 1\}$ 
10 return  $m[|s_1|, |s_2|]$ 
```

Operations: insert (cost 1), delete (cost 1), replace (cost 1), **copy (cost 0)**

Levenshtein distance: algorithm

LEVENSHTEINDISTANCE(s_1, s_2)

```
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2  do  $m[i, 0] = i$ 
3  for  $j \leftarrow 0$  to  $|s_2|$ 
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10 return  $m[|s_1|, |s_2|]$ 
```

Operations: insert, delete, replace, copy

Levenshtein distance: algorithm

LEVENSHTEINDISTANCE(s_1, s_2)

```
1  for  $i \leftarrow 1$  to  $|s_1|$ 
2  do  $m[i, 0] = i$ 
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9          else  $m[i, j] = \min\{m[i-1, j] + 1, m[i, j-1] + 1, m[i-1, j-1] + 1\}$ 
10 return  $m[|s_1|, |s_2|]$ 
```

Operations: insert, delete, replace, copy

Levenshtein distance: Example

| | | f | a | s | t |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| c | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 5</u> <u>4 4</u> |
| a | <u>2</u> <u>2</u> | <u>2 2</u> <u>3 2</u> | <u>1 3</u> <u>3 1</u> | <u>3 4</u> <u>2 2</u> | <u>4 5</u> <u>3 3</u> |
| t | <u>3</u> <u>3</u> | <u>3 3</u> <u>4 3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>2 4</u> <u>3 2</u> |
| s | <u>4</u> <u>4</u> | <u>4 4</u> <u>5 4</u> | <u>4 3</u> <u>5 3</u> | <u>2 3</u> <u>4 2</u> | <u>3 3</u> <u>3 3</u> |

Each cell of Levenshtein matrix

| | |
|--|---|
| cost of getting here from my upper left neighbor (copy or replace) | cost of getting here from my upper neighbor (delete) |
| cost of getting here from my left neighbor (insert) | the minimum of the three possible “movements”; the cheapest way of getting here |

Levenshtein distance: Example

| | | f | a | s | t |
|---|--------------------------|--------------------------------|--------------------------------|--------------------------------|--------------------------------|
| | <u> </u> 0 | <u> 1 </u> 1 1 | <u> 2 </u> 2 2 | <u> 3 </u> 3 3 | <u> 4 </u> 4 4 |
| c | <u> 1 </u> 1 | <u> 1 2 </u> 2 1 | <u> 2 3 </u> 2 2 | <u> 3 4 </u> 3 3 | <u> 4 5 </u> 4 4 |
| a | <u> 2 </u> 2 | <u> 2 2 </u> 3 2 | <u> 1 3 </u> 3 1 | <u> 3 4 </u> 2 2 | <u> 4 5 </u> 3 3 |
| t | <u> 3 </u> 3 | <u> 3 3 </u> 4 3 | <u> 3 2 </u> 4 2 | <u> 2 3 </u> 3 2 | <u> 2 4 </u> 3 2 |
| s | <u> 4 </u> 4 | <u> 4 4 </u> 5 4 | <u> 4 3 </u> 5 3 | <u> 2 3 </u> 4 2 | <u> 3 3 </u> 3 3 |

Dynamic programming (Cormen et al.)

- Optimal substructure: The optimal solution to the problem contains within it **subsolutions**, i.e., optimal solutions to subproblems.
- Overlapping subsolutions: The subsolutions overlap. These subsolutions are computed over and over again when computing the global optimal solution in a brute-force algorithm.
- Subproblem in the case of edit distance: what is the edit distance of two prefixes
- Overlapping subsolutions: We need most distances of prefixes 3 times – this corresponds to moving right, diagonally, down.

Weighted edit distance

- As above, but weight of an operation depends on the characters involved.
- Meant to capture keyboard errors, e.g., m more likely to be mistyped as n than as q .
- Therefore, replacing m by n is a smaller edit distance than by q .
- We now require a weight matrix as input.
- Modify dynamic programming to handle weights

Using edit distance for spelling correction

- Given query, first enumerate all character sequences within a preset (possibly weighted) edit distance
- Intersect this set with our list of “correct” words
- Then suggest terms in the intersection to the user.
- → exercise in a few slides

Exercise

- 1 Compute Levenshtein distance matrix for OSLO – SNOW
- 2 What are the Levenshtein editing operations that transform *cat* into *catcat*?

| | | s | n | o | w |
|---|----------------------|------------|------------|------------|------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | | | | |
| s | <u>2</u> <u>2</u> | | | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|------------|------------|------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 ?</u> | | | |
| s | <u>2</u> <u>2</u> | | | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|------------|------------|------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | | | |
| s | <u>2</u> <u>2</u> | | | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|------------|------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 ?</u> | | |
| s | <u>2</u> <u>2</u> | | | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|------------|------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | | |
| s | <u>2</u> <u>2</u> | | | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 ?</u> | |
| s | <u>2</u> <u>2</u> | | | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | |
| s | <u>2</u> <u>2</u> | | | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 ?</u> |
| s | <u>2</u> <u>2</u> | | | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | | | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 ?</u> | | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 ?</u> | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 ?</u> | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 ?</u> |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 ?</u> | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 ?</u> | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 ?</u> | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 ?</u> |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 ?</u> | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 3</u> | | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 3</u> | <u>3 3</u> <u>4 ?</u> | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 3</u> | <u>3 3</u> <u>4 3</u> | | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 3</u> | <u>3 3</u> <u>4 3</u> | <u>2 4</u> <u>4 ?</u> | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 3</u> | <u>3 3</u> <u>4 3</u> | <u>2 4</u> <u>4 2</u> | |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 3</u> | <u>3 3</u> <u>4 3</u> | <u>2 4</u> <u>4 2</u> | <u>4 5</u> <u>3 ?</u> |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 3</u> | <u>3 3</u> <u>4 3</u> | <u>2 4</u> <u>4 2</u> | <u>4 5</u> <u>3 3</u> |

| | | s | n | o | w |
|---|-------------------|--------------------------------|--------------------------------|--------------------------------|--|
| | $\frac{\quad}{0}$ | $\frac{1}{1}$ | $\frac{2}{2}$ | $\frac{3}{3}$ | $\frac{4}{4}$ |
| o | $\frac{1}{1}$ | $\frac{1}{2}$ $\frac{2}{1}$ | $\frac{2}{2}$ $\frac{3}{2}$ | $\frac{2}{3}$ $\frac{4}{2}$ | $\frac{4}{3}$ $\frac{5}{3}$ |
| s | $\frac{2}{2}$ | $\frac{1}{3}$ $\frac{2}{1}$ | $\frac{2}{2}$ $\frac{3}{2}$ | $\frac{3}{3}$ $\frac{3}{3}$ | $\frac{3}{4}$ $\frac{4}{3}$ |
| l | $\frac{3}{3}$ | $\frac{3}{4}$ $\frac{2}{2}$ | $\frac{2}{3}$ $\frac{3}{2}$ | $\frac{3}{3}$ $\frac{4}{3}$ | $\frac{4}{4}$ $\frac{4}{4}$ |
| o | $\frac{4}{4}$ | $\frac{4}{5}$ $\frac{3}{3}$ | $\frac{3}{4}$ $\frac{3}{3}$ | $\frac{2}{4}$ $\frac{4}{2}$ | $\frac{4}{3}$ $\frac{5}{3}$ 3 |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 3</u> | <u>3 3</u> <u>4 3</u> | <u>2 4</u> <u>4 2</u> | <u>4 5</u> <u>3 3</u> |

How do I read out the editing operations that transform OSLO into SNOW?

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 3</u> | <u>3 3</u> <u>4 3</u> | <u>2 4</u> <u>4 2</u> | <u>4 5</u> <u>3 3</u> |

| cost | operation | input | output |
|------|-----------|-------|--------|
| 1 | insert | * | w |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 3</u> | <u>3 3</u> <u>4 3</u> | <u>2 4</u> <u>4 2</u> | <u>4 5</u> <u>3 3</u> |

| cost | operation | input | output |
|------|-----------|-------|--------|
| 0 | (copy) | o | o |
| 1 | insert | * | w |

| | | s | n | o | w |
|---|----------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1</u> <u>1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2</u> <u>2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3</u> <u>3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4</u> <u>4</u> | <u>4 3</u> <u>5 3</u> | <u>3 3</u> <u>4 3</u> | <u>2 4</u> <u>4 2</u> | <u>4 5</u> <u>3 3</u> |

| cost | operation | input | output |
|------|-----------|-------|--------|
| 1 | replace | l | n |
| 0 | (copy) | o | o |
| 1 | insert | * | w |

| | | s | n | o | w |
|---|------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | <u>0</u> | <u>1 1</u> | <u>2 2</u> | <u>3 3</u> | <u>4 4</u> |
| o | <u>1 1</u> | <u>1 2</u> <u>2 1</u> | <u>2 3</u> <u>2 2</u> | <u>2 4</u> <u>3 2</u> | <u>4 5</u> <u>3 3</u> |
| s | <u>2 2</u> | <u>1 2</u> <u>3 1</u> | <u>2 3</u> <u>2 2</u> | <u>3 3</u> <u>3 3</u> | <u>3 4</u> <u>4 3</u> |
| l | <u>3 3</u> | <u>3 2</u> <u>4 2</u> | <u>2 3</u> <u>3 2</u> | <u>3 4</u> <u>3 3</u> | <u>4 4</u> <u>4 4</u> |
| o | <u>4 4</u> | <u>4 3</u> <u>5 3</u> | <u>3 3</u> <u>4 3</u> | <u>2 4</u> <u>4 2</u> | <u>4 5</u> <u>3 3</u> |

| cost | operation | input | output |
|------|-----------|-------|--------|
| 0 | (copy) | s | s |
| 1 | replace | l | n |
| 0 | (copy) | o | o |
| 1 | insert | * | w |

| | | s | n | o | w |
|---|-----|------------|------------|------------|------------|
| | 0 | 1 1 | 2 2 | 3 3 | 4 4 |
| o | 1 1 | 1 2 2 1 | 2 3 2 2 | 2 4 3 2 | 4 5 3 3 |
| s | 2 2 | 1 2 3 1 | 2 3 2 2 | 3 3 3 3 | 3 4 4 3 |
| l | 3 3 | 3 2 4 2 | 2 3 3 2 | 3 4 3 3 | 4 4 4 4 |
| o | 4 4 | 4 3 5 3 | 3 3 4 3 | 2 4 4 2 | 4 5 3 3 |

| cost | operation | input | output |
|------|-----------|-------|--------|
| 1 | delete | o | * |
| 0 | (copy) | s | s |
| 1 | replace | l | n |
| 0 | (copy) | o | o |
| 1 | insert | * | w |

| | | c | a | t | c | a | t |
|---|-----|------------|------------|------------|------------|------------|------------|
| | 0 | 1 1 | 2 2 | 3 3 | 4 4 | 5 5 | 6 6 |
| c | 1 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 | 5 6 4 4 | 6 7 5 5 |
| a | 2 2 | 2 1 3 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 | 5 6 4 4 |
| t | 3 3 | 3 2 4 2 | 2 1 3 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 |

| | | | | | | | |
|---|-----|------------|------------|------------|------------|------------|------------|
| | | c | a | t | c | a | t |
| | 0 | 1 1 | 2 2 | 3 3 | 4 4 | 5 5 | 6 6 |
| c | 1 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 | 5 6 4 4 | 6 7 5 5 |
| a | 2 2 | 2 1 3 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 | 5 6 4 4 |
| t | 3 3 | 3 2 4 2 | 2 1 3 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 |

| cost | operation | input | output |
|------|-----------|-------|--------|
| 1 | insert | * | c |
| 1 | insert | * | a |
| 1 | insert | * | t |
| 0 | (copy) | c | c |
| 0 | (copy) | a | a |
| 0 | (copy) | t | t |

| | | | | | | | | |
|---|--|--------|------------|------------|------------|------------|------------|------------|
| | | | c | a | t | c | a | t |
| | | 0 | 1 1 | 2 2 | 3 3 | 4 4 | 5 5 | 6 6 |
| c | | 1 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 | 5 6 4 4 | 6 7 5 5 |
| a | | 2 2 | 2 1 3 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 | 5 6 4 4 |
| t | | 3 3 | 3 2 4 2 | 2 1 3 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 |

| cost | operation | input | output |
|------|-----------|-------|--------|
| 0 | (copy) | c | c |
| 1 | insert | * | a |
| 1 | insert | * | t |
| 1 | insert | * | c |
| 0 | (copy) | a | a |
| 0 | (copy) | t | t |

| | | | | | | | | |
|---|-----|-----|-----|-----|-----|-----|-----|-----|
| | | | c | a | t | c | a | t |
| | | 0 | 1 1 | 2 2 | 3 3 | 4 4 | 5 5 | 6 6 |
| c | 1 1 | 0 2 | 2 3 | 3 4 | 3 5 | 5 6 | 6 7 | |
| | 1 | 2 0 | 1 1 | 2 2 | 3 3 | 4 4 | 5 5 | |
| a | 2 2 | 2 1 | 0 2 | 2 3 | 3 4 | 3 5 | 5 6 | |
| | 2 | 3 1 | 2 0 | 1 1 | 2 2 | 3 3 | 4 4 | |
| t | 3 3 | 3 2 | 2 1 | 0 2 | 2 3 | 3 4 | 3 5 | |
| | 3 | 4 2 | 3 1 | 2 0 | 1 1 | 2 2 | 3 3 | |

| cost | operation | input | output |
|------|-----------|-------|--------|
| 0 | (copy) | c | c |
| 0 | (copy) | a | a |
| 1 | insert | * | t |
| 1 | insert | * | c |
| 1 | insert | * | a |
| 0 | (copy) | t | t |

| | | | | | | | | |
|---|--|--------|----------------|----------------|----------------|----------------|----------------|----------------|
| | | | c | a | t | c | a | t |
| | | 0 | 1 1 | 2 2 | 3 3 | 4 4 | 5 5 | 6 6 |
| c | | 1 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 | 5 6 4 4 | 6 7 5 5 |
| a | | 2 2 | 2 1 3 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 | 5 6 4 4 |
| t | | 3 3 | 3 2 4 2 | 2 1 3 1 | 0 2 2 0 | 2 3 1 1 | 3 4 2 2 | 3 5 3 3 |

| cost | operation | input | output |
|------|-----------|-------|--------|
| 0 | (copy) | c | c |
| 0 | (copy) | a | a |
| 0 | (copy) | t | t |
| 1 | insert | * | c |
| 1 | insert | * | a |
| 1 | insert | * | t |

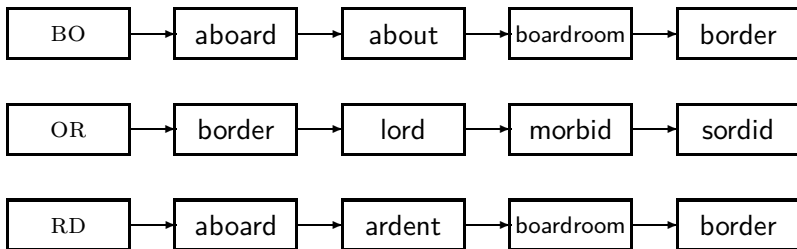
Spelling correction

- Now that we can compute edit distance: how to use it for isolated word spelling correction – this is the last slide in this section.
- k -gram indexes for isolated word spelling correction.
- Context-sensitive spelling correction
- General issues

k -gram indexes for spelling correction

- Enumerate all k -grams in the query term
- Example: bigram index, misspelled word *bordroom*
- Bigrams: *bo, or, rd, dr, ro, oo, om*
- Use the k -gram index to retrieve “correct” words that match query term k -grams
- Threshold by number of matching k -grams
- E.g., only vocabulary terms that differ by at most 3 k -grams

k -gram indexes for spelling correction: *bordroom*



Context-sensitive spelling correction

- Our example was: *an asteroid that fell **form** the sky*
- How can we correct *form* here?
- One idea: **hit-based** spelling correction
 - Retrieve “correct” terms close to each query term
 - for *flew form munich*: *flea* for *flew*, *from* for *form*, *munch* for *munich*
 - Now try all possible resulting phrases as queries with one word “fixed” at a time
 - Try query “*flea form munich*”
 - Try query “*flew from munich*”
 - Try query “*flew form munch*”
 - The correct query “*flew from munich*” has the most hits.
- Suppose we have 7 alternatives for *flew*, 20 for *form* and 3 for *munich*, how many “corrected” phrases will we enumerate?

Context-sensitive spelling correction

- The “hit-based” algorithm we just outlined is not very efficient.
- More efficient alternative: look at “collection” of queries, not documents.

General issues in spelling correction

- User interface
 - automatic vs. suggested correction
 - *Did you mean* only works for one suggestion.
 - What about multiple possible corrections?
 - Tradeoff: simple vs. powerful UI
- Cost
 - Spelling correction is potentially expensive.
 - Avoid running on every query?
 - Maybe just on queries that match few documents.
 - Guess: Spelling correction of major search engines is efficient enough to be run on every query.

Exercise: Understand Peter Norvig's spelling corrector

```
import re, collections
def words(text): return re.findall('[a-z]+', text.lower())
def train(features):
    model = collections.defaultdict(lambda: 1)
    for f in features:
        model[f] += 1
    return model
NWORDS = train(words(file('big.txt').read()))
alphabet = 'abcdefghijklmnopqrstuvwxyz'
def edits1(word):
    splits      = [(word[:i], word[i:]) for i in range(len(word) + 1)]
    deletes     = [a + b[1:] for a, b in splits if b]
    transposes  = [a + b[1] + b[0] + b[2:] for a, b in splits if len(b) > 1]
    replaces    = [a + c + b[1:] for a, b in splits for c in alphabet if b]
    inserts     = [a + c + b      for a, b in splits for c in alphabet]
    return set(deletes + transposes + replaces + inserts)
def known_edits2(word):
    return set(e2 for e1 in edits1(word) for e2 in edits1(e1) if e2 in NWORDS)
def known(words): return set(w for w in words if w in NWORDS)
def correct(word):
    candidates = known([word]) or known(edits1(word)) or known_edits2(word) or [word]
    return max(candidates, key=NWORDS.get)
```

```

import re, collections

def words(text): return re.findall('[a-z]+', text.lower())

def train(features):
    model = collections.defaultdict(lambda: 1)
    for f in features:
        model[f] += 1
    return model

NWORDS = train(words(file('big.txt').read()))

alphabet = 'abcdefghijklmnopqrstuvwxyz'

def edits1(word):
    n = len(word)
    return set([word[0:i]+word[i+1:] for i in range(n)] + # deletion
               [word[0:i]+word[i+1]+word[i]+word[i+2:] for i in range(n-1)] + # transposition
               [word[0:i]+c+word[i+1:] for i in range(n) for c in alphabet] + # alteration
               [word[0:i]+c+word[i:] for i in range(n+1) for c in alphabet]) # insertion

def known_edits2(word):
    return set(e2 for e1 in edits1(word) for e2 in edits1(e1) if e2 in NWORDS)

def known(words): return set(w for w in words if w in NWORDS)

def correct(word):
    candidates = known([word]) or known(edits1(word)) or known_edits2(word) or [word]
    return max(candidates, key=lambda w: NWORDS[w])

```

<https://norvig.com/spell-correct.html>

Soundex

- Soundex is the basis for finding **phonetic** (as opposed to orthographic) alternatives.
- Example: *chebyshev* / *tchebyscheff*
- Algorithm:
 - Turn every token to be indexed into a 4-character reduced form
 - Do the same with query terms
 - Build and search an index on the reduced forms

Soundex algorithm

- 1 Retain the first letter of the term.
- 2 Change all occurrences of the following letters to '0' (zero): A, E, I, O, U, H, W, Y
- 3 Change letters to digits as follows:
 - B, F, P, V to 1
 - C, G, J, K, Q, S, X, Z to 2
 - D, T to 3
 - L to 4
 - M, N to 5
 - R to 6
- 4 Repeatedly remove one out of each pair of consecutive identical digits
- 5 Remove all zeros from the resulting string; pad the resulting string with trailing zeros and return the first four positions, which will consist of a letter followed by three digits

Example: Soundex of *HERMAN*

- Retain H
- *ERMAN* → *ORMON*
- *ORMON* → *06505*
- *06505* → *06505*
- *06505* → *655*
- Return *H655*
- Note: *HERMANN* will generate the same code

How useful is Soundex?

- *Not very – for information retrieval, obsolete*
- Ok for “high recall” tasks in other applications (e.g., Interpol).
- Zobel and Dart (1996) suggest better alternatives for phonetic matching in IR.

Exercise

- Compute Soundex code of your last name

Take-away

- **Tolerant retrieval:** What to do if there is no exact match between query term and document term
- Wildcard queries
- Spelling correction

Resources

- Chapter 3 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cis1mu.org>, materials in MU IS and FI MU library
 - trie vs hash vs ternary tree
 - Soundex demo
 - Edit distance demo
 - Peter Norvig's spelling corrector
 - Google: wild card search, spelling correction gone wrong, a misspelling that is more frequent than the correct spelling
 - NLP IR boolean search system example: Sketch Engine – <https://ske.fi.muni.cz>

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 4: Index construction Handout version

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(compiled on 2024-02-20 00:47:52)

Overview

- 1 Introduction
- 2 BSBI algorithm
- 3 SPIMI algorithm
- 4 Distributed indexing
- 5 Dynamic indexing

Take-away

- Two index construction algorithms: **BSBI** (simple) and **SPIMI** (more realistic)
- **Distributed** index construction: MapReduce
- **Dynamic** index construction: how to keep the index up-to-date as the collection changes

Hardware basics

- Many design decisions in information retrieval are based on hardware constraints.
- We begin by reviewing hardware basics that we'll need in this course.

Hardware basics

- Access to data is **much faster in memory than on disk**. (roughly a factor of 10 SSD, 100+ for rotational disks)
- **Disk seeks are “idle” time**: No data is transferred from disk while the disk head is being positioned.
- To optimize transfer time from disk to memory: **one large chunk is faster than many small chunks**.
- **Disk I/O is block-based**: Reading and writing of entire blocks (as opposed to smaller chunks). Block sizes: 8KB to 256 KB
- Assuming an efficient decompression algorithm, the total time of reading and then decompressing compressed data is usually less than reading uncompressed data.
- Servers used in IR systems typically have many **GBs of main memory** and **TBs of disk space**.
- **Fault tolerance is expensive**: It's cheaper to use many regular machines than one fault tolerant machine.

Some stats (ca. 2008)

| symbol | statistic | value |
|--------|--|---|
| s | average seek time | 5 ms = 5×10^{-3} s |
| b | transfer time per byte | $0.02 \mu\text{s} = 2 \times 10^{-8}$ s |
| | processor's clock rate | 10^9 s^{-1} |
| p | lowlevel operation (e.g., compare & swap a word) | $0.01 \mu\text{s} = 10^{-8}$ s |
| | size of main memory | several GB |
| | size of disk space | 1 TB or more |

RCV1 collection

- Shakespeare's collected works are not large enough for demonstrating many of the points in this course.
- As an example for applying scalable index construction algorithms, we will use the [Reuters RCV1](#) collection.
- English newswire articles sent over the wire in 1995 and 1996 (one year).

A Reuters RCV1 document



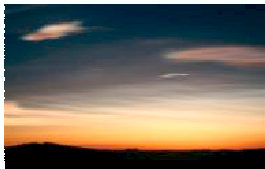
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Extreme conditions create rare Antarctic clouds

Tue Aug 1, 2006 3:20am ET

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SYDNEY (Reuters) - Rare, mother-of-pearl colored clouds caused by extreme weather conditions above Antarctica are a possible indication of global warming, Australian scientists said on Tuesday.

Known as nacreous clouds, the spectacular formations showing delicate wisps of colors were photographed in the sky over an Australian

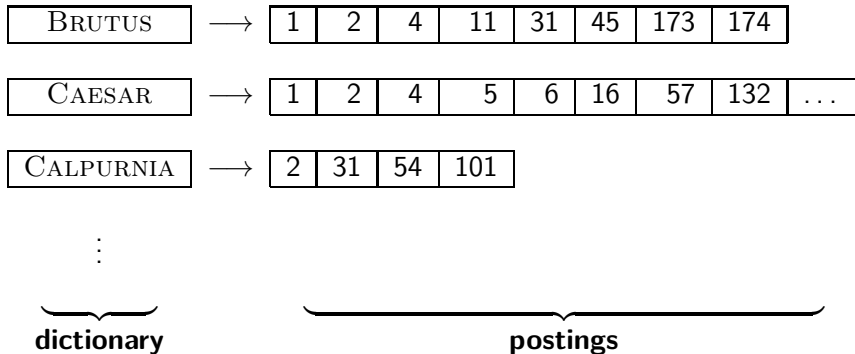
[\[-\] Text \[+\]](#)

Reuters RCV1 statistics

| | | |
|-----|---|-------------|
| N | documents | 800,000 |
| L | tokens per document | 200 |
| M | terms (= word types) | 400,000 |
| | bytes per token (incl. spaces/punct.) | 6 |
| | bytes per token (without spaces/punct.) | 4.5 |
| | bytes per term (= word type) | 7.5 |
| T | non-positional postings | 100,000,000 |

Exercise: Average frequency of a term (how many tokens)? 4.5
 bytes per word token vs. 7.5 bytes per word type: why the
 difference? How many positional postings?

Goal: construct the inverted index



Index construction in IIR 1: Sort postings in memory

| term | docID | | term | docID |
|-----------|-------|---|-----------|-------|
| l | 1 | | ambitious | 2 |
| did | 1 | | be | 2 |
| enact | 1 | | brutus | 1 |
| julius | 1 | | brutus | 2 |
| caesar | 1 | | capitol | 1 |
| l | 1 | | caesar | 1 |
| was | 1 | | caesar | 2 |
| killed | 1 | | caesar | 2 |
| i' | 1 | | did | 1 |
| the | 1 | | enact | 1 |
| capitol | 1 | | hath | 1 |
| brutus | 1 | | l | 1 |
| killed | 1 | | l | 1 |
| me | 1 | ⇒ | i' | 1 |
| so | 2 | | it | 2 |
| let | 2 | | julius | 1 |
| it | 2 | | killed | 1 |
| be | 2 | | killed | 1 |
| with | 2 | | let | 2 |
| caesar | 2 | | me | 1 |
| the | 2 | | noble | 2 |
| noble | 2 | | so | 2 |
| brutus | 2 | | the | 1 |
| hath | 2 | | the | 2 |
| told | 2 | | told | 2 |
| you | 2 | | you | 2 |
| caesar | 2 | | was | 1 |
| was | 2 | | was | 2 |
| ambitious | 2 | | with | 2 |

Scaling index construction

- How can we construct an index for very large collections?
- Taking into account the hardware constraints we just learned about ...
- ... memory, disk, speed, etc.

Sort-based index construction

- As we build index, we parse docs one at a time.
- The final postings for any term are incomplete until the end.
- Can we keep all postings in memory and then do the sort in-memory at the end?
- No, not for large collections
- Thus: We need to store intermediate results on disk.

Same algorithm for disk?

- Can we use the same index construction algorithm for larger collections, but by using disk instead of memory?
- No: Sorting very large sets of records on disk is too slow – too many disk seeks.
- We need an [external](#) sorting algorithm.

“External” sorting algorithm (using few disk seeks)

- We must sort $T = 100,000,000$ non-positional postings.
 - Each posting has size 12 bytes (4+4+4: termID, docID, term frequency).
- Define a **block** to consist of 10,000,000 such postings
 - We can easily fit that many postings into memory.
 - We will have 10 such blocks for RCV1.
- Basic idea of algorithm:
 - For each block: (i) accumulate postings, (ii) sort in memory, (iii) write to disk
 - Then merge the blocks into one long sorted order.

Merging two blocks

postings
to be merged

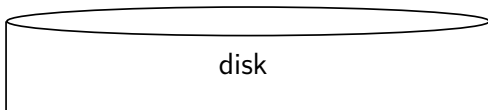
| Block 1 | |
|---------|----|
| brutus | d3 |
| caesar | d4 |
| noble | d3 |
| with | d4 |

| Block 2 | |
|---------|----|
| brutus | d2 |
| caesar | d1 |
| julius | d1 |
| killed | d2 |



| | |
|--------|----|
| brutus | d2 |
| brutus | d3 |
| caesar | d1 |
| caesar | d4 |
| julius | d1 |
| killed | d2 |
| noble | d3 |
| with | d4 |

merged
postings



Blocked Sort-Based Indexing

BSBINDEXCONSTRUCTION()

```
1  $n \leftarrow 0$ 
2 while (all documents have not been processed)
3 do  $n \leftarrow n + 1$ 
4    $block \leftarrow \text{PARSENEXTBLOCK}()$ 
5    $\text{BSBI-INVERT}(block)$ 
6    $\text{WRITEBLOCKTODISK}(block, f_n)$ 
7  $\text{MERGEBLOCKS}(f_1, \dots, f_n; f_{\text{merged}})$ 
```

Problem with sort-based algorithm

- Our assumption was: we can keep the dictionary in memory.
- We need the dictionary (which grows dynamically) in order to implement a term to termID mapping.
- Actually, we could work with term,docID postings instead of termID,docID postings . . .
- . . . but then intermediate files become very large. (We would end up with a scalable, but very slow index construction method.)

Single-pass in-memory indexing

- Abbreviation: SPIMI
- Key idea 1: Generate separate dictionaries for each block – no need to maintain term-termID mapping across blocks.
- Key idea 2: Don't sort. Accumulate postings in postings lists as they occur.
- With these two ideas we can generate a complete inverted index for each block.
- These separate indexes can then be merged into one big index.

SPIMI-Invert

```
SPIMI-INVERT(token_stream)
1  output_file ← NEWFILE()
2  dictionary ← NEWHASH()
3  while (free memory available)
4  do token ← next(token_stream)
5     if term(token) ∉ dictionary
6         then postings_list ← ADDTODICTIONARY(dictionary, term(token))
7         else postings_list ← GETPOSTINGSLIST(dictionary, term(token))
8         if full(postings_list)
9             then postings_list ← DOUBLEPOSTINGSLIST(dictionary, term(token))
10        ADDTOPOSTINGSLIST(postings_list, docID(token))
11  sorted_terms ← SORTTERMS(dictionary)
12  WRITEBLOCKTODISK(sorted_terms, dictionary, output_file)
13  return output_file
```

Merging of blocks is analogous to BSBI.

SPIMI: Compression

- Compression makes SPIMI even more efficient.
 - Compression of terms
 - Compression of postings
 - See next lecture

Distributed indexing

- For web-scale indexing (don't try this at home!): must use a distributed computer cluster
- Individual machines are fault-prone.
 - Can unpredictably slow down or fail.
- How do we exploit such a pool of machines?

Google data centers (2007 estimates; Gartner)

- Google data centers mainly contain commodity machines.
- Data centers are distributed all over the world.
- 1 million servers, 3 million processors/cores
- Google installs 100,000 servers each quarter.
- Based on expenditures of 200–250 million dollars per year
- This would be 10% of the computing capacity of the world!
- If in a non-fault-tolerant system with 1000 nodes, each node has 99.9% uptime, what is the uptime of the system (assuming it does not tolerate failures)?
- Answer: 37%
- Suppose a server will fail after 3 years. For an installation of 1 million servers, what is the interval between machine failures?
- Answer: less than two minutes

Distributed indexing

- Maintain a **master** machine directing the indexing job – considered “safe”
- Break up indexing into sets of parallel tasks
- Master machine assigns each task to an idle machine from a pool.

Parallel tasks

- We will define two sets of parallel tasks and deploy two types of machines to solve them:
 - Parsers
 - Inverters
- Break the input document collection into **splits** (corresponding to blocks in BSBI/SPIMI)
- Each split is a subset of documents.

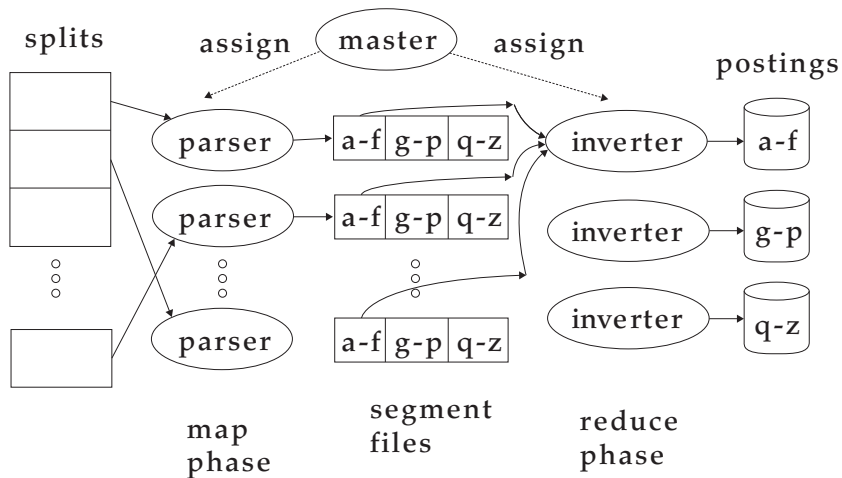
Parsers

- Master assigns a split to an idle parser machine.
- Parser reads a document at a time and **emits** (termID,docID)-pairs.
- Parser writes pairs into j term-partitions.
- Each for a range of terms' first letters
 - E.g., a-f, g-p, q-z (here: $j = 3$)

Inverters

- An inverter collects all (termID,docID) pairs (= postings) for one term-partition (e.g., for a–f).
- Sorts and writes to postings lists

Data flow



MapReduce

- The index construction algorithm we just described is an instance of MapReduce.
- MapReduce is a robust and conceptually simple framework for distributed computing . . .
- . . . without having to write code for the distribution part.
- The Google indexing system (ca. 2002) consisted of a number of phases, each implemented in MapReduce.
- Index construction was just one phase.
- Another phase: transform term-partitioned into document-partitioned index.

Index construction in MapReduce

Schema of map and reduce functions

map: input $\rightarrow \text{list}(k, v)$
 reduce: $(k, \text{list}(v)) \rightarrow \text{output}$

Instantiation of the schema for index construction

map: web collection $\rightarrow \text{list}(\text{termID}, \text{docID})$
 reduce: $((\text{termID}_1, \text{list}(\text{docID})), (\text{termID}_2, \text{list}(\text{docID})), \dots) \rightarrow (\text{postings_list}_1, \text{postings_list}_2, \dots)$

Example for index construction

map: $d_2 : C \text{ DIED}, d_1 : C \text{ CAME}, C \text{ C'ED} \rightarrow ((C, d_2), (DIED, d_2), (C, d_1), (CAME, d_1), (C, d_1), (C'ED, d_1))$
 reduce: $((C, (d_2, d_1, d_1)), (DIED, (d_2)), (CAME, (d_1)), (C'ED, (d_1))) \rightarrow ((C, (d_1:2, d_2:1)), (DIED, (d_2:1)), (CAME, (d_1:1)), (C'ED, (d_1:1)))$

Exercise

- What information does the task description contain that the master gives to a parser?
- What information does the parser report back to the master upon completion of the task?
- What information does the task description contain that the master gives to an inverter?
- What information does the inverter report back to the master upon completion of the task?

Dynamic indexing

- Up to now, we have assumed that collections are **static**.
- They rarely are: Documents are inserted, deleted and modified.
- This means that the dictionary and postings lists have to be **dynamically** modified.

Dynamic indexing: Simplest approach

- Maintain **big main index on disk**
- New docs go into **small auxiliary index in memory**.
- Search across both, merge results
- Periodically, merge auxiliary index into big index
- Deletions:
 - Invalidation bit-vector for deleted docs
 - Filter docs returned by index using this bit-vector

Issue with auxiliary and main index

- Frequent merges
- Poor search performance during index merge

Logarithmic merge

- Logarithmic merging amortizes the cost of merging indexes over time.
 - \rightarrow Users see smaller effect on response times.
- Maintain a series of indexes, each twice as large as the previous one.
- Keep smallest (Z_0) in memory
- Larger ones (l_0, l_1, \dots) on disk
- If Z_0 gets too big ($> n$), write to disk as l_0
- ... or merge with l_0 (if l_0 already exists) and write merger to l_1 , etc.

LMERGEADDTOKEN(*indexes*, Z_0 , *token*)

```

1   $Z_0 \leftarrow \text{MERGE}(Z_0, \{\text{token}\})$ 
2  if  $|Z_0| = n$ 
3    then for  $i \leftarrow 0$  to  $\infty$ 
4      do if  $l_i \in \text{indexes}$ 
5        then  $Z_{i+1} \leftarrow \text{MERGE}(l_i, Z_i)$ 
6          ( $Z_{i+1}$  is a temporary index on disk.)
7           $\text{indexes} \leftarrow \text{indexes} - \{l_i\}$ 
8        else  $l_i \leftarrow Z_i$  ( $Z_i$  becomes the permanent index  $l_i$ .)
9           $\text{indexes} \leftarrow \text{indexes} \cup \{l_i\}$ 
10         BREAK
11      $Z_0 \leftarrow \emptyset$ 

```

LOGARITHMICMERGE()

```

1   $Z_0 \leftarrow \emptyset$  ( $Z_0$  is the in-memory index.)
2   $\text{indexes} \leftarrow \emptyset$ 
3  while true
4  do LMERGEADDTOKEN(indexes,  $Z_0$ , GETNEXTTOKEN())

```

Binary numbers: $l_3l_2l_1l_0 = 2^32^22^12^0$

- 0001
- 0010
- 0011
- 0100
- 0101
- 0110
- 0111
- 1000
- 1001
- 1010
- 1011
- 1100

Logarithmic merge

- Number of indexes bounded by $O(\log T)$ (T is total number of postings read so far)
- So query processing requires the merging of $O(\log T)$ indexes
- Time complexity of index construction is $O(T \log T)$.
 - ... because each of T postings is merged $O(\log T)$ times.
- Auxiliary index: index construction time is $O(T^2)$ as each posting is touched in each merge.
 - Suppose auxiliary index has size a
 - $a + 2a + 3a + 4a + \dots + na = a \frac{n(n+1)}{2} = O(n^2)$
- So logarithmic merging is an order of magnitude more efficient.

Dynamic indexing at large search engines

- Often a combination
 - Frequent incremental changes
 - Rotation of large parts of the index that can then be swapped in
 - Occasional complete rebuild (becomes harder with increasing size – not clear if Google can do a complete rebuild)

Building positional indexes

- Basically the same problem except that the intermediate data structures are large.

Take-away

- Two index construction algorithms: **BSBI** (simple) and **SPIMI** (more realistic)
- **Distributed** index construction: MapReduce
- **Dynamic** index construction: how to keep the index up-to-date as the collection changes

Resources

- Chapter 4 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - Original publication on MapReduce by Dean and Ghemawat (2004)
 - Original publication on SPIMI by Heinz and Zobel (2003)
 - YouTube video: Google data centers

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 5: Index compression Handout version

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2024-03-14

(compiled on 2024-03-08 15:01:09)

Overview

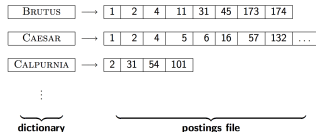
- 1 Compression
- 2 Term statistics
- 3 Dictionary compression
- 4 Postings compression

Roadmap

- Today: index compression, and vector space model
- Next week: the whole picture of complete search system, scoring and ranking

Take-away today

For each term t , we store a list of all documents that contain t .



- Motivation for compression in information retrieval systems
- How can we compress the **dictionary** component of the inverted index?
- How can we compress the **postings** component of the inverted index?
- Term statistics: how are terms distributed in document collections?

Inverted index

For each term t , we store a list of all documents that contain t .

BRUTUS → 1 | 2 | 4 | 11 | 31 | 45 | 173 | 174

CAESAR → 1 | 2 | 4 | 5 | 6 | 16 | 57 | 132 | ...

CALPURNIA → 2 | 31 | 54 | 101

⋮

⏟
dictionary

⏟
postings file

Today:

- How much space do we need for the dictionary?
- How much space do we need for the postings file?
- How can we compress them?

Why compression? (in general)

- Use less disk space (saves money).
- Keep more stuff in memory (increases speed).
- Increase speed of transferring data from disk to memory (again, increases speed).
[read compressed data and decompress in memory]
is faster than
[read uncompressed data]
- Premise: Decompression algorithms are fast.
- This is true of the decompression algorithms we will use.

Why compression in information retrieval?

- First, we will consider space for dictionary:
 - Main motivation for dictionary compression: make it small enough to keep in main memory.
- Then for the postings file
 - Motivation: reduce disk space needed, decrease time needed to read from disk.
 - Note: Large search engines keep significant part of postings in memory.
- We will devise various compression schemes for dictionary and postings.

Lossy vs. lossless compression

- Lossy compression: Discard some information
- Several of the preprocessing steps we frequently use can be viewed as lossy compression:
 - downcasing, stop words, porter, number elimination
- Lossless compression: All information is preserved.
 - What we mostly do in index compression

Model collection: The Reuters collection

| symbol | statistic | value |
|----------|---|-------------|
| <i>N</i> | documents | 800,000 |
| <i>L</i> | avg. # word tokens per document | 200 |
| <i>M</i> | word types | 400,000 |
| | avg. # bytes per word token (incl. spaces/punct.) | 6 |
| | avg. # bytes per word token (without spaces/punct.) | 4.5 |
| | avg. # bytes per word type | 7.5 |
| <i>T</i> | non-positional postings | 100,000,000 |

Effect of preprocessing for Reuters

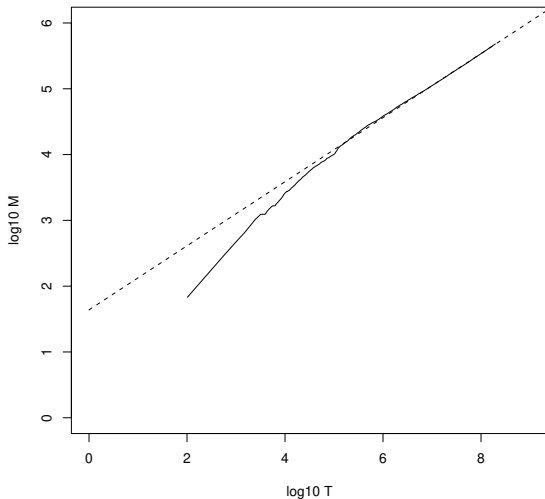
| size of | word types (terms) | non-positional postings | positional postings (word tokens) |
|--------------|-----------------------|----------------------------|--------------------------------------|
| | dictionary | non-positional index | positional index |
| | size Δ cml | size Δ cml | size Δ cml |
| unfiltered | 484,494 | 109,971,179 | 197,879,290 |
| no numbers | 473,723 -2 -2 | 100,680,242 -8 -8 | 179,158,204 -9 -9 |
| case folding | 391,523 -17 -19 | 96,969,056 -3 -12 | 179,158,204 -0 -9 |
| 30 stopw's | 391,493 -0 -19 | 83,390,443 -14 -24 | 121,857,825 -31 -38 |
| 150 stopw's | 391,373 -0 -19 | 67,001,847 -30 -39 | 94,516,599 -47 -52 |
| stemming | 322,383 -17 -33 | 63,812,300 -4 -42 | 94,516,599 -0 -52 |

Explain differences between numbers non-positional vs positional:
 -3 vs 0 , -14 vs -31 , -30 vs -47 , -4 vs 0

How big is the term vocabulary?

- That is, how many distinct words are there?
- Can we assume there is an upper bound?
- Not really: At least $70^{20} \approx 10^{37}$ different words of length 20.
- The vocabulary will keep growing with collection size.
- Heaps' law: $M = kT^b$
- M is the size of the vocabulary, T is the number of tokens in the collection.
- Typical values for the parameters k and b are: $30 \leq k \leq 100$ and $b \approx 0.5$.
- Heaps' law is linear in log-log space.
 - It is the simplest possible relationship between collection size and vocabulary size in log-log space.
 - Empirical law

Heaps' law for Reuters



Vocabulary size M as a function of collection size T (number of tokens) for Reuters-RCV1. For these data, the dashed line $\log_{10} M = 0.49 * \log_{10} T + 1.64$ is the best least squares fit. Thus, $M = 10^{1.64} T^{0.49}$ and $k = 10^{1.64} \approx 44$ and $b = 0.49$.

Empirical fit for Reuters

- Good, as we just saw in the graph.
- Example: for the first 1,000,020 tokens Heaps' law predicts 38,323 terms:

$$44 \times 1,000,020^{0.49} \approx 38,323$$

- The actual number is 38,365 terms, very close to the prediction.
- Empirical observation: fit is good in general.

Exercise

- 1 What is the effect of including spelling errors vs. automatically correcting spelling errors on Heaps' law?
- 2 Compute vocabulary size M
 - Looking at a collection of web pages, you find that there are 3,000 different terms in the first 10,000 tokens and 30,000 different terms in the first 1,000,000 tokens.
 - Assume a search engine indexes a total of 20,000,000,000 (2×10^{10}) pages, containing 200 tokens on average
 - What is the size of the vocabulary of the indexed collection as predicted by Heaps' law?

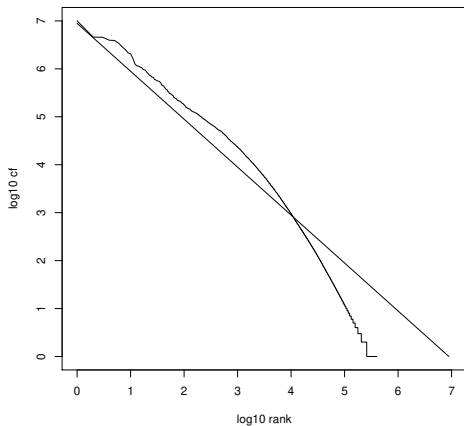
Zipf's law

- Now we have characterized the growth of the vocabulary in collections.
- We also want to know how many frequent vs. infrequent terms we should expect in a collection.
- In natural language, there are a few very frequent terms and very many very rare terms.
- Zipf's law: The i^{th} most frequent term has frequency cf_i proportional to $1/i$.
- $cf_i \propto \frac{1}{i}$
- cf_i is collection frequency: the number of occurrences of the term t_i in the collection.

Zipf's law

- Zipf's law: The i^{th} most frequent term has frequency proportional to $1/i$.
- $cf_i \propto \frac{1}{i}$
- cf is collection frequency: the number of occurrences of the term in the collection.
- So if the most frequent term (*the*) occurs cf_1 times, then the second most frequent term (*of*) has half as many occurrences $cf_2 = \frac{1}{2}cf_1 \dots$
- ... and the third most frequent term (*and*) has a third as many occurrences $cf_3 = \frac{1}{3}cf_1$, etc.
- Equivalent: $cf_i = ci^k$ and $\log cf_i = \log c + k \log i$ (for $k = -1$)
- Example of a power law

Zipf's law for Reuters



Fit is not great. What is important is the key insight: **Few frequent terms, many rare terms.**

Dictionary compression

- The dictionary is small compared to the postings file.
- But we want to keep it in memory.
- Also: competition with other applications, cell phones, onboard computers, fast startup time
- So compressing the dictionary is important.

Recall: Dictionary as array of fixed-width entries

| term | document frequency | pointer to postings list |
|--------|--------------------|--------------------------|
| a | 656,265 | → |
| aachen | 65 | → |
| ... | ... | ... |
| zulu | 221 | → |

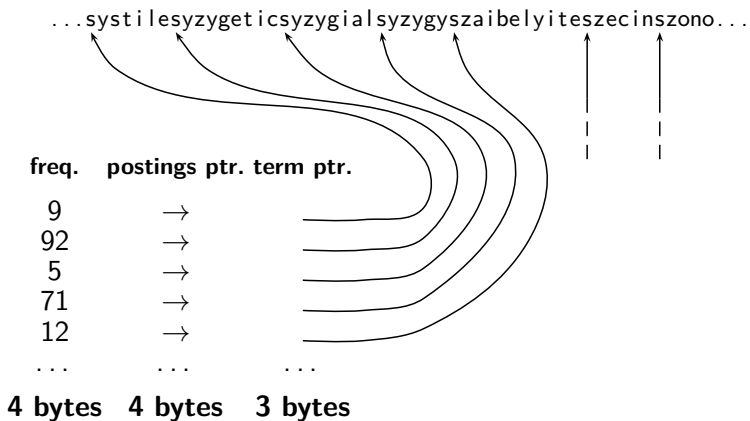
space needed: 20 bytes 4 bytes 4 bytes

Space for Reuters: $(20+4+4)*400,000 = 11.2$ MB

Fixed-width entries are bad.

- Most of the bytes in the term column are wasted.
 - We allot 20 bytes for terms of length 1.
- We cannot handle HYDROCHLOROFLUOROCARBONS and SUPERCALIFRAGILISTICEXPIALIDOCIOUS
- Average length of a term in English: 8 characters (or a little bit less)
- How can we use on average 8 characters per term?

Dictionary as a string



Space for dictionary as a string

- 4 bytes per term for frequency
- 4 bytes per term for pointer to postings list
- 8 bytes (on average) for term in string
- 3 bytes per pointer into string (need $\log_2 8 \cdot 400,000 < 24$ bits to resolve $8 \cdot 400,000$ positions)
- Space: $400,000 \times (4 + 4 + 3 + 8) = 7.6$ MB (compared to 11.2 MB for fixed-width array)

Dictionary as a string with blocking

...7systile9syzygetic8syzygia16syzygy11szaibelyite6szecin...

| freq. | postings ptr. | term ptr. |
|-------|---------------|-----------|
|-------|---------------|-----------|

| | | |
|---|---|--|
| 9 | → | |
|---|---|--|

| | | |
|----|---|--|
| 92 | → | |
|----|---|--|

| | | |
|---|---|--|
| 5 | → | |
|---|---|--|

| | | |
|----|---|--|
| 71 | → | |
|----|---|--|

| | | |
|----|---|--|
| 12 | → | |
|----|---|--|

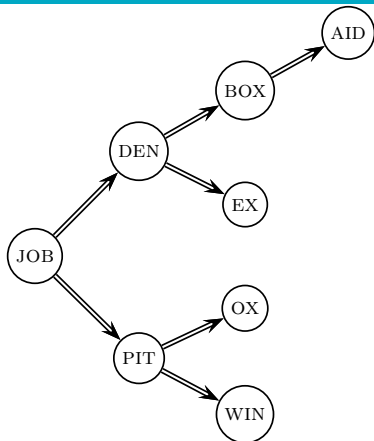
| | | |
|-----|-----|-----|
| ... | ... | ... |
|-----|-----|-----|

...

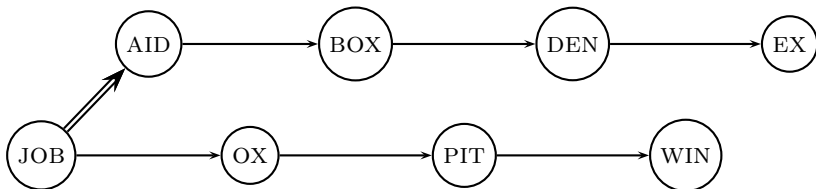
Space for dictionary as a string with blocking

- Example block size $k = 4$
- Where we used 4×3 bytes for term pointers without blocking
...
- ... we now use 3 bytes for one pointer plus 4 bytes for indicating the length of each term.
- We save $12 - (3 + 4) = 5$ bytes per block.
- Total savings: $400,000/4 * 5 = 0.5$ MB
- This reduces the size of the dictionary from 7.6 MB to 7.1 MB.

Lookup of a term without blocking



Lookup of a term with blocking: (slightly) slower



Front coding

One block in blocked compression ($k = 4$) ...

8 a u t o m a t a **8** a u t o m a t e **9** a u t o m a t i c **10** a u t o m a t i o n



... further compressed with front coding.

8 a u t o m a t * a **1** ◊ e **2** ◊ i c **3** ◊ i o n

Dictionary compression for Reuters: Summary

| data structure | size in MB |
|---------------------------------------|------------|
| dictionary, fixed-width | 11.2 |
| dictionary, term pointers into string | 7.6 |
| ~, with blocking, $k = 4$ | 7.1 |
| ~, with blocking & front coding | 5.9 |

Exercise

- Which prefixes should be used for front coding? What are the tradeoffs?
- Input: list of terms (= the term vocabulary)
- Output: list of prefixes that will be used in front coding

Postings compression

- The postings file is much larger than the dictionary, factor of at least 10.
- Key desideratum: store each posting compactly
- A posting for our purposes is a docID.
- For Reuters (800,000 documents), we would use 32 bits per docID when using 4-byte integers.
- Alternatively, we can use $\log_2 800,000 \approx 19.6 < 20$ bits per docID.
- Our goal: use a lot less than 20 bits per docID.

Key idea: Store gaps instead of docIDs

- Each postings list is ordered in increasing order of docID.
- Example postings list: COMPUTER: 283154, 283159, 283202, ...
- It suffices to store **gaps**: $283159 - 283154 = 5$, $283202 - 283159 = 43$
- Example postings list using gaps: COMPUTER: 283154, 5, 43, ...
- Gaps for frequent terms are small.
- Thus: We can encode small gaps with fewer than 20 bits.

Gap encoding

| | encoding | postings list | | | | |
|----------------|----------|---------------|--------|--------|--------|------------|
| THE | docIDs | ... | 283042 | 283043 | 283044 | 283045 ... |
| | gaps | | 1 | 1 | 1 | ... |
| COMPUTER | docIDs | ... | 283047 | 283154 | 283159 | 283202 ... |
| | gaps | | 107 | 5 | 43 | ... |
| ARACHNOCENTRIC | docIDs | 252000 | 500100 | | | |
| | gaps | 252000 | 248100 | | | |

Variable length encoding

- Aim:
 - For ARACHNOCENTRIC and other rare terms, we will use about 20 bits per gap (= posting).
 - For THE and other very frequent terms, we will use only a few bits per gap (= posting).
- In order to implement this, we need to devise some form of [variable length encoding](#).
- Variable length encoding uses few bits for small gaps and many bits for large gaps.

Variable byte (VB) code

- Used by many commercial/research systems
- Good low-tech blend of variable-length coding and sensitivity to alignment matches (bit-level codes, see later).
- Dedicate 1 bit (high bit) to be a **continuation bit** c .
- If the gap G fits within 7 bits, binary-encode it in the 7 available bits and set $c = 1$.
- Else: encode lower-order 7 bits and then use one or more additional bytes to encode the higher order bits using the same algorithm.
- At the end set the continuation bit of the last byte to 1 ($c = 1$) and of the other bytes to 0 ($c = 0$).

VB code examples

| | | | | | | |
|---------|----------|----------|----------|----------|----------|----------|
| docIDs | 824 | | 829 | | 215406 | |
| gaps | | | 5 | | 214577 | |
| VB code | 00000110 | 10111000 | 10000101 | 00001101 | 00001100 | 10110001 |

VB code encoding algorithm

VBENCODENUMBER(n)

```
1 bytes  $\leftarrow \langle \rangle$ 
2 while true
3 do PREPEND(bytes,  $n \bmod 128$ )
4   if  $n < 128$ 
5     then BREAK
6    $n \leftarrow n \text{ div } 128$ 
7 bytes[LENGTH(bytes)] += 128
8 return bytes
```

VBENCODE(*numbers*)

```
1 bytestream  $\leftarrow \langle \rangle$ 
2 for each  $n \in \textit{numbers}$ 
3 do bytes  $\leftarrow$  VBENCODENUMBER( $n$ )
4   bytestream  $\leftarrow$  EXTEND(bytestream, bytes)
5 return bytestream
```

VB code decoding algorithm

```
VBDECODE(bytestream)
1  numbers  $\leftarrow \langle \rangle$ 
2  n  $\leftarrow 0$ 
3  for i  $\leftarrow 1$  to LENGTH(bytestream)
4  do if bytestream[i] < 128
5      then n  $\leftarrow 128 \times n + \textit{bytestream}[i]$ 
6      else n  $\leftarrow 128 \times n + (\textit{bytestream}[i] - 128)$ 
7          APPEND(numbers, n)
8          n  $\leftarrow 0$ 
9  return numbers
```


Other variable codes

- Instead of bytes, we can also use a different “unit of alignment”: 32 bits (words), 16 bits, 4 bits (nibbles), etc.
- Variable byte alignment wastes space if you have many small gaps – nibbles do better on those.
- There is work on word-aligned codes that efficiently “pack” a variable number of gaps into one word – see resources at the end

Codes for gap encoding

- You can get even more compression with another type of variable length encoding: [bitlevel](#) code.
- Gamma code is the best known of these.
- First, we need unary code to be able to introduce gamma code.
- Unary code
 - Represent n as n 1s with a final 0.
 - Unary code for 3 is 1110
 - Unary code for 1 is 10, for 0 is 0, for 30 is 11111111111111111111111111111110

Gamma code

- Represent a gap G as a pair of **length** and **offset**.
- Offset is the gap in binary, with the leading bit chopped off.
- For example $13 \rightarrow 1101 \rightarrow 101 = \text{offset}$
- Length is the length of offset.
- For 13 (offset 101), this is 3.
- Encode length in **unary** code: 1110.
- Gamma code of 13 is the concatenation of length and offset: 1110101.

Another Gamma code (γ) examples

| number | unary code | length | offset | γ code |
|--------|------------|--------------|------------|-------------------------|
| 0 | 0 | | | |
| 1 | 10 | 0 | | 0 |
| 2 | 110 | 10 | 0 | 10,0 |
| 3 | 1110 | 10 | 1 | 10,1 |
| 4 | 11110 | 110 | 00 | 110,00 |
| 9 | 1111111110 | 1110 | 001 | 1110,001 |
| 13 | | 1110 | 101 | 1110,101 |
| 24 | | 11110 | 1000 | 11110,1000 |
| 511 | | 1111111110 | 11111111 | 111111110,11111111 |
| 1025 | | 111111111110 | 0000000001 | 111111111110,0000000001 |

The universal coding of the integers: Elias codes

- ☞ unary code $\alpha(N) = \underbrace{11\dots1}_N 0$. $\alpha(4) = 11110$
- ☞ binary code $\beta(1) = 1, \beta(2N + j) = \beta(N)j, j = 0, 1$. $\beta(4) = 100$
- ☞ β is not uniquely decodable (it is not a prefix code).
- ☞ ternary $\tau(N) = \beta(N)\#$. $\tau(4) = 100\#$
- ☞ $\beta'(1) = \epsilon, \beta'(2N) = \beta'(N)0, \beta'(2N + 1) = \beta'(N)1,$
 $\tau'(N) = \beta'(N)\#$. $\beta'(4) = 00$.
- ☞ $\gamma(N) = \alpha|\beta'(N)|\beta'(N)$. $\gamma(4) = 11000$
- ☞ alternatively, γ' : every bit $\beta'(N)$ is inserted between a pair from $\alpha(|\beta'(N)|)$. the same length as γ (bit permutation $\gamma(N)$), but less readable
- ☞ example: $\gamma'(4) = 1\bar{0}1\bar{0}0$
- ☞ $C_\gamma = \{\gamma(N) : N > 0\} = (1\{0, 1\})^*0$ is regular and therefore it is decodable by finite automaton.

Elias codes: gamma, delta, omega: formal definitions II

☞ $\delta(N) = \gamma(|\beta(N)|)\beta'(N)$

☞ example: $\delta(4) = \gamma(3)00 = 01100$

☞ decoder δ : $\delta(?) = 1001?$

☞ ω :

```
K := 0;
```

```
while  $\lfloor \log_2(N) \rfloor > 0$  do
```

```
  begin K :=  $\beta(N)K$ ;
```

```
    N :=  $\lfloor \log_2(N) \rfloor$ 
```

```
  end.
```

Exercise

- Compute the variable byte code of 130
- Compute the gamma code of 130
- Compute $\delta(42)$

Length of gamma code

- The length of *offset* is $\lfloor \log_2 G \rfloor$ bits.
- The length of *length* is $\lfloor \log_2 G \rfloor + 1$ bits,
- So the length of the entire code is $2 \times \lfloor \log_2 G \rfloor + 1$ bits.
- γ codes are always of odd length.
- Gamma codes are within a factor of 2 of the optimal encoding length $\log_2 G$.
 - (assuming the frequency of a gap G is proportional to $\log_2 G$ – only approximately true)

Gamma code: Properties

- Gamma code is **prefix-free**: a valid code word is not a prefix of any other valid code.
- Encoding is optimal within a factor of 3 (and within a factor of 2 making additional assumptions).
- This result is independent of the distribution of gaps!
- We can use gamma codes for any distribution. Gamma code is **universal**.
- Gamma code is **parameter-free**.

Gamma codes: Alignment

- Machines have word boundaries – 8, 16, 32 bits
- Compressing and manipulating at granularity of bits can be slow.
- Variable byte encoding is aligned and thus potentially more efficient.
- Another word aligned scheme: Anh and Moffat 2005
- Regardless of efficiency, variable byte is conceptually simpler at little additional space cost.

Compression of Reuters

| data structure | size in MB |
|---------------------------------------|--------------|
| dictionary, fixed-width | 11.2 |
| dictionary, term pointers into string | 7.6 |
| ~, with blocking, $k = 4$ | 7.1 |
| ~, with blocking & front coding | 5.9 |
| collection (text, xml markup, etc.) | 3600.0 |
| collection (text) | 960.0 |
| T/D incidence matrix | 40,000.0 |
| postings, uncompressed (32-bit words) | 400.0 |
| postings, uncompressed (20 bits) | 250.0 |
| postings, variable byte encoded | 116.0 |
| postings, γ encoded | 101.0 |

Term-document incidence matrix

| | Anthony and Cleopatra | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth | ... |
|-----------|-----------------------------|------------------|----------------|--------|---------|---------|-----|
| ANTHONY | 1 | 1 | 0 | 0 | 0 | 1 | |
| BRUTUS | 1 | 1 | 0 | 1 | 0 | 0 | |
| CAESAR | 1 | 1 | 0 | 1 | 1 | 1 | |
| CALPURNIA | 0 | 1 | 0 | 0 | 0 | 0 | |
| CLEOPATRA | 1 | 0 | 0 | 0 | 0 | 0 | |
| MERCY | 1 | 0 | 1 | 1 | 1 | 1 | |
| WORSER | 1 | 0 | 1 | 1 | 1 | 0 | |

...

Entry is 1 if term occurs.

Example: CALPURNIA occurs in *Julius Caesar*.

Entry is 0 if term does not occur.

Example: CALPURNIA doesn't occur in *The tempest*.

Compression of Reuters

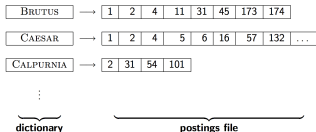
| data structure | size in MB |
|---------------------------------------|--------------|
| dictionary, fixed-width | 11.2 |
| dictionary, term pointers into string | 7.6 |
| ~, with blocking, $k = 4$ | 7.1 |
| ~, with blocking & front coding | 5.9 |
| collection (text, xml markup, etc.) | 3600.0 |
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| postings, uncompressed (32-bit words) | 400.0 |
| postings, uncompressed (20 bits) | 250.0 |
| postings, variable byte encoded | 116.0 |
| postings, γ encoded | 101.0 |

Summary

- We can now create an index for highly efficient Boolean retrieval that is very space efficient.
- Only 4% of the total size of the collection.
- Only 10–15% of the total size of the text in the collection.
- However, we've ignored positional and frequency information.
- For this reason, space savings are less in reality.

Take-away today

For each term t , we store a list of all documents that contain t .



- Motivation for compression in information retrieval systems
- How can we compress the **dictionary** component of the inverted index?
- How can we compress the **postings** component of the inverted index?
- Term statistics: how are terms distributed in document collections?

Resources

`http://ske.fi.muni.cz`

- Chapter 5 of IIR
- Resources at `https://www.fi.muni.cz/~sojka/PV211/` and `http://cislmu.org`, materials in MU IS and FI MU library
 - Original publication on word-aligned binary codes by Anh and Moffat (2005); also: Anh and Moffat (2006a).
 - Original publication on variable byte codes by Scholer, Williams, Yiannis and Zobel (2002).
 - More details on compression (including compression of positions and frequencies) in Zobel and Moffat (2006).

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 6: Scoring, term weighting, the vector space model

Handout version

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(compiled on 2024-03-08 15:05:57)

Overview

- 1 Why ranked retrieval?
- 2 Term frequency
- 3 tf-idf weighting
- 4 The vector space model

Take-away today

- **Ranking** search results: why it is important (as opposed to just presenting a set of unordered Boolean results)
- **Term frequency**: This is a key ingredient for ranking.
- **Tf-idf ranking**: best known traditional ranking scheme
- **Vector space model**: One of the most important formal models for information retrieval (along with Boolean and probabilistic models)

Ranked retrieval

- Thus far, our queries have been **Boolean**.
 - Documents either match or do not.
- **Good for expert users** with precise understanding of their needs and of the collection.
- Also **good for applications**: Applications can easily consume 1000s of results.
- **Not good for the majority of users**
- Most users are not capable of writing Boolean queries ...
 - ...or they are, but they think it's too much work.
- Most users don't want to wade through 1000s of results.
- This is particularly true of web search.

Problem with Boolean search: Feast or famine

- Boolean queries often result in either too few ($=0$) or too many (1000s) results.
- Query 1 (boolean conjunction): [standard user dlink 650]
 - \rightarrow 200,000 hits – [feast](#)
- Query 2 (boolean conjunction): [standard user dlink 650 no card found]
 - \rightarrow 0 hits – [famine](#)
- In Boolean retrieval, it takes a lot of skill to come up with a query that produces a manageable number of hits.

Feast or famine: No problem in ranked retrieval

- With ranking, large result sets are not an issue.
- Just show the top 10 results
- Doesn't overwhelm the user
- Premise: the ranking algorithm works: **More relevant results are ranked higher than less relevant results.**

Scoring as the basis of ranked retrieval

- We wish to rank documents that are more relevant higher than documents that are less relevant.
- How can we accomplish such a ranking of the documents in the collection with respect to a query?
- Assign a score to each query-document pair, say in $[0, 1]$.
- This score measures how well document and query “match”.

Query-document matching scores

- How do we compute the score of a query-document pair?
- Let's start with a one-term query.
- If the query term does not occur in the document: score should be 0.
- The more frequent the query term in the document, the higher the score.
- We will look at a number of alternatives for doing this.

Take 1: Jaccard coefficient

- A commonly used measure of overlap of two sets
- Let A and B be two sets
- Jaccard coefficient:

$$\text{JACCARD}(A, B) = \frac{|A \cap B|}{|A \cup B|}$$

($A \neq \emptyset$ or $B \neq \emptyset$)

- $\text{JACCARD}(A, A) = 1$
- $\text{JACCARD}(A, B) = 0$ if $A \cap B = \emptyset$
- A and B don't have to be the same size.
- Always assigns a number between 0 and 1.

Jaccard coefficient: Example

- What is the query-document match score that the Jaccard coefficient computes for:
 - Query: “ides of March”
 - Document “Caesar died in March”
 - $JACCARD(q, d) = 1/6$

What's wrong with Jaccard?

- It doesn't consider term frequency (how many occurrences a term has).
- Rare terms are more informative than frequent terms. Jaccard does not consider this information.
- We need a more sophisticated way of normalizing for the length of a document.
- Later in this lecture, we'll use $|A \cap B| / \sqrt{|A \cup B|}$ (cosine) ...
- ... instead of $|A \cap B| / |A \cup B|$ (Jaccard) for length normalization.

Binary incidence matrix

| | Anthony and Cleopatra | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth | ... |
|-----------|-----------------------------|------------------|----------------|--------|---------|---------|-----|
| ANTHONY | 1 | 1 | 0 | 0 | 0 | 1 | |
| BRUTUS | 1 | 1 | 0 | 1 | 0 | 0 | |
| CAESAR | 1 | 1 | 0 | 1 | 1 | 1 | |
| CALPURNIA | 0 | 1 | 0 | 0 | 0 | 0 | |
| CLEOPATRA | 1 | 0 | 0 | 0 | 0 | 0 | |
| MERCY | 1 | 0 | 1 | 1 | 1 | 1 | |
| WORSER | 1 | 0 | 1 | 1 | 1 | 0 | |
| ... | | | | | | | |

Each document is represented as a **binary vector** $\in \{0, 1\}^{\dim(V)}$.

Count matrix

| | Anthony and Cleopatra | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth | ... |
|-----------|-----------------------------|------------------|----------------|--------|---------|---------|-----|
| ANTHONY | 157 | 73 | 0 | 0 | 0 | 1 | |
| BRUTUS | 4 | 157 | 0 | 2 | 0 | 0 | |
| CAESAR | 232 | 227 | 0 | 2 | 1 | 0 | |
| CALPURNIA | 0 | 10 | 0 | 0 | 0 | 0 | |
| CLEOPATRA | 57 | 0 | 0 | 0 | 0 | 0 | |
| MERCY | 2 | 0 | 3 | 8 | 5 | 8 | |
| WORSER | 2 | 0 | 1 | 1 | 1 | 5 | |
| ... | | | | | | | |

Each document is now represented as a **count vector** $\in \mathbb{N}^{\dim(V)}$.

Bag of words model

- We do not consider the **order** of words in a document.
- *John is quicker than Mary* and *Mary is quicker than John* are represented the same way.
- This is called a **bag of words model**.
- In a sense, this is a step back: The positional index was able to distinguish these two documents.
- We will look at “recovering” positional information later in this course.
- For now: bag of words model

Term frequency tf

- The term frequency $tf_{t,d}$ of term t in document d is defined as the **number of times that t occurs in d** .
- We want to use tf when computing query-document match scores.
- But how?
- Raw term frequency is not what we want because:
- **A document with $tf = 10$ occurrences of the term is more relevant than a document with $tf = 1$ occurrence of the term.**
- But not 10 times more relevant.
- **Relevance does not increase proportionally with term frequency.**

Instead of raw frequency: Log frequency weighting

- The log frequency weight of term t in d is defined as follows

$$w_{t,d} = \begin{cases} 1 + \log_{10} \text{tf}_{t,d} & \text{if } \text{tf}_{t,d} > 0 \\ 0 & \text{otherwise} \end{cases}$$

- $\text{tf}_{t,d} \rightarrow w_{t,d}$:
 $0 \rightarrow 0, 1 \rightarrow 1, 2 \rightarrow 1.3, 10 \rightarrow 2, 1000 \rightarrow 4$, etc.
- Score for a document-query pair: sum over terms t in both q and d :
 $\text{tf-matching-score}(q, d) = \sum_{t \in q \cap d} (1 + \log \text{tf}_{t,d})$
- The score is 0 if none of the query terms is present in the document.

Exercise

- Compute the Jaccard matching score and the tf matching score for the following query-document pairs.
- q: [information on cars] d: “all you’ve ever wanted to know about cars”
- q: [information on cars] d: “information on trucks, information on planes, information on trains”
- q: [red cars and red trucks] d: “cops stop red cars more often”

Frequency in document vs. frequency in collection

- In addition, to term frequency (the frequency of the term in the document) ...
- ... we also want to use the frequency of the term **in the collection** for weighting and ranking.

Desired weight for rare terms

- Rare terms are more informative than frequent terms.
- Consider a term in the query that is **rare** in the collection (e.g., ARACHNOCENTRIC).
- A document containing this term is very likely to be relevant.
- → We want **high weights for rare terms** like ARACHNOCENTRIC.

Desired weight for frequent terms

- Frequent terms are less informative than rare terms.
- Consider a term in the query that is **frequent** in the collection (e.g., GOOD, INCREASE, LINE).
- A document containing this term is more likely to be relevant than a document that doesn't ...
- ...but words like GOOD, INCREASE and LINE are not sure indicators of relevance.
- → **For frequent terms** like GOOD, INCREASE, and LINE, we want positive weights ...
- ...but **lower weights** than for rare terms.

Document frequency

- We want **high weights for rare terms** like ARACHNOCENTRIC.
- We want **low (positive) weights for frequent words** like GOOD, INCREASE, and LINE.
- We will use **document frequency** to factor this into computing the matching score.
- The document frequency is **the number of documents in the collection that the term occurs in.**

idf weight

- df_t is the document frequency, the number of documents that t occurs in.
- df_t is an inverse measure of the **informativeness** of term t .
- We define the **idf weight** of term t as follows:

$$\text{idf}_t = \log_{10} \frac{N}{df_t}$$

(N is the number of documents in the collection.)

- idf_t is a measure of the **informativeness** of the term.
- $[\log N/df_t]$ instead of $[N/df_t]$ to “dampen” the effect of idf
- Note that we use the log transformation for both term frequency and document frequency.

Examples for idf

Compute idf_t using the formula: $idf_t = \log_{10} \frac{1,000,000}{df_t}$

| term | df_t | idf_t |
|-----------|-----------|---------|
| calpurnia | 1 | 6 |
| animal | 100 | 4 |
| sunday | 1000 | 3 |
| fly | 10,000 | 2 |
| under | 100,000 | 1 |
| the | 1,000,000 | 0 |

Effect of idf on ranking

- idf affects the ranking of documents for **queries with at least two terms**.
- For example, in the query “arachnocentric line”, idf weighting **increases** the relative weight of ARACHNOCENTRIC and **decreases** the relative weight of LINE.
- idf has **little effect** on ranking for **one-term queries**.

Collection frequency vs. Document frequency

| word | collection frequency | document frequency |
|-----------|----------------------|--------------------|
| INSURANCE | 10440 | 3997 |
| TRY | 10422 | 8760 |

- Collection frequency of t : number of tokens of t in the collection
- Document frequency of t : number of documents t occurs in
- Why these numbers?
- Which word is a better search term (and should get a higher weight)?
- This example suggests that df (and idf) is better for weighting than cf (and “icf”).

tf-idf weighting

- The tf-idf weight of a term is the **product of its tf weight and its idf weight.**



$$w_{t,d} = (1 + \log \text{tf}_{t,d}) \cdot \log \frac{N}{\text{df}_t}$$

- **tf-weight**
- **idf-weight**
- Best known weighting scheme in information retrieval
- Note: the “-” in tf-idf is a hyphen, not a minus sign!
- Alternative names: tf.idf, tf x idf

Summary: tf-idf

- Assign a tf-idf weight for each term t in each document d :
$$w_{t,d} = (1 + \log \text{tf}_{t,d}) \cdot \log \frac{N}{\text{df}_t}$$
- The tf-idf weight ...
 - ... increases with the number of occurrences within a document. (term frequency)
 - ... increases with the rarity of the term in the collection. (inverse document frequency)

Exercise: Term, collection and document frequency

| Quantity | Symbol | Definition |
|----------------------|------------|--|
| term frequency | $tf_{t,d}$ | number of occurrences of t in d |
| document frequency | df_t | number of documents in the collection that t occurs in |
| collection frequency | cf_t | total number of occurrences of t in the collection |

- Relationship between df and cf ?
- Relationship between tf and cf ?
- Relationship between tf and df ?

Binary incidence matrix

| | Anthony and Cleopatra | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth | ... |
|-----------|-----------------------------|------------------|----------------|--------|---------|---------|-----|
| ANTHONY | 1 | 1 | 0 | 0 | 0 | 1 | |
| BRUTUS | 1 | 1 | 0 | 1 | 0 | 0 | |
| CAESAR | 1 | 1 | 0 | 1 | 1 | 1 | |
| CALPURNIA | 0 | 1 | 0 | 0 | 0 | 0 | |
| CLEOPATRA | 1 | 0 | 0 | 0 | 0 | 0 | |
| MERCY | 1 | 0 | 1 | 1 | 1 | 1 | |
| WORSER | 1 | 0 | 1 | 1 | 1 | 0 | |
| ... | | | | | | | |

Each document is represented as a **binary vector** $\in \{0, 1\}^{\dim(V)}$.

Count matrix

| | Anthony and Cleopatra | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth | ... |
|-----------|-----------------------------|------------------|----------------|--------|---------|---------|-----|
| ANTHONY | 157 | 73 | 0 | 0 | 0 | 1 | |
| BRUTUS | 4 | 157 | 0 | 2 | 0 | 0 | |
| CAESAR | 232 | 227 | 0 | 2 | 1 | 0 | |
| CALPURNIA | 0 | 10 | 0 | 0 | 0 | 0 | |
| CLEOPATRA | 57 | 0 | 0 | 0 | 0 | 0 | |
| MERCY | 2 | 0 | 3 | 8 | 5 | 8 | |
| WORSER | 2 | 0 | 1 | 1 | 1 | 5 | |
| ... | | | | | | | |

Each document is now represented as a **count vector** $\in \mathbb{N}^{\dim(V)}$.

Binary \rightarrow count \rightarrow weight matrix

| | Anthony and Cleopatra | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth | ... |
|-----------|-----------------------------|------------------|----------------|--------|---------|---------|-----|
| ANTHONY | 5.25 | 3.18 | 0.0 | 0.0 | 0.0 | 0.35 | |
| BRUTUS | 1.21 | 6.10 | 0.0 | 1.0 | 0.0 | 0.0 | |
| CAESAR | 8.59 | 2.54 | 0.0 | 1.51 | 0.25 | 0.0 | |
| CALPURNIA | 0.0 | 1.54 | 0.0 | 0.0 | 0.0 | 0.0 | |
| CLEOPATRA | 2.85 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | |
| MERCY | 1.51 | 0.0 | 1.90 | 0.12 | 5.25 | 0.88 | |
| WORSER | 1.37 | 0.0 | 0.11 | 4.15 | 0.25 | 1.95 | |
| ... | | | | | | | |

Each document is now represented as a **real-valued vector** of tf-idf weights $\in \mathbb{R}^{|V|}$.

Documents as vectors

- Each document is now represented as a real-valued vector of tf-idf weights $\in \mathbb{R}^{|V|}$.
- So we have a $|V|$ -dimensional real-valued vector space.
- Terms are **axes** of the space.
- Documents are **points** or **vectors** in this space.
- Very high-dimensional: tens of millions of dimensions when you apply this to web search engines
- Each vector is very sparse - most entries are zero.

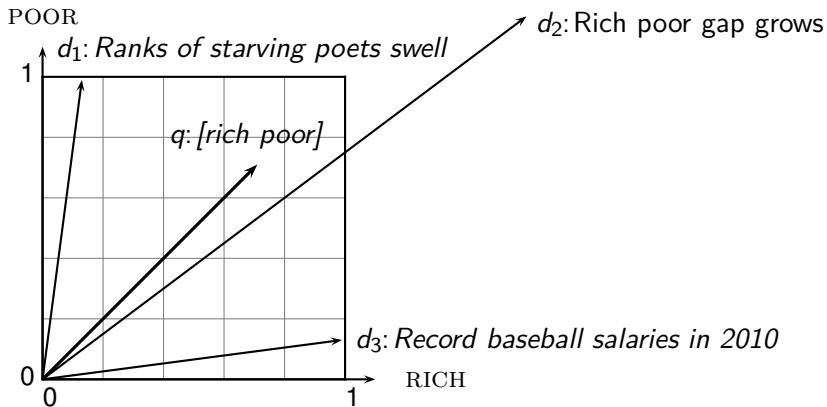
Queries as vectors

- Key idea 1: do the same for queries: represent them as vectors in the high-dimensional space
- Key idea 2: Rank documents according to their proximity to the query
- proximity = similarity
- proximity \approx negative distance
- Recall: We're doing this because we want to get away from the you're-either-in-or-out, feast-or-famine Boolean model.
- Instead: rank relevant documents higher than nonrelevant documents.

How do we formalize vector space similarity?

- First cut: (negative) distance between two points
- (= distance between the end points of the two vectors)
- Euclidean distance?
- Euclidean distance is a bad idea . . .
- . . . because Euclidean distance is **large** for vectors **of different lengths**.

Why distance is a bad idea



The Euclidean distance of \vec{q} and \vec{d}_2 is large although the distribution of terms in the query q and the distribution of terms in the document d_2 are very similar.

Questions about basic vector space setup?

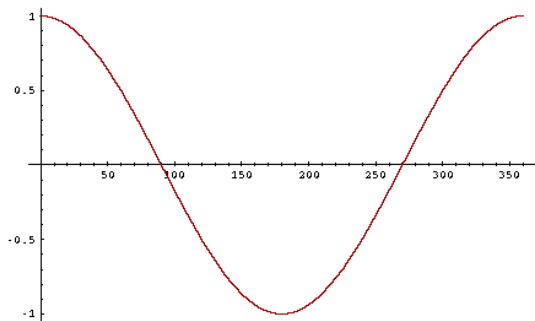
Use angle instead of distance

- Rank documents according to angle with query
- Thought experiment: take a document d and append it to itself. Call this document d' . d' is twice as long as d .
- “Semantically” d and d' have the same content.
- The angle between the two documents is 0, corresponding to maximal similarity . . .
- . . . even though the Euclidean distance between the two documents can be quite large.

From angles to cosines

- The following two notions are equivalent.
 - Rank documents according to the **angle** between query and document in decreasing order
 - Rank documents according to **cosine**(query,document) in increasing order
- Cosine is a monotonically decreasing function of the angle for the interval $[0^\circ, 180^\circ]$

Cosine



Length normalization

- How do we compute the cosine?
- A vector can be (length-) normalized by dividing each of its components by its length – here we use the L_2 norm:
$$\|x\|_2 = \sqrt{\sum_i x_i^2}$$
- This maps vectors onto the unit sphere ...
- ... since after normalization: $\|x\|_2 = \sqrt{\sum_i x_i^2} = 1.0$
- As a result, longer documents and shorter documents have weights of the same order of magnitude.
- Effect on the two documents d and d' (d appended to itself) from earlier slide: they have **identical vectors** after length-normalization.

Cosine similarity between query and document

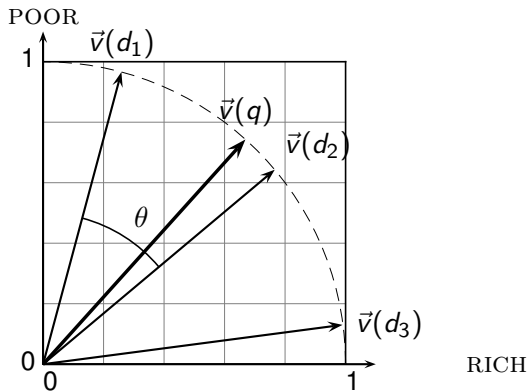
$$\cos(\vec{q}, \vec{d}) = \text{SIM}(\vec{q}, \vec{d}) = \frac{\vec{q} \cdot \vec{d}}{|\vec{q}||\vec{d}|} = \frac{\sum_{i=1}^{|\mathcal{V}|} q_i d_i}{\sqrt{\sum_{i=1}^{|\mathcal{V}|} q_i^2} \sqrt{\sum_{i=1}^{|\mathcal{V}|} d_i^2}}$$

- q_i is the tf-idf weight of term i in the query.
- d_i is the tf-idf weight of term i in the document.
- $|\vec{q}|$ and $|\vec{d}|$ are the lengths of \vec{q} and \vec{d} .
- This is the **cosine similarity** of \vec{q} and \vec{d} or, equivalently, the cosine of the angle between \vec{q} and \vec{d} .

Cosine for normalized vectors

- For normalized vectors, the cosine is equivalent to the dot product or scalar product.
- $\cos(\vec{q}, \vec{d}) = \vec{q} \cdot \vec{d} = \sum_i q_i \cdot d_i$
 - (if \vec{q} and \vec{d} are length-normalized).

Cosine similarity illustrated



Cosine: Example

How similar are these novels?

SaS: Sense and Sensibility

PaP: Pride and Prejudice

WH: Wuthering Heights

term frequencies (counts)

| term | SaS | PaP | WH |
|-----------|-----|-----|----|
| AFFECTION | 115 | 58 | 20 |
| JEALOUS | 10 | 7 | 11 |
| GOSSIP | 2 | 0 | 6 |
| WUTHERING | 0 | 0 | 38 |

Cosine: Example

term frequencies (counts)

| term | SaS | PaP | WH |
|-----------|-----|-----|----|
| AFFECTION | 115 | 58 | 20 |
| JEALOUS | 10 | 7 | 11 |
| GOSSIP | 2 | 0 | 6 |
| WUTHERING | 0 | 0 | 38 |

log frequency weighting

| term | SaS | PaP | WH |
|-----------|------|------|------|
| AFFECTION | 3.06 | 2.76 | 2.30 |
| JEALOUS | 2.0 | 1.85 | 2.04 |
| GOSSIP | 1.30 | 0 | 1.78 |
| WUTHERING | 0 | 0 | 2.58 |

(To simplify this example, we don't do idf weighting.)

Cosine: Example

log frequency weighting

| term | SaS | PaP | WH |
|-----------|------|------|------|
| AFFECTION | 3.06 | 2.76 | 2.30 |
| JEALOUS | 2.0 | 1.85 | 2.04 |
| GOSSIP | 1.30 | 0 | 1.78 |
| WUTHERING | 0 | 0 | 2.58 |

log frequency weighting
& cosine normalization

| term | SaS | PaP | WH |
|-----------|-------|-------|-------|
| AFFECTION | 0.789 | 0.832 | 0.524 |
| JEALOUS | 0.515 | 0.555 | 0.465 |
| GOSSIP | 0.335 | 0.0 | 0.405 |
| WUTHERING | 0.0 | 0.0 | 0.588 |

- $\cos(\text{SaS}, \text{PaP}) \approx 0.789 * 0.832 + 0.515 * 0.555 + 0.335 * 0.0 + 0.0 * 0.0 \approx 0.94$.
- $\cos(\text{SaS}, \text{WH}) \approx 0.79$
- $\cos(\text{PaP}, \text{WH}) \approx 0.69$
- Why do we have $\cos(\text{SaS}, \text{PaP}) > \cos(\text{SAS}, \text{WH})$?

Computing the cosine score

COSINESCORE(q)

```
1  float Scores[ $N$ ] = 0
2  float Length[ $N$ ]
3  for each query term  $t$ 
4  do calculate  $w_{t,q}$  and fetch postings list for  $t$ 
5      for each pair( $d, tf_{t,d}$ ) in postings list
6          do  $Scores[d] += w_{t,d} \times w_{t,q}$ 
7  Read the array Length
8  for each  $d$ 
9  do  $Scores[d] = Scores[d] / Length[d]$ 
10 return Top  $K$  components of Scores[]
```

Components of tf-idf weighting

| Term frequency | | Document frequency | | Normalization | |
|----------------|---|--------------------|---------------------------------------|--------------------|--|
| n (natural) | $tf_{t,d}$ | n (no) | 1 | n (none) | 1 |
| l (logarithm) | $1 + \log(tf_{t,d})$ | t (idf) | $\log \frac{N}{df_t}$ | c (cosine) | $\frac{1}{\sqrt{w_1^2 + w_2^2 + \dots + w_M^2}}$ |
| a (augmented) | $0.5 + \frac{0.5 \times tf_{t,d}}{\max_t(tf_{t,d})}$ | p (prob idf) | $\max\{0, \log \frac{N-df_t}{df_t}\}$ | u (pivoted unique) | $1/u$ |
| b (boolean) | $\begin{cases} 1 & \text{if } tf_{t,d} > 0 \\ 0 & \text{otherwise} \end{cases}$ | | | b (byte size) | $1/CharLength^\alpha$, $\alpha < 1$ |
| L (log ave) | $\frac{1 + \log(tf_{t,d})}{1 + \log(\text{ave}_{t \in d}(tf_{t,d}))}$ | | | | |

Best known combination of weighting options

Default: no weighting

tf-idf example

- We often use **different weightings** for queries and documents.
- Notation: ddd.qqq
- Example: Inc.ltn
- document: logarithmic tf, no df weighting, cosine normalization
- query: logarithmic tf, idf, no normalization
- **Isn't it bad to not idf-weight the document?**
- Example query: “best car insurance”
- Example document: “car insurance auto insurance”

tf-idf example: Inc.ltn

Query: "best car insurance". Document: "car insurance auto insurance".

| word | query | | | | | document | | | | product |
|-----------|--------|---------|-------|-----|--------|----------|---------|--------|---------|---------|
| | tf-raw | tf-wght | df | idf | weight | tf-raw | tf-wght | weight | n'lized | |
| auto | 0 | 0 | 5000 | 2.3 | 0 | 1 | 1 | 1 | 0.52 | 0 |
| best | 1 | 1 | 50000 | 1.3 | 1.3 | 0 | 0 | 0 | 0 | 0 |
| car | 1 | 1 | 10000 | 2.0 | 2.0 | 1 | 1 | 1 | 0.52 | 1.04 |
| insurance | 1 | 1 | 1000 | 3.0 | 3.0 | 2 | 1.3 | 1.3 | 0.68 | 2.04 |

Key to columns: **tf-raw**: raw (unweighted) term frequency, **tf-wght**: logarithmically weighted term frequency, **df**: document frequency, **idf**: inverse document frequency, **weight**: the final weight of the term in the query or document, **n'lized**: document weights after cosine normalization, **product**: the product of final query weight and final document weight

$$\sqrt{1^2 + 0^2 + 1^2 + 1.3^2} \approx 1.92$$

$$1/1.92 \approx 0.52$$

$$1.3/1.92 \approx 0.68$$

Final similarity score between query and document: $\sum_i w_{qi} \cdot w_{di} = 0 + 0 + 1.04 + 2.04 = 3.08$

Questions?

Summary: Ranked retrieval in the vector space model

- Represent the query as a weighted tf-idf vector
- Represent each document as a weighted tf-idf vector
- Compute the cosine similarity between the query vector and each document vector
- Rank documents with respect to the query
- Return the top K (e.g., $K = 10$) to the user

Take-away today

- **Ranking** search results: why it is important (as opposed to just presenting a set of unordered Boolean results)
- **Term frequency**: This is a key ingredient for ranking.
- **Tf-idf ranking**: best known traditional ranking scheme
- **Vector space model**: One of the most important formal models for information retrieval (along with Boolean and probabilistic models)

Resources

- Chapter 6 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - Vector space for dummies
 - Exploring the similarity space (Moffat and Zobel, 2005)
 - Okapi BM25 (a state-of-the-art weighting method, 11.4.3 of IIR)

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 7: Scores in a complete search system Handout version

Petr Sojka, Hinrich Schütze et al.

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Center for Information and Language Processing, University of Munich

2024-03-21

(compiled on 2024-02-20 00:50:46)

Overview

- 1 Why rank?
- 2 More on cosine
- 3 The complete search system
- 4 Implementation of ranking

Take-away today

- The importance of ranking: User studies at Google
- Length normalization: Pivot normalization
- The complete search system
- Implementation of ranking

Why is ranking so important?

- Last lecture: Problems with unranked retrieval
 - Users want to look at a few results – not thousands.
 - It's very hard to write queries that produce a few results.
 - Even for expert searchers
 - → Ranking is important because it effectively **reduces a large set of results to a very small one.**
- Next: More data on “users only look at a few results”
- Actually, in the vast majority of cases they only examine 1, 2, or 3 results.

Empirical investigation of the effect of ranking

- The following slides are from Dan Russell's JCDL talk
- Dan Russell was the "Über Tech Lead for Search Quality & User Happiness" at Google.
- How can we measure how important ranking is?
- Observe what searchers do when they are searching in a controlled setting
 - Videotape them
 - Ask them to "think aloud"
 - Interview them
 - Eye-track them
 - Time them
 - Record and count their clicks



So.. Did you notice the FTD official site?

To be honest, I didn't even look at that.

At first I saw "from \$20" and \$20 is what I was looking for.

To be honest, 1800-flowers is what I'm familiar with and why I went there next even though I kind of assumed they wouldn't have \$20 flowers

And you knew they were expensive?

I knew they were expensive but I thought "hey, maybe they've got some flowers for under \$20 here..."

But you didn't notice the FTD?

No I didn't, actually... that's really funny.

Interview video

Rapidly scanning the results

Note scan pattern:

- Page 3:
- Result 1
 - Result 2
 - Result 3
 - Result 4
 - Result 3
 - Result 2
 - Result 4
 - Result 5
 - Result 6 <click>

Q: Why do this?

A: What's learned later influences judgment of earlier content.

The screenshot shows a Google search for "children's unicycle". The search results are listed under the "Web" tab. A red arrow starts at the search bar, points to the first result, then moves down to the second, then to the third, then to the fourth, then to the fifth, then to the sixth, and finally to the seventh result. The results are:

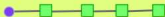
- 1 **Unicycle UK.com - F.A.Q. - What size?**
12" wheel unicycle: this is a small children's unicycle size. It's good for children who are too small to ride a 16" unicycle, but it needs smooth ground ...
www.unicycle.uk.com/FAQ.asp?Category=53 - 23k - Cached - Similar pages
- 2 **Selecting a unicycle Unicycle.com NZ : buy a unicycle or learn ...**
16" wheel unicycle: this is a children's unicycle, the small wheel makes it only suitable for smooth areas. Best used indoors or on smooth ground. ...
www.unicycle.co.nz/View.php?action=Page&Name=Selectingaunicycle - 22k - Cached - Similar pages
- 3 **100 Miles for Kids - The Goal**
The Afghan Mobile Mini Circus - Children is an established ... attempt to break the GUINNESS WORLD RECORD for the ONE HOUR UNICYCLE DISTANCE RECORD. ...
www.unicycle4kids.org/ - 9k - Cached - Similar pages
- 4 **Unicycles page at Juggling World**
This is a children's unicycle, the small wheel makes it only suitable for very smooth areas. Best used indoors or on smooth ground, not so good outdoors ...
www.jugglingworld.biz/shop/products_unicycles.html - 100k - Cached - Similar pages
- 5 **Buy a Unicycle Unicycle.com AU : buy a unicycle or learn unicycling**
Check out a Unicycle Learners Pack for an easy and economical way to take your first steps into the One Wheeled World ... Suitable as a Children's Unicycle ...
www.unicycle.au.com/View.php?action=Page&Name=Unicycles - 10k - Cached - Similar pages
- 6 **Article - News - A unicycle ride for children**
Adam Brody, 21, of San Juan Capistrano, led a charity event Saturday that benefits the Orangewood Children's Foundation. The Unicycle Club of Southern ...
www.ocregister.com/ocregister/news/homepage/article_1293785.php - 31k - Cached - Similar pages

Kinds of behaviors we see in the data

Short / Nav



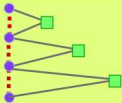
Topic exploration



Topic switch



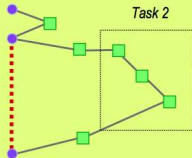
Methodical results exploration



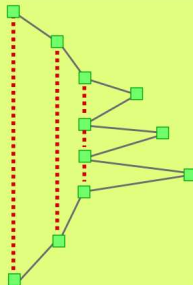
Query reform



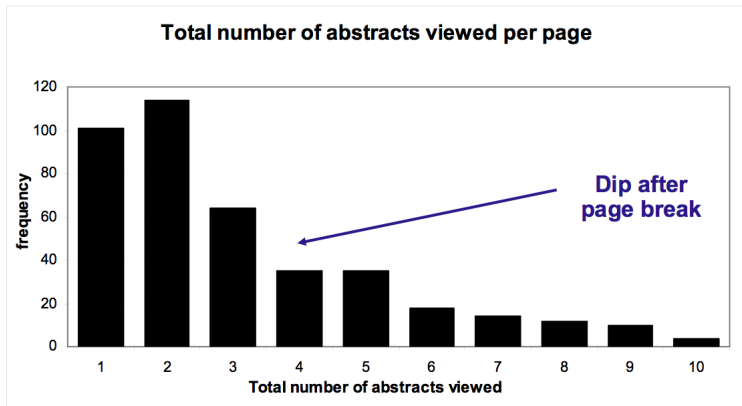
Multitasking



Stacking behavior

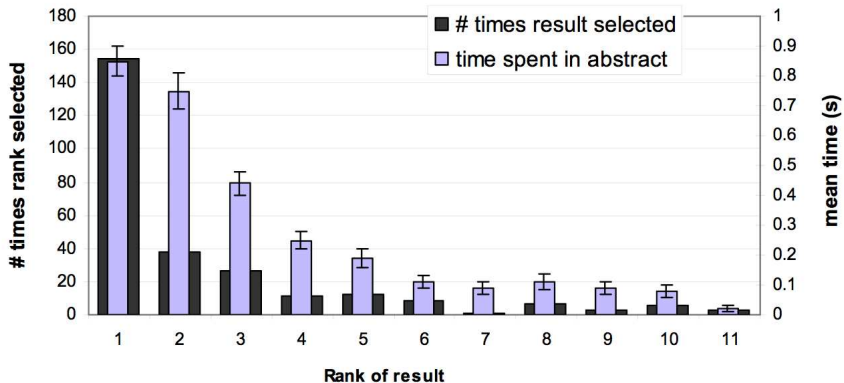


How many links do users view?



Mean: 3.07 Median/Mode: 2.00

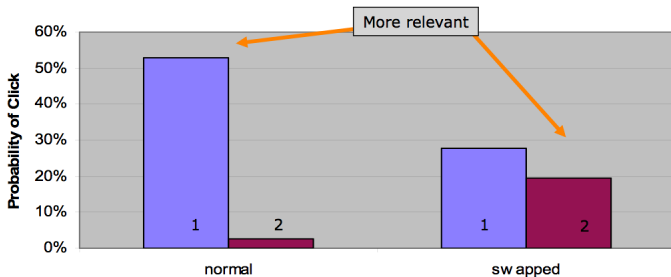
Looking vs. Clicking



- Users view results one and two more often / thoroughly
- Users click most frequently on result one

Presentation bias – reversed results

- Order of presentation influences where users look **AND** where they click



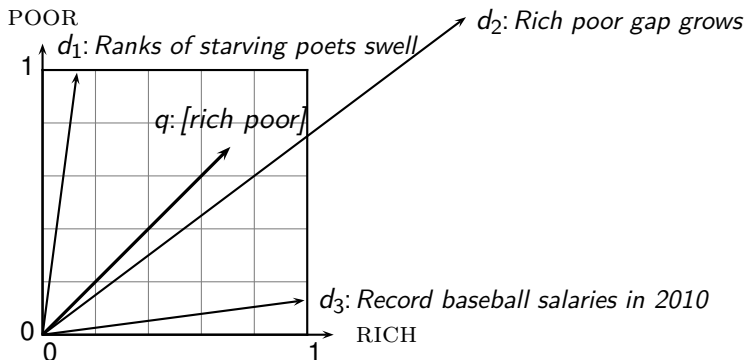
Importance of ranking: Summary

- **Viewing abstracts:** Users are a lot more likely to read the abstracts of the top-ranked pages (1, 2, 3, 4) than the abstracts of the lower ranked pages (7, 8, 9, 10).
- **Clicking:** Distribution is even more skewed for clicking
- In 1 out of 2 cases, users click on the top-ranked page.
- Even if the top-ranked page is not relevant, 30% of users will click on it.
- → Getting the ranking right is very important.
- → Getting the top-ranked page right is most important.

Exercise

- Ranking is also one of the high barriers to entry for competitors to established players in the search engine market.
- Why?

Why distance is a bad idea



The Euclidean distance of \vec{q} and \vec{d}_2 is large although the distribution of terms in the query q and the distribution of terms in the document d_2 are very similar.

That's why we do length normalization or, equivalently, use cosine to compute query-document matching scores.

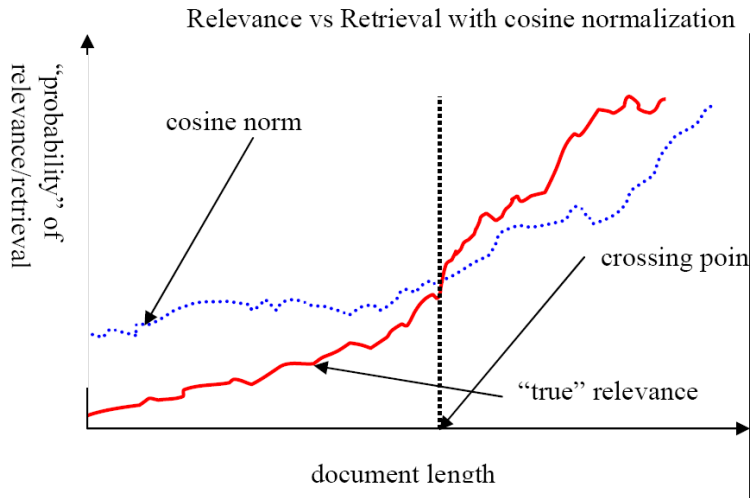
Exercise: A problem for cosine normalization

- Query q : “anti-doping rules Beijing 2008 olympics”
- Compare three documents
 - d_1 : a short document on anti-doping rules at 2008 Olympics
 - d_2 : a long document that consists of a copy of d_1 and 5 other news stories, all on topics different from Olympics/anti-doping
 - d_3 : a short document on anti-doping rules at the 2004 Athens Olympics
- What ranking do we expect in the vector space model?
- What can we do about this?

Pivot normalization

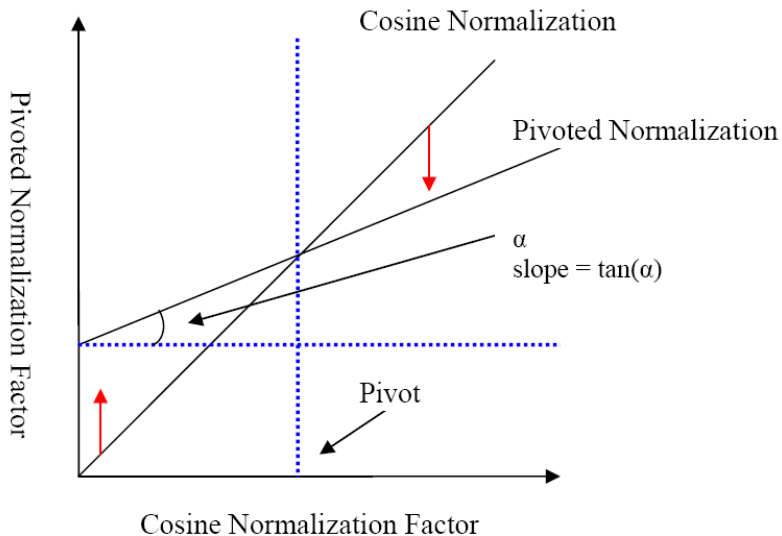
- Cosine normalization produces weights that are **too large for short documents** and **too small for long documents** (on average).
- Adjust cosine normalization by linear adjustment: “turning” the average normalization on the **pivot**
- Effect: Similarities of short documents with query **decrease**; similarities of long documents with query **increase**.
- This removes the unfair advantage that short documents have.

Predicted and true probability of relevance



source:
Lillian Lee

Pivot normalization



source:

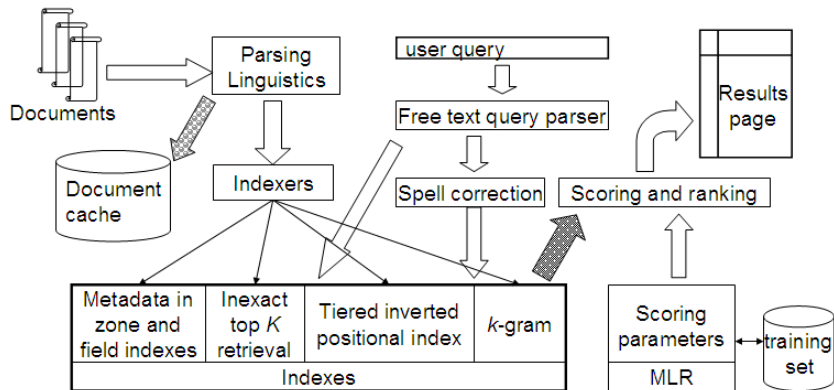
Lillian Lee

Pivoted normalization: Amit Singhal's experiments

| Cosine | Pivoted Cosine Normalization | | | | |
|-------------|------------------------------|--------|--------|---------------|--------|
| | Slope | | | | |
| | 0.60 | 0.65 | 0.70 | 0.75 | 0.80 |
| 6,526 | 6,342 | 6,458 | 6,574 | 6,629 | 6,671 |
| 0.2840 | 0.3024 | 0.3097 | 0.3144 | 0.3171 | 0.3162 |
| Improvement | + 6.5% | + 9.0% | +10.7% | +11.7% | +11.3% |

(relevant documents retrieved and (change in) average precision)

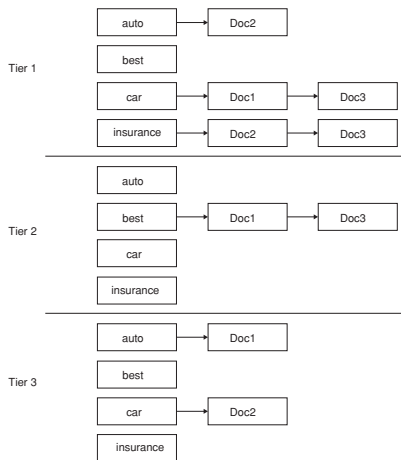
Complete search system



Tiered indexes

- Basic idea:
 - Create several tiers of indexes, corresponding to importance of indexing terms
 - During query processing, start with highest-tier index
 - If highest-tier index returns at least k (e.g., $k = 100$) results: stop and return results to user
 - If we've only found $< k$ hits: repeat for next index in tier cascade
- Example: two-tier system
 - Tier 1: Index of all titles
 - Tier 2: Index of the rest of documents
 - Pages containing the search words in the title are better hits than pages containing the search words in the body of the text.

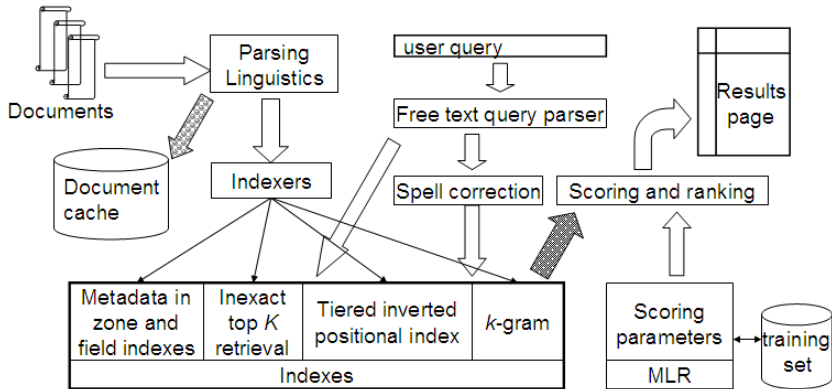
Tiered index



Tiered indexes

- The use of tiered indexes is believed to be one of the reasons that Google search quality was significantly higher initially (2000/01) than that of competitors.
- (along with PageRank, use of anchor text and proximity constraints)

Complete search system



Components we have introduced thus far

- Document preprocessing (linguistic and otherwise)
- Positional indexes
- Tiered indexes
- Spelling correction
- k-gram indexes for wildcard queries and spelling correction
- Query processing
- Document scoring

Components we haven't covered yet

- Document cache: we need this for generating snippets (= dynamic summaries)
- Zone indexes: They separate the indexes for different zones: the body of the document, all highlighted text in the document, anchor text, text in metadata fields,...
- Machine-learned ranking functions
- Proximity ranking (e.g., rank documents in which the query terms occur in the same local window higher than documents in which the query terms occur far from each other)
- Query parser

Components we haven't covered yet: Query parser

- IR systems often guess what the user intended.
- The two-term query *London tower* (without quotes) may be interpreted as the phrase query “*London tower*”.
- The query *100 Madison Avenue, New York* may be interpreted as a request for a map.
- How do we “parse” the query and translate it into a formal specification containing phrase operators, proximity operators, indexes to search, etc.?

Vector space retrieval: Interactions

- How do we combine phrase retrieval with vector space retrieval?
- We do not want to compute document frequency / idf for every possible phrase. Why?
- How do we combine Boolean retrieval with vector space retrieval?
- For example: “+”-constraints and “-”-constraints
- Postfiltering is simple, but can be very inefficient – no easy answer.
- How do we combine wild cards with vector space retrieval?
- Again, no easy answer.

Exercise

- Design criteria for tiered system
 - Each tier should be an order of magnitude smaller than the next tier.
 - The top 100 hits for most queries should be in tier 1, the top 100 hits for most of the remaining queries in tier 2, etc.
 - We need a simple test for “can I stop at this tier or do I have to go to the next one?”
 - There is no advantage to tiering if we have to hit most tiers for most queries anyway.
- Consider a two-tier system where the first tier indexes titles and the second tier everything.
- Question: Can you think of a better way of setting up a multitier system? Which “zones” of a document should be indexed in the different tiers (title, body of document, others?)? What criterion do you want to use for including a document in tier 1?

Now we also need term frequencies in the index

| | | | | | | |
|--------|---|-----|-----|------|------|-----|
| BRUTUS | → | 1,2 | 7,3 | 83,1 | 87,2 | ... |
|--------|---|-----|-----|------|------|-----|

| | | | | | | |
|--------|---|-----|-----|------|------|-----|
| CAESAR | → | 1,1 | 5,1 | 13,1 | 17,1 | ... |
|--------|---|-----|-----|------|------|-----|

| | | | | | |
|-----------|---|-----|-----|------|------|
| CALPURNIA | → | 7,1 | 8,2 | 40,1 | 97,3 |
|-----------|---|-----|-----|------|------|

term frequencies

We also need positions. Not shown here.

Term frequencies in the inverted index

- Thus: In each posting, store $tf_{t,d}$ in addition to docID d .
- As an integer frequency, not as a (log-)weighted real number
...
- ... because real numbers are difficult to compress.
- Overall, additional space requirements are small: a byte per posting or less

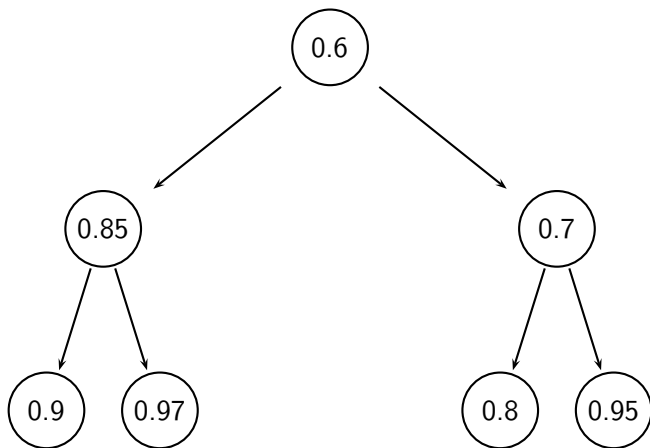
How do we compute the top k in ranking?

- We usually do not need a complete ranking.
- We just need the top k for a small k (e.g., $k = 100$).
- If we don't need a complete ranking, is there an efficient way of computing just the top k ?
- Naïve:
 - Compute scores for all N documents
 - Sort
 - Return the top k
- Not very efficient
- Alternative: min heap

Use min heap for selecting top k out of N

- A binary min heap is a binary tree in which each node's value is less than the values of its children.
- Takes $O(N \log k)$ operations to construct (where N is the number of documents) ...
- ... then read off k winners in $O(k \log k)$ steps

Binary min heap



Selecting top k scoring documents in $O(N \log k)$

- Goal: Keep the top k documents seen so far
- Use a binary min heap
- To process a new document d' with score s' :
 - Get current minimum h_m of heap ($O(1)$)
 - If $s' \leq h_m$ skip to next document
 - If $s' > h_m$ heap-delete-root ($O(\log k)$)
 - Heap-add d'/s' ($O(\log k)$)

Even more efficient computation of top k ?

- Ranking has time complexity $O(N)$ where N is the number of documents.
- Optimizations reduce the constant factor, but they are still $O(N)$, $N > 10^{10}$
- Are there sublinear algorithms?
- What we're doing in effect: solving the k -nearest neighbor (kNN) problem for the query vector (= query point).
- There are no general solutions to this problem that are sublinear.

More efficient computation of top k : Heuristics

- Idea 1: Reorder postings lists
 - Instead of ordering according to docID ...
 - ...order according to some measure of “expected relevance”.
- Idea 2: Heuristics to prune the search space
 - Not guaranteed to be correct ...
 - ...but fails rarely.
 - In practice, close to constant time.
 - For this, we'll need the concepts of document-at-a-time processing and term-at-a-time processing.

Non-docID ordering of postings lists

- So far: postings lists have been ordered according to docID.
- Alternative: a query-independent measure of “goodness” (credibility) of a page
- Example: [PageRank](#) $g(d)$ of page d , a measure of how many “good” pages hyperlink to d (chapter 21)
- Order documents in postings lists according to PageRank:
 $g(d_1) > g(d_2) > g(d_3) > \dots$
- Define composite score of a document:

$$\text{net-score}(q, d) = g(d) + \cos(q, d)$$

- This scheme supports early termination: We do not have to process postings lists in their entirety to find top k .

Non-docID ordering of postings lists (2)

- Order documents in postings lists according to PageRank:
 $g(d_1) > g(d_2) > g(d_3) > \dots$
- Define composite score of a document:

$$\text{net-score}(q, d) = g(d) + \cos(q, d)$$

- Suppose: (i) $g \rightarrow [0, 1]$; (ii) $g(d) < 0.1$ for the document d we're currently processing; (iii) smallest top k score we've found so far is 1.2
- Then all subsequent scores will be < 1.1 .
- So we've already found the top k and can stop processing the remainder of postings lists.
- Questions?

Document-at-a-time processing

- Both docID-ordering and PageRank-ordering impose a consistent ordering on documents in postings lists.
- Computing cosines in this scheme is [document-at-a-time](#).
- We complete computation of the query-document similarity score of document d_i before starting to compute the query-document similarity score of d_{i+1} .
- Alternative: term-at-a-time processing

Weight-sorted postings lists

- Idea: don't process postings that contribute little to final score
- Order documents in postings list according to **weight**
- Simplest case: normalized tf-idf weight (rarely done: hard to compress)
- Documents in the top k are likely to occur early in these ordered lists.
- → Early termination while processing postings lists is unlikely to change the top k .
- But:
 - We no longer have a consistent ordering of documents in postings lists.
 - We no longer can employ document-at-a-time processing.

Term-at-a-time processing

- Simplest case: completely process the postings list of the first query term
- Create an accumulator for each docID you encounter
- Then completely process the postings list of the second query term
- . . . and so forth

Term-at-a-time processing

COSINESCORE(q)

```
1  float Scores[N] = 0
2  float Length[N]
3  for each query term  $t$ 
4  do calculate  $w_{t,q}$  and fetch postings list for  $t$ 
5      for each pair( $d, tf_{t,d}$ ) in postings list
6      do  $Scores[d] + = w_{t,d} \times w_{t,q}$ 
7  Read the array  $Length$ 
8  for each  $d$ 
9  do  $Scores[d] = Scores[d] / Length[d]$ 
10 return Top  $k$  components of  $Scores[]$ 
```

The elements of the array “Scores” are called [accumulators](#).

Computing cosine scores

- Use inverted index
- At query time use an array of accumulators A to store sum (= the cosine score)



$$A_j = \sum_k w_{qk} \cdot w_{d_jk}$$

(for document d_j)

- “Accumulate” scores as postings lists are being processed.

Accumulators

- For the web (20 billion documents), an array of accumulators A in memory is infeasible.
- Thus: Only create accumulators for docs occurring in postings lists
- This is equivalent to: Do not create accumulators for docs with zero scores (i.e., docs that do not contain any of the query terms)

Accumulators: Example

BRUTUS →

| | | | | |
|-----|-----|------|------|-----|
| 1,2 | 7,3 | 83,1 | 87,2 | ... |
|-----|-----|------|------|-----|

CAESAR →

| | | | | |
|-----|-----|------|------|-----|
| 1,1 | 5,1 | 13,1 | 17,1 | ... |
|-----|-----|------|------|-----|

CALPURNIA →

| | | | |
|-----|-----|------|------|
| 7,1 | 8,2 | 40,1 | 97,3 |
|-----|-----|------|------|

- For query: [Brutus Caesar]:
- Only need accumulators for 1, 5, 7, 13, 17, 83, 87
- Don't need accumulators for 3, 8, etc.

Enforcing conjunctive search

- We can enforce conjunctive search (à la Google): only consider documents (and create accumulators) if all terms occur.
- Example: just one accumulator for [Brutus Caesar] in the example above . . .
- . . . because only d_1 contains both words.

Implementation of ranking: Summary

- Ranking is **very expensive** in applications where we have to compute similarity scores for all documents in the collection.
- In most applications, the vast majority of documents have **similarity score 0** for a given query → lots of potential for speeding things up.
- However, there is **no fast nearest neighbor algorithm** that is guaranteed to be correct even in this scenario.
- In practice: **use heuristics** to prune search space – usually works very well.

Take-away today

- The importance of ranking: User studies at Google
- Length normalization: Pivot normalization
- The complete search system
- Implementation of ranking

Resources

- Chapter 7 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - How Google tweaks its ranking function?
 - Interview with Google search guru Udi Manber
 - Amit Singhal on Google ranking
 - SEO perspective: ranking factors
 - Yahoo Search BOSS: Opens up the search engine to developers. For example, you can rerank search results.
 - How Google uses eye tracking for improving search.

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 8: Evaluation & Result Summaries Handout version

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2024-03-21

(compiled on 2024-06-10 08:50)

Overview

- 1 Introduction
- 2 Unranked evaluation
- 3 Ranked evaluation
- 4 Benchmarks
- 5 Result summaries

Take-away today

- Introduction to evaluation: Measures of an IR system
- Evaluation of unranked and ranked retrieval
- Evaluation benchmarks
- Result summaries

Evaluation

How well does an IR system work?

Přibližný počet výsledků: 108 000 000 (0,00002 s)

Při poskytování služeb nám pomáhají soubory cookie. Používáním našich služeb vyjadřujete souhlas s naším používáním souborů cookie.

OK

[Další informace](#)

Rihanna – Wikipedie

cs.wikipedia.org/wiki/Rihanna ▾

Rihanna /ˈriːɑːnɑː/, narozena jako Robyn **Rihanna** Fenty (* 20. února 1988, Saint Michael, Barbados) je barbadoská zpěvačka, která je ve své tvorbě ...

[Biografie](#) - [Hudební kariéra](#) - [Turné](#) - [Diskografie](#)

Rihanna - Osobnosti.cz

www.osobnosti.cz/rihanna.php ▾

Rihanna, narozena jako Robyn **Rihanna** Fenty je barbadoská zpěvačka, která je ve své tvorbě ovlivněna styly R&B, reggae, dancehall a dance. Nahrává u ...

[Životopis](#) - [Tapety \(185\)](#) - [LOUD Tour 2011](#) - [All Of The Lights](#)

Rihanna Fenty - Super.cz

www.super.cz/celebrity/rihanna-fenty/ ▾

Počet položek: 5+ - Bulvární status: Známa provokatérka se už dávno ...

Největší sígr Hollywoodu už bručí v base: Porušil podmínku, kterou dostal za ...

Rihanna má v Česku dvojnici! Začínající zpěvačka jako by z oka vypadla ...

Rihanna (rihanna) on Twitter

<https://twitter.com/rihanna> ▾ [Přeložit tuto stránku](#)

The latest from **Rihanna (@rihanna)** · WHAT NOW on VEVO! CLICK here to WATCH ...



Measures for a search engine

- How fast does it index
 - e.g., number of bytes per hour
- How fast does it search
 - e.g., latency as a function of queries per second
- What is the cost per query?
 - in dollars

Measures for a search engine

- All of the preceding criteria are **measurable**: we can quantify speed / size / money
- However, the key measure for a search engine is **user happiness**.
- What is user happiness?
- Factors include:
 - Speed of response
 - Size of index
 - Uncluttered UI
 - Most important: **relevance**
 - (actually, maybe even more important: it's free)
- Note that none of these is sufficient: blindingly fast, but useless answers won't make a user happy.
- **How can we quantify user happiness?**

Who is the user?

- Who is the user we are trying to make happy?
- Web search engine: searcher. Success: Searcher finds what she was looking for. Measure: rate of return to this search engine
- Web search engine: advertiser. Success: Searcher clicks on ad. Measure: clickthrough rate
- E-commerce: buyer. Success: Buyer buys something. Measures: time to purchase, fraction of “conversions” of searchers to buyers
- E-commerce: seller. Success: Seller sells something. Measure: profit per item sold
- Enterprise: CEO. Success: Employees are more productive (because of effective search). Measure: profit of the company

Most common definition of user happiness: Relevance

- User happiness is equated with the relevance of search results to the query.
- But how do you measure relevance?
- Standard methodology in information retrieval consists of three elements.
 - A benchmark document collection
 - A benchmark suite of queries
 - An assessment of the relevance of each query-document pair

Relevance: query vs. information need

- Relevance to **what?**
- First take: relevance to the query
- “Relevance to the query” is very problematic.
- **Information need i** : “I am looking for information on whether drinking red wine is more effective at reducing your risk of heart attacks than white wine.”
- This is an information need, not a query.
- **Query q** : [red wine white wine heart attack]
- Consider document d' : *At the heart of his speech was an attack on the wine industry lobby for downplaying the role of red and white wine in drunk driving.*
- d' is an excellent match for query q . . .
- d' is **not** relevant to the information need i .

Relevance: query vs. information need

- User happiness can only be measured by relevance to an information need, not by relevance to queries.
- Our terminology is sloppy in these slides and in IIR: we talk about query-document relevance judgments even though we mean information-need-document relevance judgments.

Precision and recall

- Precision (P) is the fraction of retrieved documents that are relevant

$$\text{Precision} = \frac{\#(\text{relevant items retrieved})}{\#(\text{retrieved items})} = P(\text{relevant}|\text{retrieved})$$

- Recall (R) is the fraction of relevant documents that are retrieved

$$\text{Recall} = \frac{\#(\text{relevant items retrieved})}{\#(\text{relevant items})} = P(\text{retrieved}|\text{relevant})$$

Precision and recall

| | Relevant | Nonrelevant |
|---------------|----------------------|----------------------|
| Retrieved | true positives (TP) | false positives (FP) |
| Not retrieved | false negatives (FN) | true negatives (TN) |

$$P = TP / (TP + FP)$$

$$R = TP / (TP + FN)$$

Precision/recall tradeoff

- You can increase recall by returning more docs.
- Recall is a non-decreasing function of the number of docs retrieved.
- A system that returns all docs has 100% recall!
- The converse is also true (usually): It's easy to get high precision for very low recall.
- Suppose the document with the largest score is relevant. How can we maximize precision?

A combined measure: F

- F allows us to trade off precision against recall.
-

$$F = \frac{1}{\alpha \frac{1}{P} + (1 - \alpha) \frac{1}{R}} = \frac{(\beta^2 + 1)PR}{\beta^2 P + R} \quad \text{where} \quad \beta^2 = \frac{1 - \alpha}{\alpha}$$

- $\alpha \in [0, 1]$ and thus $\beta^2 \in [0, \infty]$
- Most frequently used: **balanced F** with $\beta = 1$ or $\alpha = 0.5$
 - This is the **harmonic mean** of P and R : $\frac{1}{F} = \frac{1}{2}(\frac{1}{P} + \frac{1}{R})$
- What value range of β weights recall higher than precision?

Example for precision, recall, F1

| | relevant | not relevant | |
|---------------|----------|--------------|-----------|
| retrieved | 20 | 40 | 60 |
| not retrieved | 60 | 1,000,000 | 1,000,060 |
| | 80 | 1,000,040 | 1,000,120 |

- $P = 20 / (20 + 40) = 1/3$
- $R = 20 / (20 + 60) = 1/4$
- $F_1 = 2 \frac{1}{\frac{1}{3} + \frac{1}{4}} = 2/7$

Accuracy

- Why do we use complex measures like precision, recall, and F ?
- Why not something simple like accuracy?
- Accuracy is the fraction of decisions (relevant/nonrelevant) that are correct.
- In terms of the contingency table above,
accuracy = $(TP + TN)/(TP + FP + FN + TN)$.
- Why is accuracy not a useful measure for web information retrieval?

Exercise

- Compute precision, recall and F_1 for this result set:

| | relevant | not relevant |
|---------------|----------|---------------|
| retrieved | 18 | 2 |
| not retrieved | 82 | 1,000,000,000 |

- The snoogle search engine below always returns 0 results (“0 matching results found”), regardless of the query. Why does snoogle demonstrate that accuracy is not a useful measure in IR?

The logo for snoogle.com, featuring the word 'snoogle.com' in a stylized, multi-colored font (blue, orange, red) on a light green background.

Search for:

0 matching results found.

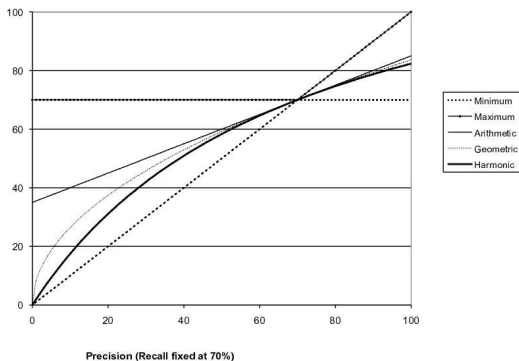
Why accuracy is a useless measure in IR

- Simple trick to maximize accuracy in IR: always say no and return nothing
- You then get 99.99% accuracy on most queries.
- Searchers on the web (and in IR in general) **want to find something** and have a certain tolerance for junk.
- It's better to return some bad hits as long as you return something.
- → We use precision, recall, and F for evaluation, not accuracy.

F: Why harmonic mean?

- Why don't we use a different mean of P and R as a measure?
 - e.g., the arithmetic mean
- The simple (arithmetic) mean is 50% for “return-everything” search engine, which is too high.
- Desideratum: Punish really bad performance on either precision or recall.
- Taking the minimum achieves this.
- But minimum is not smooth and hard to weight.
- F (harmonic mean) is a kind of smooth minimum.

F_1 and other averages



- We can view the harmonic mean as a kind of soft minimum

Difficulties in using precision, recall and F

- We need relevance judgments for information-need-document pairs – but they are expensive to produce.
- For alternatives to using precision/recall and having to produce relevance judgments – see end of this lecture.

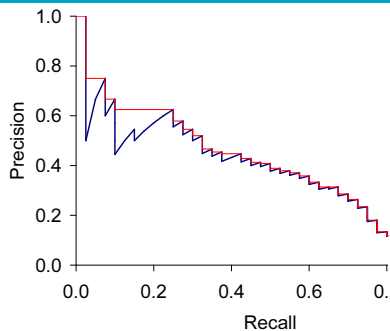
Mean Average Precision

- $\text{MAP}(Q) = \frac{1}{|Q|} \sum_{j=1}^{|Q|} \frac{1}{m_j} \sum_{k=1}^{m_j} \text{Precision}(R_{jk})$
- For one query it is the area under the uninterpolated precision-recall curve,
- and so the MAP is roughly the *average* area under the precision-recall curve for a set of queries.

Precision-recall curve

- Precision/recall/F are measures for **unranked sets**.
- We can easily turn set measures into measures of **ranked lists**.
- Just compute the set measure for each “prefix”: the top 1 (P@1), top 2, top 3, top 4, etc., results
- Doing this for precision and recall gives you a **precision-recall curve**.

A precision-recall curve



- Each point corresponds to a result for the top k ranked hits ($k = 1, 2, 3, 4, \dots$).
- **Interpolation (in red): Take maximum of all future points**
- Rationale for interpolation: The user is willing to look at more stuff if both precision and recall get better.
- **Questions?**

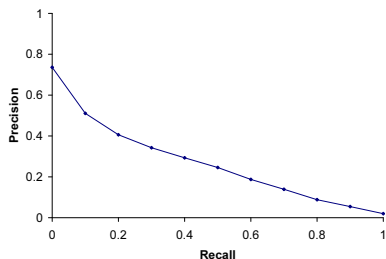
11-point interpolated average precision

| Recall | Interpolated Precision |
|--------|---------------------------|
| 0.0 | 1.00 |
| 0.1 | 0.67 |
| 0.2 | 0.63 |
| 0.3 | 0.55 |
| 0.4 | 0.45 |
| 0.5 | 0.41 |
| 0.6 | 0.36 |
| 0.7 | 0.29 |
| 0.8 | 0.13 |
| 0.9 | 0.10 |
| 1.0 | 0.08 |

11-point average: \approx
0.425

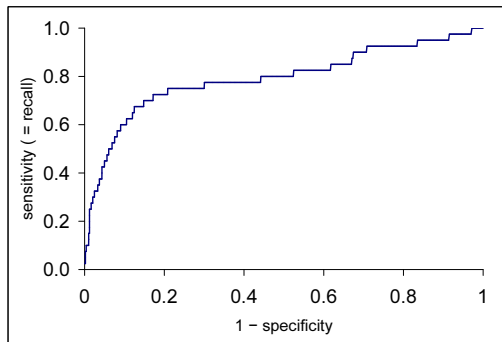
How can precision
at 0.0 be > 0 ?

Averaged 11-point precision/recall graph



- Compute interpolated precision at recall levels 0.0, 0.1, 0.2, ...
- Do this for each of the queries in the evaluation benchmark
- Average over queries
- This measure measures performance **at all recall levels**.
- The curve is typical of performance levels at TREC.
- Note that performance is not very good!

ROC curve



- Similar to precision-recall graph
- But we are only interested in the small area in the lower left corner.
- Precision-recall graph “blows up” this area.

Variance of measures like precision/recall

- For a test collection, it is usual that a system does badly on some information needs (e.g., $P = 0.2$ at $R = 0.1$) and really well on others (e.g., $P = 0.95$ at $R = 0.1$).
- Indeed, it is usually the case that the **variance of the same system across queries** is much **greater than the variance of different systems on the same query**.
- That is, there are easy information needs and hard ones.

What we need for a benchmark

- A collection of documents
 - Documents must be representative of the documents we expect to see in reality.
- A collection of information needs
 - ... which we will often incorrectly refer to as queries
 - Information needs must be representative of the information needs we expect to see in reality.
- Human relevance assessments
 - We need to hire/pay “judges” or assessors to do this.
 - Expensive, time-consuming
 - Judges must be representative of the users we expect to see in reality.

First standard relevance benchmark: Cranfield

- Pioneering: first testbed allowing precise quantitative measures of information retrieval effectiveness
- Late 1950s, UK
- 1398 abstracts of aerodynamics journal articles, a set of 225 queries, exhaustive relevance judgments of all query-document-pairs
- Too small, too untypical for serious IR evaluation today

Second-generation relevance benchmark: TREC

- TREC = Text Retrieval Conference (TREC)
- Organized by the U.S. National Institute of Standards and Technology (NIST)
- TREC is actually a set of several different relevance benchmarks.
- Best known: TREC Ad Hoc, used for first 8 TREC evaluations between 1992 and 1999
- 1.89 million documents, mainly newswire articles, 450 information needs
- No exhaustive relevance judgments – too expensive
- Rather, NIST assessors' relevance judgments are available only for the documents that were among the top k returned for some system which was entered in the TREC evaluation for which the information need was developed.

Standard relevance benchmarks: Others

- GOV2
 - Another TREC/NIST collection
 - 25 million web pages
 - Used to be largest collection that is easily available
 - But still 3 orders of magnitude smaller than what Google/Yahoo/MSN index
- NTCIR: East Asian language and cross-language information retrieval
- CLEF: Cross Language Evaluation Forum: This evaluation series has concentrated on European languages and cross-language information retrieval.
- Many others

Example of more recent benchmark: ClueWeb datasets

Clueweb09:

- 1 billion web pages, 25 terabytes (compressed: 5 terabyte) collected during January/February 2009
- crawl of pages in 10 languages
- Unique URLs: 4,780,950,903 (325 GB uncompressed, 105 GB compressed)
- Total Outlinks: 7,944,351,835 (71 GB uncompressed, 24 GB compressed)

Clueweb12:

- 733,019,372 docs, 27.3 TB (5.54 TB compressed)

Indexed in Sketch Engine, cf. LREC 2012 paper.

Validity of relevance assessments



- Relevance assessments are only usable if they are **consistent**.
- If they are not consistent, then there is no “truth” and experiments are not repeatable.
- How can we measure this consistency or agreement among judges?
- → Kappa measure

Kappa measure

- Kappa is measure of how much judges agree or disagree.
- Designed for categorical judgments
- Corrects for chance agreement
- $P(A)$ = proportion of time judges agree
- $P(E)$ = what agreement would we get by chance

-

$$\kappa = \frac{P(A) - P(E)}{1 - P(E)}$$

- $\kappa = ?$ for (i) chance agreement (ii) total agreement

Kappa measure (2)

- Values of κ in the interval $[2/3, 1.0]$ are seen as acceptable.
- With smaller values: need to redesign relevance assessment methodology used, etc.

Calculating the kappa statistic

| | | Judge 2 Relevance | | |
|----------------------|-------|-------------------|----|-------|
| | | Yes | No | Total |
| Judge 1 Relevance | Yes | 300 | 20 | 320 |
| | No | 10 | 70 | 80 |
| | Total | 310 | 90 | 400 |

Observed proportion of the times the judges agreed

$$P(A) = (300 + 70)/400 = 370/400 = 0.925$$

Pooled marginals

$$P(\text{nonrelevant}) = (80 + 90)/(400 + 400) = 170/800 = 0.2125$$

$$P(\text{relevant}) = (320 + 310)/(400 + 400) = 630/800 = 0.7878$$

Probability that the two judges agreed by chance $P(E) =$

$$P(\text{nonrelevant})^2 + P(\text{relevant})^2 = 0.2125^2 + 0.7878^2 = 0.665$$

Kappa statistic $\kappa = (P(A) - P(E))/(1 - P(E)) =$

$$(0.925 - 0.665)/(1 - 0.665) = 0.776 \text{ (still in acceptable range)}$$

Interjudge agreement at TREC

| information need | number of docs judged | disagreements |
|---------------------|--------------------------|---------------|
| 51 | 211 | 6 |
| 62 | 400 | 157 |
| 67 | 400 | 68 |
| 95 | 400 | 110 |
| 127 | 400 | 106 |

Impact of interjudge disagreement

- Judges disagree a lot. Does that mean that the results of information retrieval experiments are meaningless?
- No.
- Large impact on absolute performance numbers
- Virtually no impact on ranking of systems
- Supposes we want to know if algorithm A is better than algorithm B.
- An information retrieval experiment will give us a reliable answer to this question. . .
- . . . even if there is a lot of disagreement between judges.

Evaluation at large search engines

- Recall is difficult to measure on the web
- Search engines often use precision at top k , e.g., $k = 10 \dots$
- \dots or use measures that reward you more for getting rank 1 right than for getting rank 10 right.
- Search engines also use non-relevance-based measures.
 - Example 1: clickthrough on first result
 - Not very reliable if you look at a single clickthrough (you may realize after clicking that the summary was misleading and the document is nonrelevant) \dots
 - \dots but pretty reliable in the aggregate.
 - Example 2: Ongoing studies of user behavior in the lab – recall last lecture
 - Example 3: A/B testing

A/B testing

- Purpose: Test a single innovation
- Prerequisite: You have a large search engine up and running.
- Have most users use old system
- Divert a small proportion of traffic (e.g., 1%) to the new system that includes the innovation
- Evaluate with an “automatic” measure like clickthrough on first result
- Now we can directly see if the innovation does improve user happiness.
- Probably the evaluation methodology that large search engines trust most
- Variant: Give users the option to switch to new algorithm/interface

Critique of pure relevance

- We've defined relevance for an isolated query-document pair.
- Alternative definition: marginal relevance
- The **marginal relevance** of a document at position k in the result list is the additional information it contributes over and above the information that was contained in documents $d_1 \dots d_{k-1}$.
- Exercise
 - Why is marginal relevance a more realistic measure of user happiness?
 - Give an example where a non-marginal measure like precision or recall is a misleading measure of user happiness, but marginal relevance is a good measure.
 - In a practical application, what is the difficulty of using marginal measures instead of non-marginal measures?

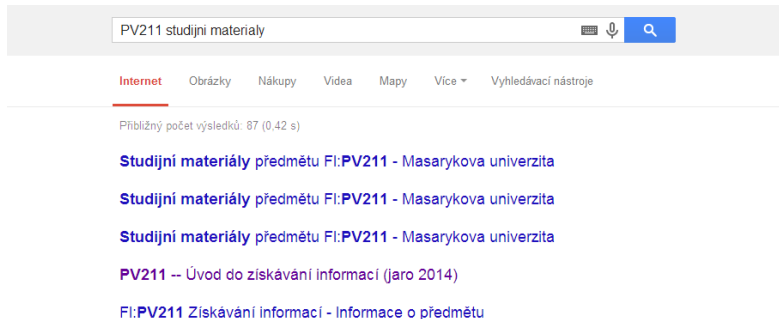
Yet another metrics to be used in IR evaluation

There are many other evaluation measures in IR.

- DCG, nDCG: Discounted cumulative gain, normalized Discounted cumulative gain
- ROC: Receiver operating characteristic or
- Bref: Bpref computes a preference relation of whether judged relevant documents are retrieved ahead of judged irrelevant documents. Thus, it is based on the relative ranks of judged documents only.

Most metrics are implemented and documented in our glorious pv211-utils and their use is supported by tutorials.



How do we present results to the user?



The screenshot shows a search engine interface. At the top, a search bar contains the text "PV211 studijni materialy". To the right of the search bar are icons for keyboard search, voice search, and a magnifying glass. Below the search bar, there are navigation tabs: "Internet" (highlighted with a red underline), "Obrázky", "Nákupy", "Videa", "Mapy", "Více", and "Vyhledávací nástroje". Below the tabs, the text "Přibližný počet výsledků: 87 (0,42 s)" is displayed. The search results are listed below, each with a blue link:

- [Studijní materiály předmětu FI:PV211 - Masarykova univerzita](#)
- [Studijní materiály předmětu FI:PV211 - Masarykova univerzita](#)
- [Studijní materiály předmětu FI:PV211 - Masarykova univerzita](#)
- [PV211 -- Úvod do získávání informací \(jaro 2014\)](#)
- [FI:PV211 Získávání informací - Informace o předmětu](#)

How do we present results to the user?

Internet Obrázky Nákupy Vídea Mapy Více ▾ Vyhledávací nástroje

Přibližný počet výsledků: 87 (0,42 s)

Studijní materiály předmětu FI:PV211 - Masarykova univerzita
<https://is.muni.cz/el/1433/jaro2014/PV211/> ▾
Studijní materiály předmětu FI:PV211 /PV211/ Popis: FI:PV211 Úvod do získávání informací (Introduction to Information Retrieval), jaro 2014, 5. 6. 2013. Číst smí:.

Studijní materiály předmětu FI:PV211 - Masarykova univerzita
<https://is.muni.cz/el/1433/jaro2013/PV211/> ▾
Studijní materiály předmětu FI:PV211 /PV211/ Popis: FI:PV211 Introduction to Information Retrieval (Introduction to Information Retrieval), jaro 2013, 18. 1. 2014.

Studijní materiály předmětu FI:PV211 - Masarykova univerzita
<https://is.muni.cz/el/1433/jaro2009/PV211/> ▾
Studijní materiály předmětu FI:PV211 /PV211/ Popis: FI:PV211 Introduction to Information Retrieval (Introduction to Information Retrieval), jaro 2009, 30. 3. 2008.

PV211 -- Úvod do získávání informací (jaro 2014)
www.fi.muni.cz/~sojka/PV211/ ▾
Support of lecture PV211 given by Petr Sojka at FI MU, Brno, CZ. ... materiálů kurzu PV211. 27. 1.: Založený studijní materiály předmětu s trailerem kurzu. 26. 1.

How do we present results to the user?

- Most often: as a list – aka “10 blue links”
- How should each document in the list be described?
- This description is crucial.
- The user often can identify good hits (= relevant hits) based on the description.
- No need to actually view any document

Doc description in result list

- Most commonly: doc title, url, some metadata ...
- ... and a summary
- How do we “compute” the summary?

Summaries

- Two basic kinds: (i) static (ii) dynamic
- A **static summary** of a document is always the same, regardless of the query that was issued by the user.
- **Dynamic summaries** are **query-dependent**. They attempt to explain why the document was retrieved for the query at hand.

Static summaries

- In typical systems, the static summary is a subset of the document.
- Simplest heuristic: the first 50 or so words of the document
- More sophisticated: extract from each document a set of “key” sentences
 - Simple NLP heuristics to score each sentence
 - Summary is made up of top-scoring sentences.
 - Machine learning approach: see IIR 13
- Most sophisticated: complex NLP to synthesize/generate a summary
 - For most IR applications: not quite ready for prime time yet

Dynamic summaries

- Present one or more “windows” or **snippets** within the document that contain several of the query terms.
- Prefer snippets in which query terms occurred as a phrase
- Prefer snippets in which query terms occurred jointly in a small window
- The summary that is computed this way gives the entire content of the window – all terms, not just the query terms.

Google dynamic summaries for [vegetarian diet running]

[No Meat Athlete | Vegetarian Running and Fitness](#)

www.nomeatathlete.com/ ▼

Vegetarian Running and Fitness. ... (Oh, and did I mention Rich did it all on a plant-based **diet**?) In this episode of No Meat Athlete Radio, Doug and I had the ...
[Vegetarian Recipes for Athletes](#) - [Vegetarian Shirts](#) - [How to Run Long](#) - [About](#)

[Running on a vegetarian diet – Top tips | Freedom2Train Blog](#)

www.freedom2train.com/blog/?p=4 ▼

Nov 8, 2012 – In this article we look to tackle the issues faced by long distance runners on a **vegetarian diet**. By its very nature, a **vegetarian diet** can lead to ...

[HowStuffWorks "5 Nutrition Tips for Vegetarian Runners"](#)

www.howstuffworks.com/.../running/.../5-nutrition-tips-for-vegetarian-r... ▼

Even without meat, you can get enough fuel to keep on **running**. Stockbyte/Thinkstock
... Unfortunately, a **vegetarian diet** is not a panacea for runners. It could, for ...

[Nutrition Guide for Vegetarian and Vegan Runners - The Running Bug](#)

therunningbug.co.uk/.../nutrition-guide-for-vegetarian-and-vegan-runne... ▼

Feb 28, 2012 – The **Running Bug**'s guide to nutrition for vegetarian and vegan ...
different types of **vegetarian diet** ranging from lacto-ovo-vegetarians who eat ...

[Vegetarian Runner](#)

www.vegetarianrunner.com/ ▼

Vegetarian Runner - A resource center for vegetarianism and **running** and how to make sure you have proper nutrition as an athlete with a **vegetarian diet**.

- Good example that snippet selection is non-trivial.
- Criteria: occurrence of keywords, density of keywords, coherence of snippet, number of different snippets in summary, good cutting points, etc.

A dynamic summary

Query: [new guinea economic development]

Snippets (in bold) that were extracted from a document: ... ***In recent years, Papua New Guinea has faced severe economic difficulties and*** economic growth has slowed, partly as a result of weak governance and civil war, and partly as a result of external factors such as the Bougainville civil war which led to the closure in 1989 of the Panguna mine (at that time the most important foreign exchange earner and contributor to Government finances), the Asian financial crisis, a decline in the prices of gold and copper, and a fall in the production of oil. ***PNG's economic development record over the past few years is evidence that*** governance issues underly many of the country's problems. Good governance, which may be defined as the transparent and accountable management of human, natural, economic and financial resources for the purposes of equitable and sustainable development, flows from proper public sector management, efficient fiscal and accounting mechanisms, and a willingness to make service delivery a priority in practice. ...

Generating dynamic summaries

- Where do we get these other terms in the snippet from?
- We cannot construct a dynamic summary from the positional inverted index – at least not efficiently.
- We need to cache documents.
- The positional index tells us: query term occurs at position 4378 in the document.
- Byte offset or word offset?
- Note that the cached copy can be outdated
- Don't cache very long documents – just cache a short prefix

Dynamic summaries

- Real estate on the search result page is limited → snippets must be short . . .
- . . . but snippets must be long enough to be meaningful.
- Snippets should communicate whether and how the document answers the query.
- Ideally: linguistically well-formed snippets
- Ideally: the snippet should answer the query, so we don't have to look at the document.
- Dynamic summaries are a big part of user happiness because . . .
 - . . . we can quickly scan them to find the relevant document we then click on.
 - . . . in many cases, we don't have to click at all and save time.

Resources

- Chapter 8 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - The TREC home page – TREC had a huge impact on information retrieval evaluation.
 - Originator of F -measure: Keith van Rijsbergen
 - More on A/B testing
 - Too much A/B testing at Google?
 - Tombros & Sanderson 1998: one of the first papers on dynamic summaries
 - Google VP of Engineering on search quality evaluation at Google
 - ClueWeb12 and other datasets available in Sketch Engine

CQL and Texts From Web

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March 26, 2024

Terms in Rocket Science

A friend of yours is applying for a job in NASA. He is going on an interview tomorrow and does not know much about **rocket science**. He needs help with terminology.

1. What terms are used in **rocket science**?
2. How do you find these terms?

Gathering Documents from the Internet¹

1. Gather webpages.
2. (optional) Explore links. (Spiderlink)
3. Remove meaningless sentences. (JustText)
4. Deduplicate sentences. (Onion)
5. Tag and lemmatize gathered texts. (Unitok)
6. Create a corpus from gathered texts. ((No)Sketch Engine)

¹<https://corpus.tools>

(No)Sketch Engine

- Doing all gathering from scratch can be time-consuming.
- (No)Sketch Engine offers to create your own corpus from the web with just a few keywords.
- <https://app.sketchengine.eu>

Queries

Simple

- Word frequency, lemma frequency.
- Keyword in context. (KWIC)

Advanced

- Corpus Query Language (CQL)

Corpus Query Language (CQL)

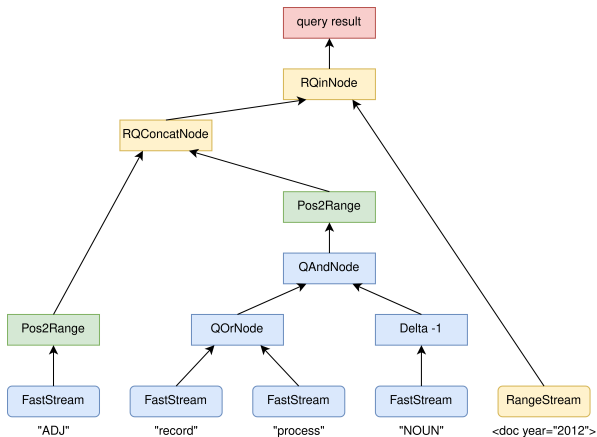
- ? optional token
- * any number of repetition
- + at least one
- {N} exact number of repetitions
- {M,N} from M to N repetitions
- [] any token
- examples:
 - []{1,3} [word="un.*"]
 - First, up to three words before "un.*".

Corpus Query Language (CQL)

- within - sequence within sequence
- containing - inverse of within, matches results of the first subquery, which contains matches of the second subquery
- other:
 - union, meet, global conditions, structure boundaries
- example:
 - `[word="process"] within <doc year="2012"/>`

Corpus Query Language (CQL)

`[tag="ADJ"]+ [(word="record" | word="process") & tag="NOUN"]
within <doc year="2012"/>`



Terms

- Most frequent combination of keywords. (Not ideal.)
- Most frequent combination of keywords without stopwords. (Not ideal.)
- Term grammar.

Thank You for Your Attention!

[PV 211] 06 Word and Document Embeddings

Santosh Kesiraju

March 27, 2024

About me

- Researcher in Speech@FIT, Brno University of Technology.
- Working at the intersection of speech and NLP.
 - Speech recognition, translation.
 - Spoken dialogue systems.
 - Multilingual models.
 - Interpretability of models.

Today's topics

1. Introduction to embeddings
2. Popular methods for learning word embeddings
 - continuous bag-of-words
 - skip-gram
3. Methods for learning document and word embeddings **jointly**
 - Paragraph vector and variants.
4. Objective function and gradient.
5. Interpretation of the gradient.

Where do we begin?

- Let's say you are given N number of text documents.
- **Tokenize** every document and build a set of unique words (vocabulary).
 - Vocabulary \mathcal{V} , where $V = |\mathcal{V}|$
 - Index the words from 1 to V .
- Example:

| word | index | word | index |
|-------------|-------|-----------|-------|
| a : | 1 | elephant: | 50 |
| antelope: | 2 | giraffe: | 61 |
| atmosphere: | 3 | ⋮ | ⋮ |
| ⋮ | ⋮ | tv: | 7289 |
| radio: | 5002 | | |
| ⋮ | ⋮ | | |
| xerox: | 12348 | | |
| ⋮ | ⋮ | | |

Build co-occurrence matrix

- Words co-occurring (follow) with other words.

| Word index ↓ | Word index → | | | | | | |
|-------------------------|---------------------|-------|--------|-------|-----------|-------|-------|
| | w_1 | w_2 | ... | w_i | w_{i+1} | ... | w_V |
| w_1 | 14 | 23 | 0 ... | 36 | 0 | 0 ... | 0 |
| w_2 | 1 | 0 | 14 ... | 0 | 3 | 2 ... | 0 |
| ⋮ | ... | 30 | 0 | ... | 0 | 0 | 1 |
| w_i | 12 | ... | 0 | 0 | ... | 30 | 0 |
| ⋮ | 12 | ... | 0 | 3 | ... | 0 | 0 |
| w_V | 0 | ... | 92 | 0 | ... | 6 | 0 |

Build contextual co-occurrence matrix

- Words are present in a given context window.

| Context index ↓ | Word index → | | | | | | |
|--------------------|--------------|-------|-------|-------|-----------|-------|-------|
| | w_1 | w_2 | ... | w_i | w_{i+1} | ... | w_V |
| C_1 | 1 | 1 | 0 ... | 1 | 0 | 0 ... | 0 |
| C_2 | 1 | 0 | 1 ... | 0 | 1 | 0 ... | 0 |
| ⋮ | ... | 1 | 0 | ... | 0 | 0 | 1 |
| C_i | 1 | ... | 0 | 0 | ... | 1 | 0 |
| ⋮ | 1 | ... | 0 | 1 | ... | 0 | 0 |
| C_M | 0 | ... | 1 | 0 | ... | 1 | 0 |

Build n -gram co-occurrence matrix

- Number of times a word follows given a $n - 1$ gram history.

| History index ↓ | Word index → | | | | | | |
|--------------------|--------------|-------|--------|-------|-----------|-------|-------|
| | w_1 | w_2 | ... | w_i | w_{i+1} | ... | w_V |
| \mathcal{H}_1 | 3 | 1 | 0 ... | 15 | 0 | 0 ... | 0 |
| \mathcal{H}_2 | 5 | 0 | 21 ... | 0 | 6 | 0 ... | 0 |
| ⋮ | ... | 6 | 0 | ... | 0 | 0 | 9 |
| \mathcal{H}_i | 12 | ... | 0 | 0 | ... | 12 | 0 |
| ⋮ | 1 | ... | 0 | 13 | ... | 0 | 0 |
| \mathcal{H}_M | 20 | ... | 1 | 0 | ... | 11 | 0 |

Build Bag-of-words

- Represent every document n with word counts, **ignoring** the word order.

| Document index ↓ | Word index → | | | | | | |
|---------------------|--------------|-------|--------|-------|-----------|-------|-------|
| | w_1 | w_2 | ... | w_i | w_{i+1} | ... | w_V |
| 1 | 51 | 4 | 0 ... | 6 | 0 | 0 ... | 0 |
| 2 | 18 | 0 | 13 ... | 0 | 3 | 2 ... | 0 |
| ⋮ | ... | 0 | 0 | ... | 0 | 0 | 1 |
| n | 7 | ... | 0 | 0 | ... | 0 | 0 |
| ⋮ | 1 | ... | 0 | 3 | ... | 0 | 0 |
| N | 0 | ... | 29 | 0 | ... | 6 | 0 |

Problems with the co-occurrence matrices?

- They are sparse and huge.
- Hard to find relations between multiple words.
- Not optimal to use them as feature vectors in a machine learning model.

Word embeddings

- A low-dimensional continuous vector, that captures **word** semantics.
- Continuous vectors allows us to use them in other machine learning models (for classification, retrieval, clustering).

| Type of relationship | Word pair 1 | | Word pair 2 | |
|----------------------|-------------|------------|-------------|---------------|
| Common capital city | Athens | Greece | Oslo | Norway |
| All capital cities | Astana | Kazakhstan | Harare | Zimbabwe |
| Currency | Angola | Kwanza | Iran | Rial |
| City-in-state | Chicago | Illinois | Stockton | California |
| Man-Woman | brother | sister | grandson | granddaughter |
| Adjective-to-adverb | apparent | apparently | rapid | rapidly |
| Opposite | possibly | impossibly | ethical | unethical |

Document embeddings

- A low-dimensional continuous vector, that captures semantic relations of words present a document.
- Additionally learns word embeddings.
- Applications:
 - Discover topics from a large collection of documents.
 - Cluster documents based on similarity (one cluster - one topic).
 - Ability to compute similarity between words and documents.
 - Retrieve relevant documents given a query phrase.
 - Train classifiers on top of document embeddings for topic classification.
 - Multilingual models - cross-lingual topic discovery or classification.

Cross-lingual topic discovery

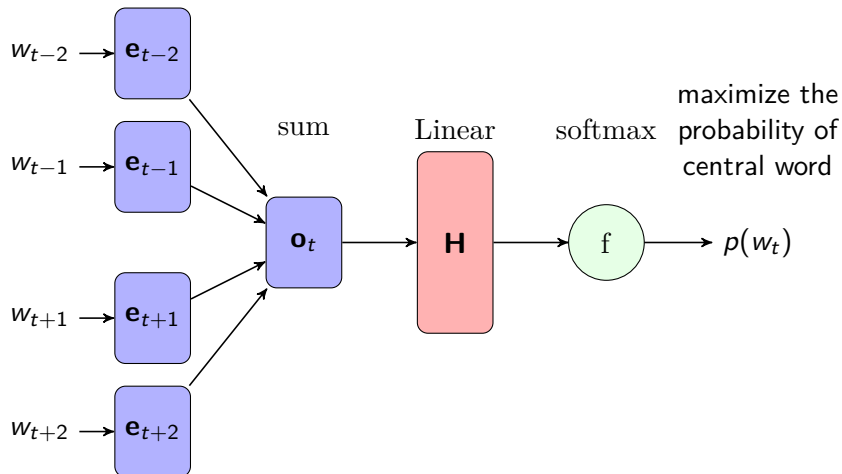
| | |
|----|---|
| EN | resellers, dealer, stabilises, volatility |
| DE | uberschussen, marktpreise, preislich, anzukommen |
| FR | negociants, volatilité, nourrie, commercialisent |
| IT | responsabilizzati, concessionari, volatilità, compra |
| ES | subprimes, pingues, mora, abastecer |
| EN | inflation, inflationary, predictions, slowdown |
| DE | wirtschaftsindikatoren, haushaltsdefiziten, inflationsrate, wirtschaftsdaten |
| FR | inflationniste, inflation, inflationnistes, pronostics |
| IT | inflazione, inflazionistici, inflazionistiche, ciclica |
| ES | inflacion, inflacionistas, predicciones, coyuntural |
| EN | overvaluation, yen, lira, dollar |
| DE | dollars, yuan, wechselkurses, chinesischem |
| FR | surevaluation, croissant, dollar, degonflement |
| IT | sopravalutazione, valutarì, yen, dollaro |
| ES | dolar, fly, yen, redondeo |

Table: An example of automatic discovery on Multilingual Reuters news.

Models for learning word embeddings

1. Continuous bag-of-words (CBoW)
2. Continuous skip-gram

CBoW



CBoW

- $\mathcal{C}_t = \{w_{t-2}, w_{t-1}, w_{t+1}, w_{t+2}\}$: context of word w_t .
- d : dimension of word embedding

$$\underbrace{\mathbf{o}_t}_{d \times 1} = \sum_{i \in \mathcal{C}_t} \underbrace{\mathbf{e}_i}_{d \times 1} \quad (1)$$

$$\underbrace{\mathbf{s}_t}_{V \times 1} = \underbrace{\mathbf{b}}_{V \times 1} + \underbrace{\mathbf{H}}_{V \times d} \underbrace{\mathbf{o}_t}_{d \times 1} \quad (2)$$

$$\underbrace{\boldsymbol{\theta}_t}_{V \times 1} = \text{softmax}(\mathbf{s}_t) \quad (3)$$

$$\text{softmax}(\mathbf{s}) := \frac{\exp\{s_i\}}{\sum_{j=1}^V s_j} \quad \forall i = 1 \dots V \quad (4)$$

$$p(w_t) := \theta_{w_t} := \theta_t \quad // \text{ abuse of notation for convenience}$$

- Training data $\mathcal{D} = \{(w_t, C_t) \dots\}$
set of words and corresponding contexts.
- $\mathbf{E} \in \mathbb{R}^{V \times d}$ word embeddings : *latent variables*.
- $\mathbf{H}, \mathbf{b} \in \mathbb{R}^{d \times V}$ linear projection matrix, and bias: *model parameters*.
- Training objective:

$$\begin{aligned} & \arg \max_{\mathbf{H}, \mathbf{b}, \mathbf{E}} \sum_{w_t, C_t \in \mathcal{D}} p(w_t | C_t) \\ & \arg \max_{\mathbf{H}, \mathbf{b}, \mathbf{E}} \sum_{w_t, C_t \in \mathcal{D}} \log p(w_t | C_t) \end{aligned} \quad (5)$$

CBoW: training objective

$$\begin{aligned}\mathcal{L} &= \sum_{\mathcal{D}} \log p(w_t | \mathcal{C}_t) \\ &= \sum_{\mathcal{D}} \log \theta_t \\ &= \sum_{\mathcal{D}} \log \left(\frac{\exp\{s_t\}}{\sum_{j=1}^V \exp\{s_j\}} \right) \\ &= \sum_{\mathcal{D}} s_t - \log \left(\sum_{j=1}^V \exp\{s_j\} \right) \\ &= \sum_{\mathcal{D}} (b_t + \mathbf{h}_t^\top \mathbf{o}_t) - \log \left(\sum_{j=1}^V \exp\{(b_j + \mathbf{h}_j^\top \mathbf{o}_t)\} \right) \\ &= \sum_{\mathcal{D}} (b_t + \mathbf{h}_t^\top \sum_{i \in \mathcal{C}_t} \mathbf{e}_i)_t - \log \left(\sum_{j=1}^V \exp \left\{ (b_j + \mathbf{h}_j^\top \sum_{i \in \mathcal{C}_t} \mathbf{e}_i) \right\} \right) \quad (6)\end{aligned}$$

CBoW: derivative of the objective

$$\mathcal{L} = \sum_{\mathcal{D}} (b_t + \mathbf{h}_t^\top \sum_{i \in \mathcal{C}_t} \mathbf{e}_i)_t - \log \left(\sum_{j=1}^V \exp \left\{ (b_j + \mathbf{h}_j^\top \sum_{i \in \mathcal{C}_t} \mathbf{e}_i) \right\} \right)$$

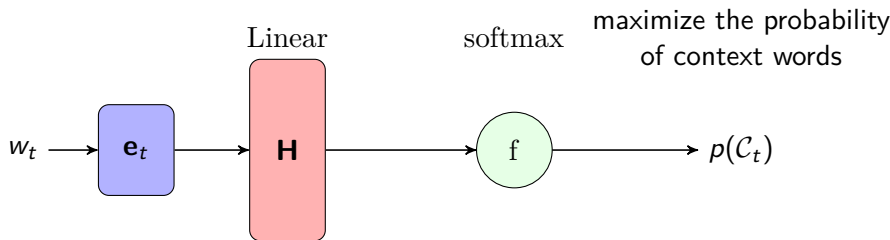
taking the derivative with respect to word embedding \mathbf{e}_i

$$\frac{\partial \mathcal{L}}{\partial \mathbf{e}_i} = \sum_{\mathcal{D}} \frac{\partial (b_t + \mathbf{h}_t^\top \sum_{i \in \mathcal{C}_t} \mathbf{e}_i)}{\partial \mathbf{e}_i} - \frac{\partial \log \left(\sum_{j=1}^V \exp \left\{ (b_j + \mathbf{h}_j^\top \sum_{i \in \mathcal{C}_t} \mathbf{e}_i) \right\} \right)}{\partial \mathbf{e}_i}$$

Remember the pattern in this expression.

1. derivative of a linear term.
2. derivative of a log-sum-exp.

Skip-gram



Skip-gram: training objective

- Training data $\mathcal{D} = \{(w_t, \mathcal{C}_t) \dots\}$
set of words and corresponding contexts.
- $\mathbf{E} \in \mathbb{R}^{V \times d}$ word embeddings.
- $\mathbf{H}, \mathbf{b} \in \mathbb{R}^{d \times V}$ linear projection matrix, and bias.
- Training objective:

$$\begin{aligned} \arg \max_{\mathbf{H}, \mathbf{b}, \mathbf{E}} \sum_{\mathcal{D}} p(\mathcal{C}_t | w_t) \\ &= \sum_{\mathcal{D}} p(w_{t-2} | w_t) p(w_{t-1} | w_t) p(w_{t+1} | w_t) p(w_{t+2} | w_t) \\ &= \sum_{\mathcal{D}} \prod_{w_k \in \mathcal{C}_t} p(w_k | w_t) \\ &= \sum_{\mathcal{D}} \log \left(\prod_{w_k \in \mathcal{C}_t} p(w_k | w_t) \right) \\ &= \sum_{\mathcal{D}} \sum_{w_k \in \mathcal{C}_t} \log p(w_k | w_t) \end{aligned}$$

Skip-gram: training objective

$$\begin{aligned}\mathcal{L} &= \sum_{\mathcal{D}} \sum_{w_k \in \mathcal{C}_t} \log p(w_k | w_t) \\ &= \sum_{\mathcal{D}} \sum_{w_k \in \mathcal{C}_t} \log(\theta_k) \quad \text{simplified notation: } \theta_{w_k} \rightarrow \theta_k \\ &= \sum_{\mathcal{D}} \sum_{w_k \in \mathcal{C}_t} \log \frac{\exp\{s_k\}}{\sum_{j=1}^V \exp\{s_j\}} \\ &= \sum_{\mathcal{D}} \sum_{w_k \in \mathcal{C}_t} s_k - \log \left(\sum_{j=1}^V \exp\{s_j\} \right) \\ &= \sum_{\mathcal{D}} \sum_{w_k \in \mathcal{C}_t} (b_k + \mathbf{h}_k^T \mathbf{e}_t) - \log \left(\sum_j \exp\{b_j + \mathbf{h}_j^T \mathbf{e}_t\} \right) \quad (7)\end{aligned}$$

skip-gram: derivative of the objective

$$\mathcal{L} = \sum_{\mathcal{D}} \sum_{w_k \in \mathcal{C}_t} (b_k + \mathbf{h}_k^T \mathbf{e}_t) - \log \left(\sum_j \exp \{ b_j + \mathbf{h}_j^T \mathbf{e}_t \} \right)$$

taking the derivative with respect to word embedding \mathbf{e}_i

$$\frac{\partial \mathcal{L}}{\partial \mathbf{e}_i} = \sum_{\mathcal{D}} \sum_{w_k \in \mathcal{C}_t} \frac{\partial (b_k + \mathbf{h}_k^T \mathbf{e}_t)}{\partial \mathbf{e}_i} - \frac{\partial \log \left(\sum_{j=1}^V \exp \{ (b_j + \mathbf{h}_j^T \mathbf{e}_t) \} \right)}{\partial \mathbf{e}_i}$$

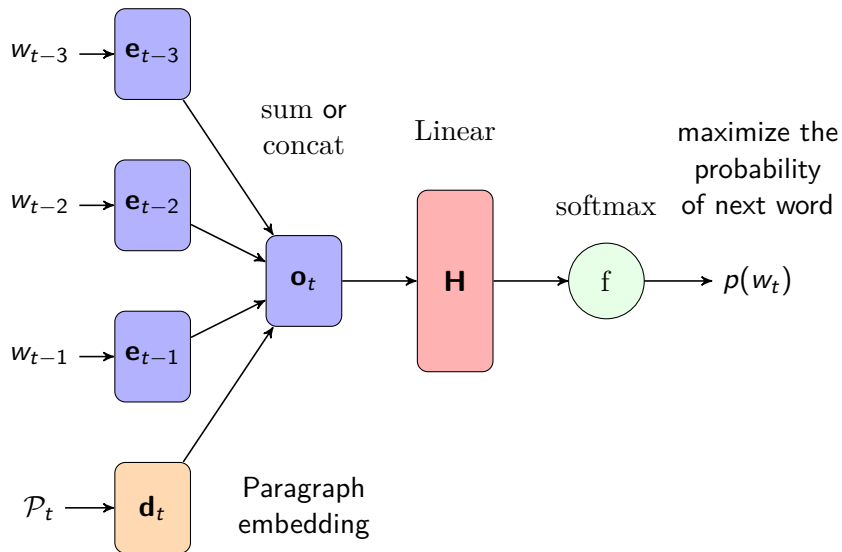
Similar pattern as earlier.

1. derivative of a linear term.
2. derivative of a log-sum-exp.

Paragraph vector (PV)

- Learn word and document embeddings jointly
 1. PV - distributed memory (PV-DM)
 2. PV - distributed bag-of-words (PV-DBOW)

PV-DM



PV-DM

- \mathcal{C}_t : a set with n number of context (history) words for w_t

option 1: sum

$$\underbrace{\mathbf{o}_t}_{d \times 1} = \mathbf{d}_t + \sum_{w_k \in \mathcal{C}_t} \mathbf{e}_k \quad // \text{ notation: } \mathbf{e}_{w_k} \rightarrow \mathbf{e}_k$$
$$\mathbf{s}_t = \mathbf{b} + \underbrace{\mathbf{H}}_{V \times d} \mathbf{o}_t$$

option 2: concat

$$\underbrace{\mathbf{o}_t}_{(dn+1) \times 1} = [\mathbf{d}_t; \mathbf{e}_k; \dots] \quad \forall w_k \in \mathcal{C}_t$$
$$\mathbf{s}_t = \mathbf{b} + \underbrace{\mathbf{H}}_{V \times (dn+1)} \mathbf{o}_t$$

generic notation for both options:

$$\mathbf{o}_t = f(\mathbf{d}_t, \mathbf{E}, \mathcal{C}_t)$$

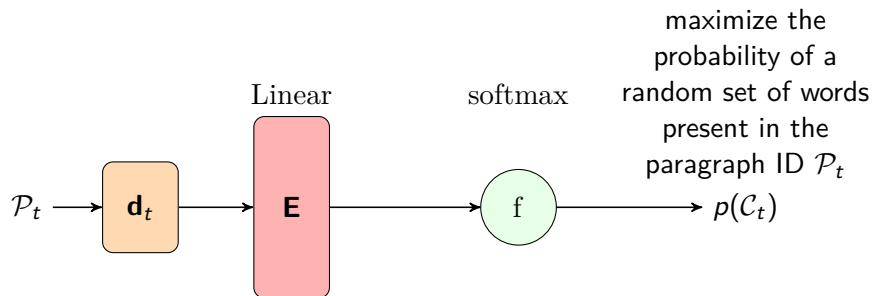
PV-DM: training objective

- Training data $\mathcal{D} = \{(w_t, \mathcal{C}_t, \mathcal{P}_t) \dots\}$
- $\mathbf{E} \in \mathbb{R}^{V \times d}$ word embeddings.
- $\mathbf{H}, \mathbf{b} \in \mathbb{R}^{d \times V}$ linear projection matrix, and bias.
- $\mathbf{D} \in \mathbb{R}^{d \times M}$ M number of paragraph (document) embeddings.

$$\begin{aligned} \arg \max_{\mathbf{H}, \mathbf{b}, \mathbf{E}, \mathbf{D}} \sum_{\mathcal{D}} p(w_t | \mathcal{C}_t, \mathcal{P}_t) \\ = \sum_{\mathcal{D}} \log p(w_t | \mathcal{C}_t, \mathcal{P}_t) \end{aligned} \quad (8)$$

$$\begin{aligned}\mathcal{L} &= \sum_{\mathcal{D}} \log p(w_t | \mathcal{C}_t, \mathcal{P}_t) \\ &= \sum_{\mathcal{D}} \log(\theta_t) \quad \text{simplified notation: } \theta_{w_t} \rightarrow \theta_t \\ &= \sum_{\mathcal{D}} \log \frac{\exp\{s_t\}}{\sum_{j=1}^V \exp\{s_j\}} \\ &= \sum_{\mathcal{D}} s_t - \log \left(\sum_{j=1}^V \exp\{s_j\} \right) \\ &= \sum_{\mathcal{D}} (b_t + \mathbf{h}_t^T \mathbf{o}_t) - \log \left(\sum_{j=1}^V (b_j + \mathbf{h}_j^T \mathbf{o}_t) \right)\end{aligned}$$

We ended up with a similar expression as before.



- \mathcal{C}_t : a random set of words in paragraph \mathcal{P}_t .
- Training data $\mathcal{D} = \{(\mathcal{C}_t, \mathcal{P}_t) \dots\}$
- $\mathbf{E} \in \mathbb{R}^{V \times d}$, $\mathbf{b} \in \mathbb{R}^{V \times 1}$ linear projection matrix, and bias.
- $\mathbf{D} \in \mathbb{R}^{d \times M}$ M number of paragraph (document) embeddings.

$$\begin{aligned}
 \arg \max_{\mathbf{E}, \mathbf{b}, \mathbf{D}} \sum_{\mathcal{D}} p(\mathcal{C}_t | \mathcal{P}_t) \\
 &= \sum_{\mathcal{D}} \prod_{w_k \in \mathcal{C}_t} p(w_k | \mathcal{P}_t) \\
 &= \sum_{\mathcal{D}} \sum_{w_k \in \mathcal{C}_t} \log p(w_k | \mathcal{C}_t, \mathcal{P}_t) \quad (9)
 \end{aligned}$$

Document model

- Generalize PV-DBoW to all the words present in the document.
- Let x_{ni} denote the number of occurrences of word w_i in document n .

$$\begin{aligned}\mathcal{L} &= \sum_n \prod_{i=1}^V p(w_{ni})^{x_{ni}} \\ &= \sum_n \sum_{i=1}^V \log p(w_{ni})^{x_{ni}} \\ &= \sum_n \sum_{i=1}^V x_{ni} \log \theta_{ni} \\ &= \sum_n \sum_{i=1}^V x_{ni} \log \frac{\exp\{b_i + \mathbf{e}_i^\top \mathbf{d}_n\}}{\sum_j \exp\{b_j + \mathbf{h}_j^\top \mathbf{d}_n\}}\end{aligned}$$

Document model: training objective

$$\begin{aligned}\mathcal{L} &= \sum_n \sum_{i=1}^V x_{ni} \log \frac{\exp\{b_i + \mathbf{e}_i^\top \mathbf{d}_n\}}{\sum_j \exp\{b_j + \mathbf{e}_j^\top \mathbf{d}_n\}} \\ &= \sum_n \sum_{i=1}^V x_{ni} \left[(b_i + \mathbf{e}_i^\top \mathbf{d}_n) - \log \left(\sum_j \exp\{b_j + \mathbf{e}_j^\top \mathbf{d}_n\} \right) \right]\end{aligned}$$

taking the derivative w.r.t. word embedding \mathbf{e}_k

$$\frac{\partial \mathcal{L}}{\partial \mathbf{e}_k} = \nabla_{\mathbf{e}_k} \mathcal{L}$$

derivative

$$\begin{aligned}
 \nabla_{\mathbf{e}_k} \mathcal{L} &= \frac{\partial \sum_{n=1}^N \sum_{i=1}^V x_{ni} \left[(b_i + \mathbf{e}_i^T \mathbf{d}_n) - \log \left(\sum_j \exp\{b_j + \mathbf{e}_j^T \mathbf{d}_n\} \right) \right]}{\partial \mathbf{e}_k} \\
 &= \sum_n \sum_i x_{ni} \left[\frac{\partial (b_i + \mathbf{e}_i^T \mathbf{d}_n)}{\partial \mathbf{e}_k} \right] - \sum_i x_{ni} \left[\frac{\partial \log \left(\sum_j \exp\{b_j + \mathbf{e}_j^T \mathbf{d}_n\} \right)}{\partial \mathbf{e}_k} \right] \\
 &= \sum_n \left[x_{nk} (\mathbf{d}_n^T) \right] - \sum_i x_{ni} \left[\frac{1}{\sum_j \exp\{b_j + \mathbf{e}_j^T \mathbf{d}_n\}} \left(\frac{\partial \sum_j \exp\{b_j + \mathbf{e}_j^T \mathbf{d}_n\}}{\partial \mathbf{e}_k} \right) \right] \\
 &= \sum_n \left[x_{nk} \mathbf{d}_n^T \right] - \sum_i x_{ni} \left[\frac{1}{\sum_j \exp\{b_j + \mathbf{e}_j^T \mathbf{d}_n\}} (0 + \dots + \exp\{b_k + \mathbf{e}_k^T \mathbf{d}_n\} \mathbf{d}_n^T) \right] \\
 &= \sum_n \left[x_{nk} \mathbf{d}_n^T \right] - \sum_i x_{ni} \left[\frac{\exp\{b_i + \mathbf{e}_k^T \mathbf{d}_n^T\}}{\sum_j \exp\{b_j + \mathbf{e}_j^T \mathbf{d}_n\}} \mathbf{d}_n \right] \\
 &= \sum_n \left[x_{nk} \mathbf{d}_n^T \right] - \sum_i x_{in} \left[\theta_{nk} \mathbf{d}_n^T \right] \\
 &= \sum_{n=1}^N \left[x_{nk} - \left(\sum_{i=1}^V x_{ni} \right) \theta_{nk} \right] \mathbf{d}_n^T
 \end{aligned}$$

derivative w.r.t word embeddings

$$\nabla_{\mathbf{e}_k} \mathcal{L} = \sum_{n=1}^N \left[x_{nk} - \left(\sum_{i=1}^V x_{ni} \right) \theta_{nk} \right] \mathbf{d}_n^T \quad (10)$$

- x_{nk} : number of times word k appeared in document n .
- θ_{nk} : the estimated probability of word k in document n .
- $\sum_i x_{ni}$: sum of all the word counts in document n .
- $(\sum_i x_{ni})\theta_{nk}$: relative count of word k in document n .
- $\left[x_{nk} - (\sum_i x_{ni})\theta_{nk} \right]$: the difference of absolute word count to the relative word count.
- $\left[x_{nk} - (\sum_i x_{ni})\theta_{nk} \right] \mathbf{d}_n$, and weight this along the direction of document embedding.
- The final gradient is the sum of all weighted document embeddings.

Why this gradient

- The softmax function appears nearly everywhere in current neural architectures.
- All forms of expressions involving softmax have the same interpretation.
- In the seminar, you will have hands on experience training the document model.
- Along with some application in classification, retrieval.



Lessons Learned While Building Infrastructure Software at Google

Jeff Dean

`jeff@google.com`

“Google” Circa 1997 (google.stanford.edu)



“Corkboards” (1999)



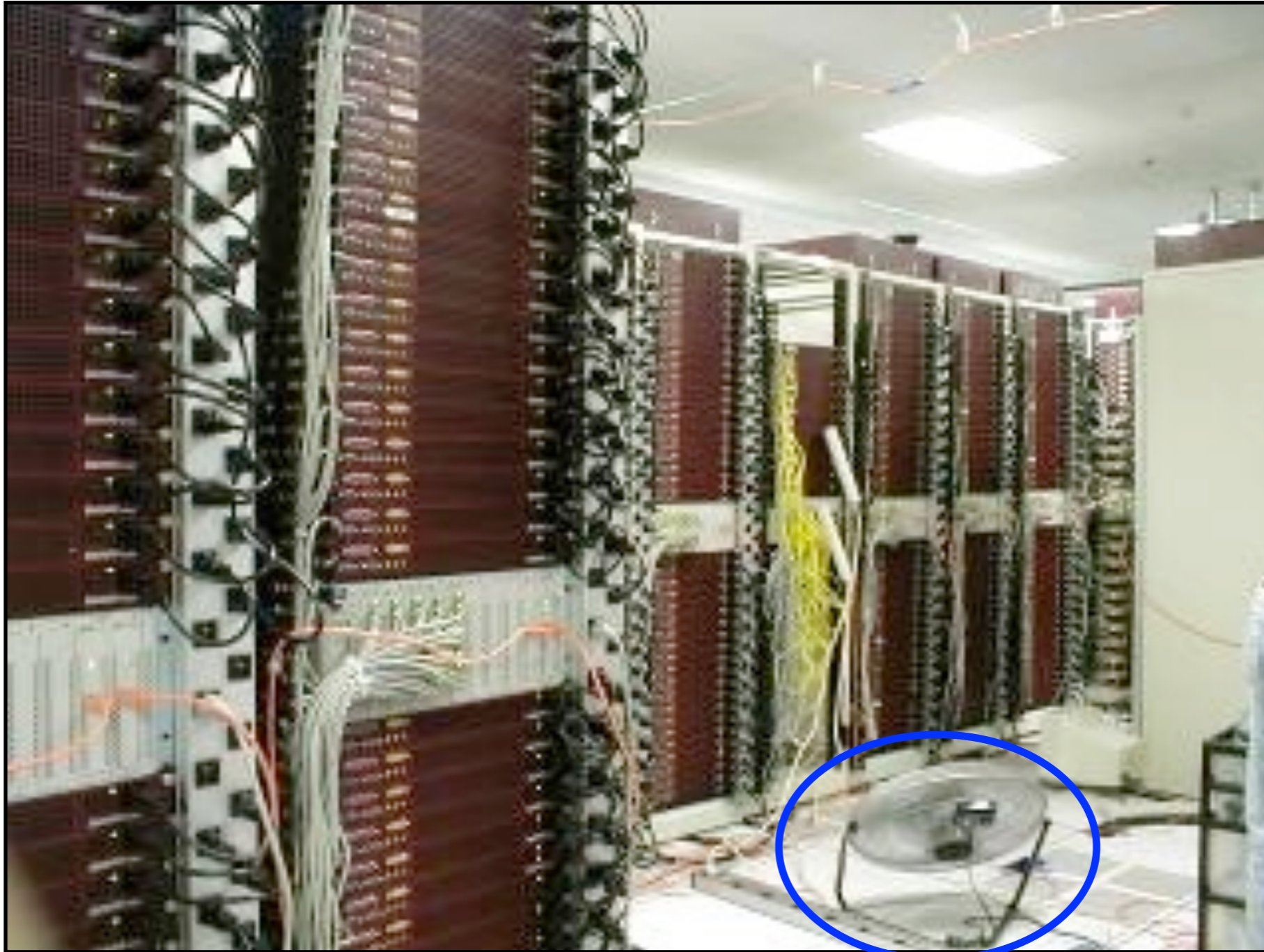
Google Data Center (2000)



Google Data Center (2000)



Google Data Center (2000)



Google (new data center 2001)

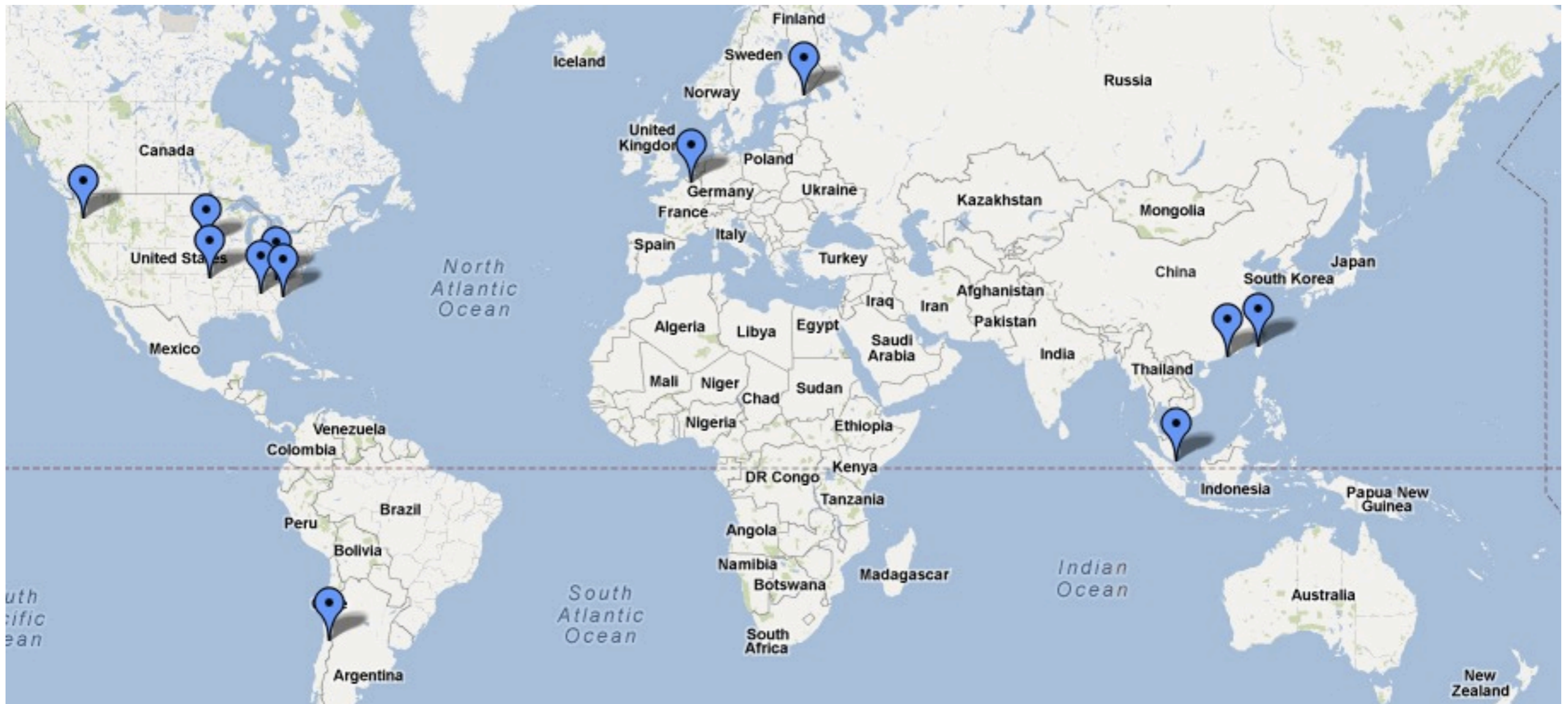


Google Data Center (3 days later)



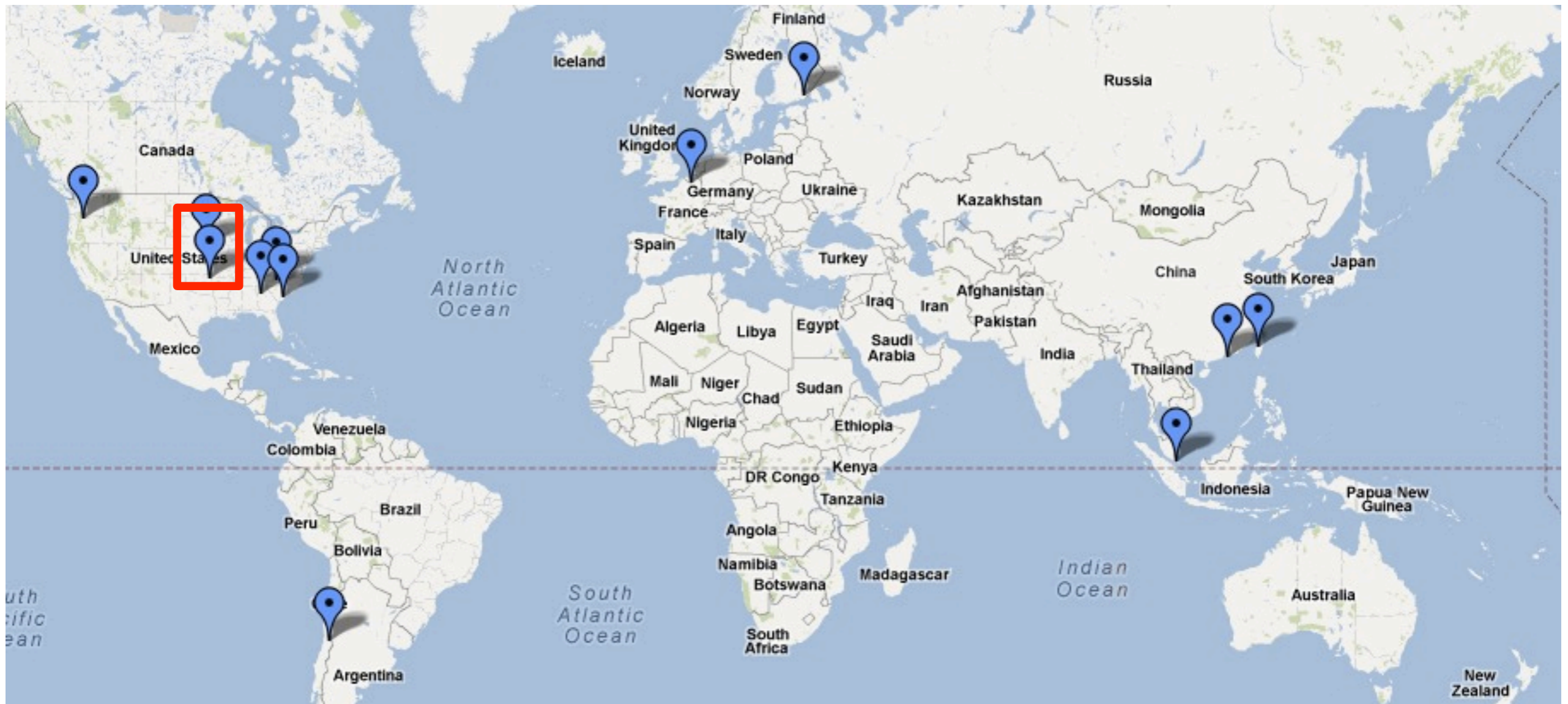
Google's Computational Environment Today

- Many datacenters around the world

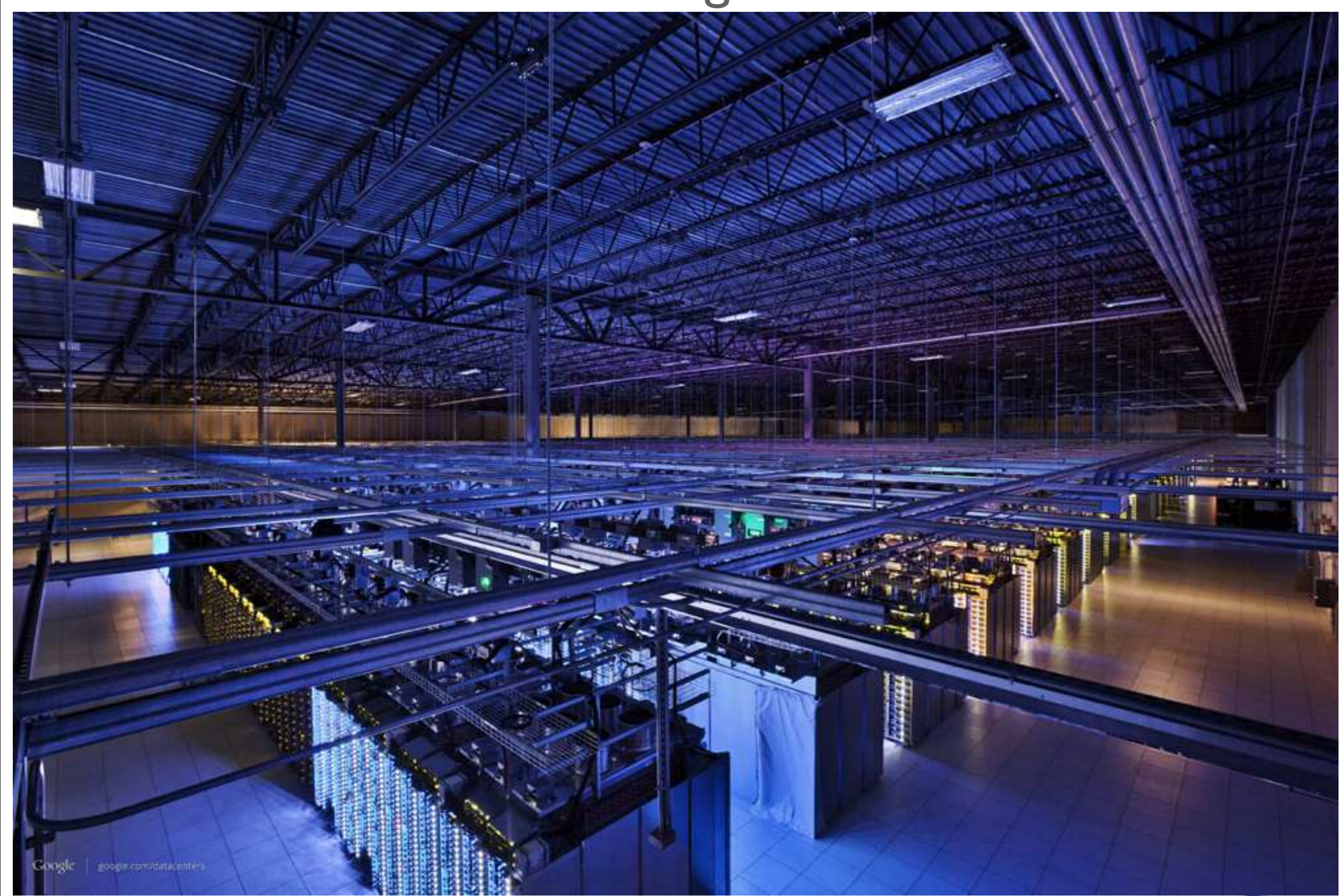


Google's Computational Environment Today

- Many datacenters around the world



Zooming In...



Lots of machines...



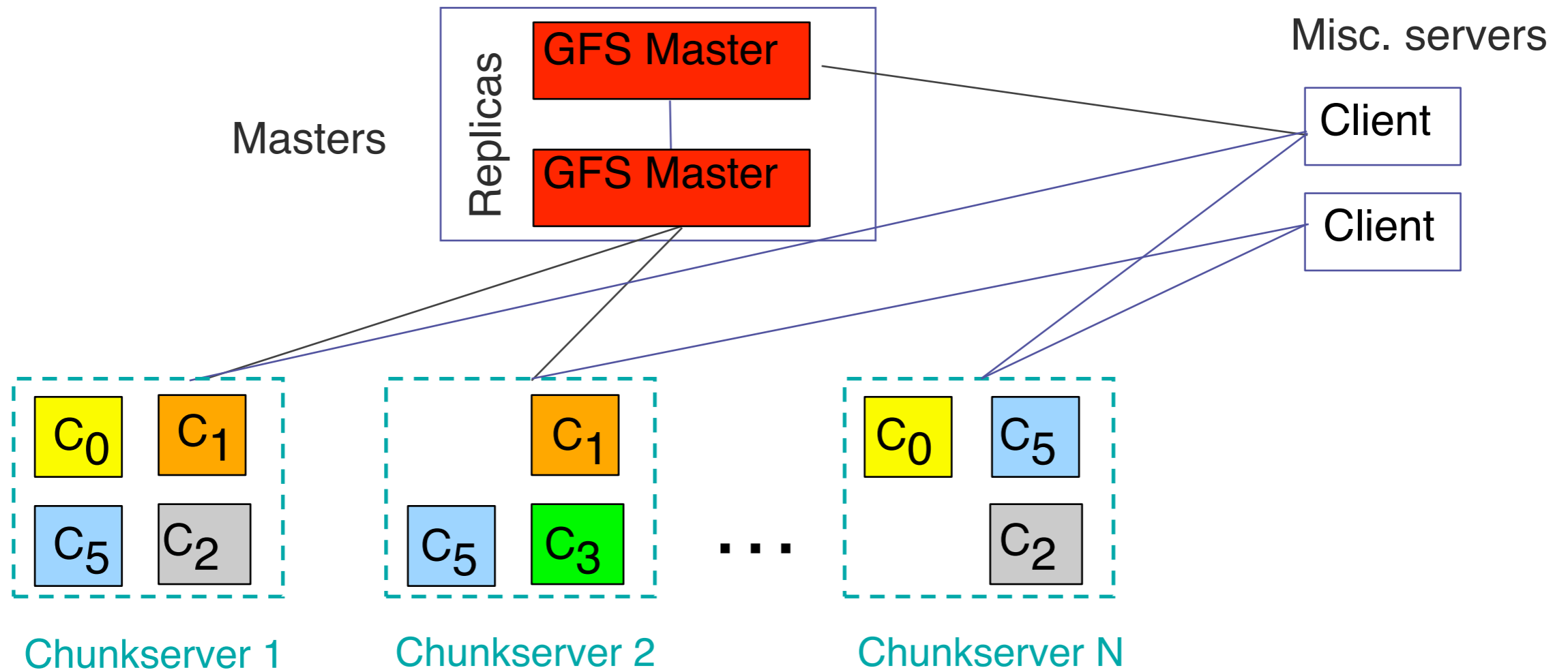
Cool...



Low-Level Systems Software Desires

- If you have lots of machines, you want to:
- **Store data persistently**
 - w/ high availability
 - high read and write bandwidth
- **Run large-scale computations reliably**
 - without having to deal with machine failures
- GFS, MapReduce, BigTable, Spanner, ...

Google File System (GFS) Design



- Master manages metadata
- Data transfers are directly between clients/chunkservers
- Files broken into chunks (typically 64 MB)
- Chunks replicated across multiple machines (usually 3)

GFS Motivation and Lessons

- Indexing system clearly needed a large-scale distributed file system
 - wanted to treat whole cluster as single file system
- Developed by subset of same people working on indexing system
- Identified minimal set of features needed
 - *e.g.* Not POSIX compliant
 - actual data was distributed, but kept metadata centralized
 - Colossus: Follow-on system developed many years later distributed the metadata
- Lesson: Don't solve everything all at once



MapReduce History

- 2003: Sanjay Ghemawat and I were working on rewriting indexing system:
 - starts with raw page contents on disk
 - many phases:
 - (near) duplicate elimination, anchor text extraction, language identification, index shard generation, etc.
 - end result is data structures for index and doc serving
- Each phase was hand written parallel computation:
 - hand parallelized
 - hand-written checkpointing code for fault-tolerance

MapReduce

- A simple programming model that applies to many large-scale computing problems
 - allowed us to express all phases of our indexing system
 - since used across broad range of computer science areas, plus other scientific fields
 - Hadoop open-source implementation seeing significant usage
- Hide messy details in MapReduce runtime library:
 - automatic parallelization
 - load balancing
 - network and disk transfer optimizations
 - handling of machine failures
 - robustness
 - **improvements to core library benefit all users of library!**



Typical problem solved by MapReduce

- Read a lot of data
- **Map**: extract something you care about from each record
- Shuffle and Sort
- **Reduce**: aggregate, summarize, filter, or transform
- Write the results

Outline stays the same,
User writes Map and Reduce functions to fit the problem



MapReduce Motivation and Lessons

- Developed by two people that were also doing the indexing system rewrite
 - squinted at various phases with an eye towards coming up with common abstraction
- Initial version developed quickly
 - proved initial API utility with very simple implementation
 - rewrote much of implementation 6 months later to add lots of the performance wrinkles/tricks that appeared in original paper
- Lesson: Very close ties with initial users of system make things happen faster
 - in this case, we were both building MapReduce and using it simultaneously

BigTable: Motivation

- Lots of (semi-)structured data at Google
 - URLs: Contents, crawl metadata, links, anchors, pagerank, ...
 - Per-user data: User preferences, recent queries, ...
 - Geographic locations: Physical entities, roads, satellite image data, user annotations, ...
- Scale is large
- Want to be able to grow and shrink resources devoted to system as needed

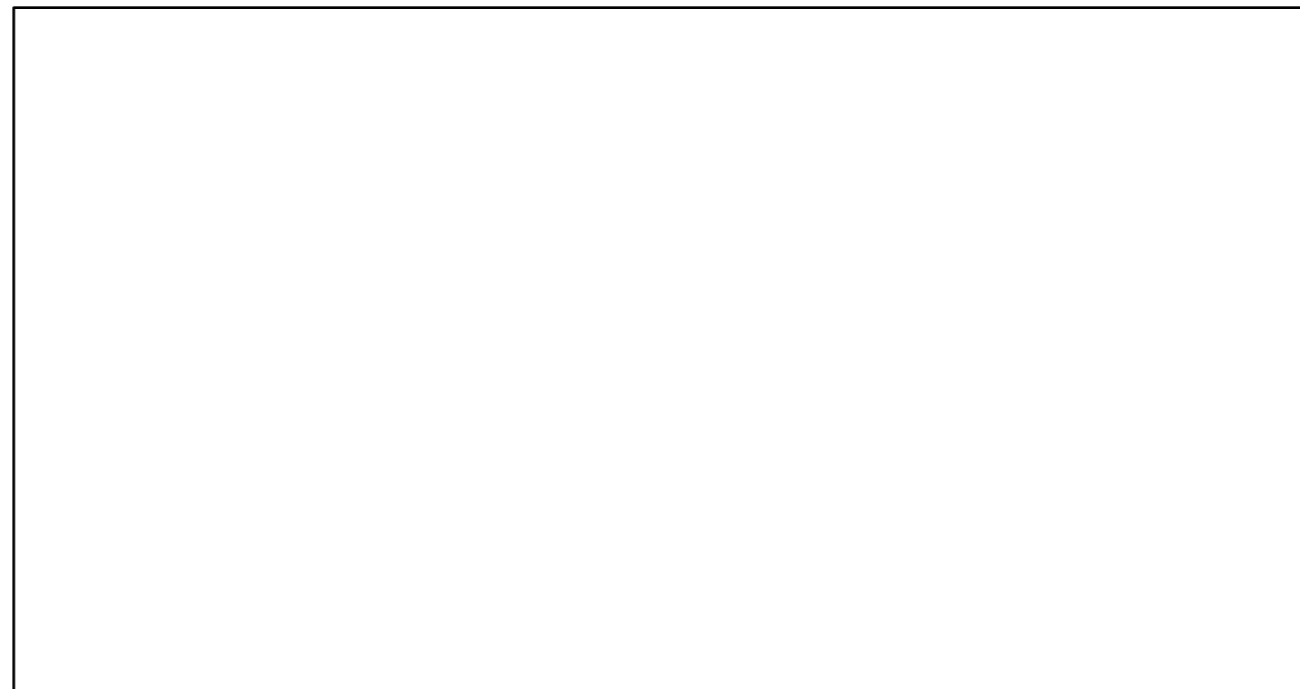


BigTable: Basic Data Model

- Distributed multi-dimensional sparse map
(row, column, timestamp) → cell contents

Rows

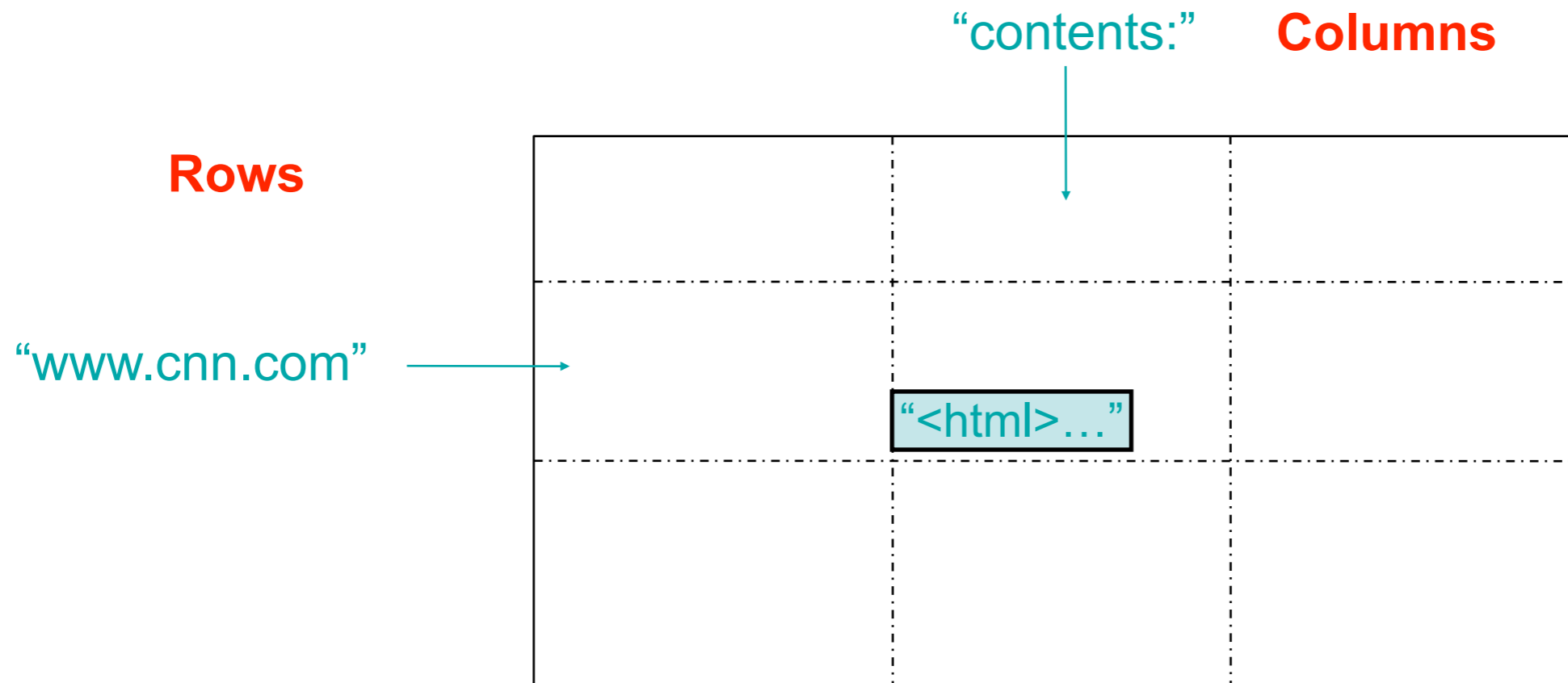
Columns



- Rows are ordered lexicographically
- Good match for most of our applications

BigTable: Basic Data Model

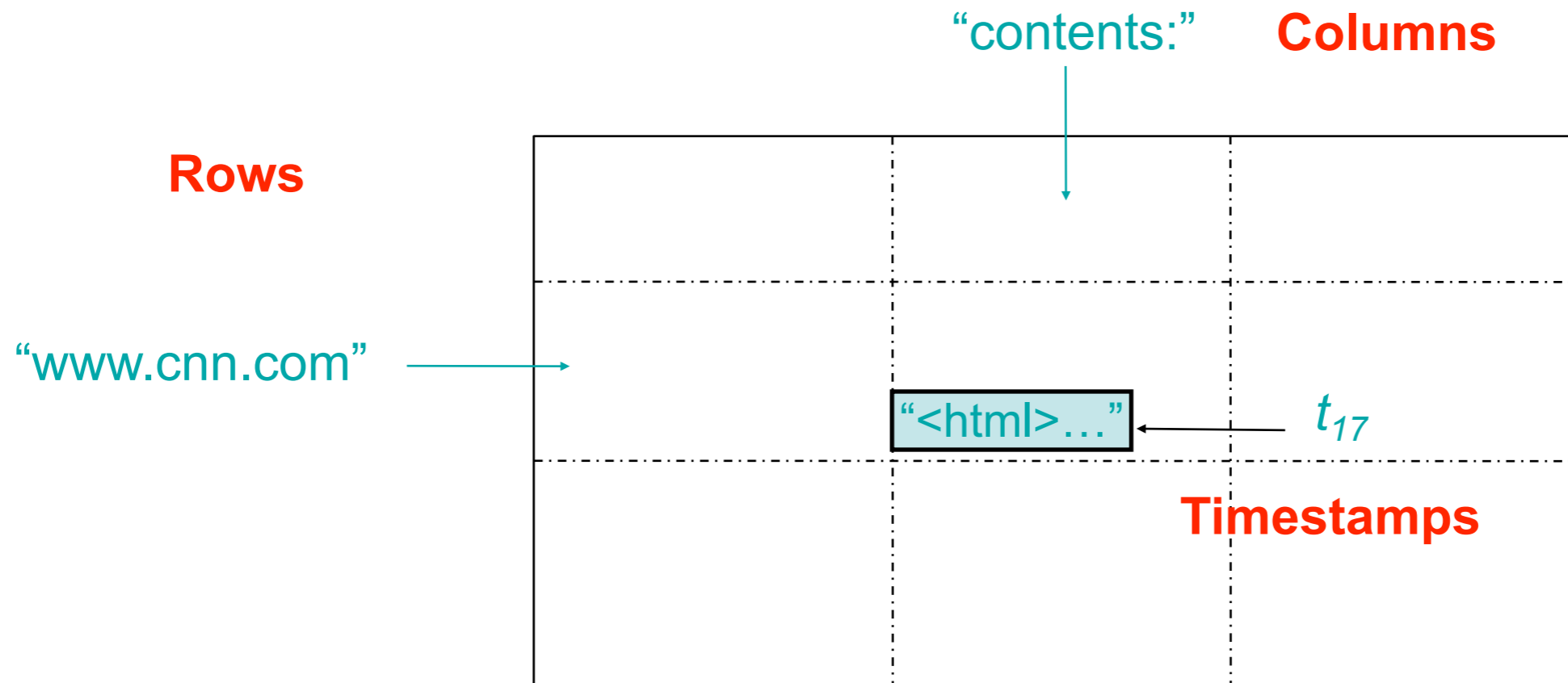
- Distributed multi-dimensional sparse map
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- Rows are ordered lexicographically
- Good match for most of our applications

BigTable: Basic Data Model

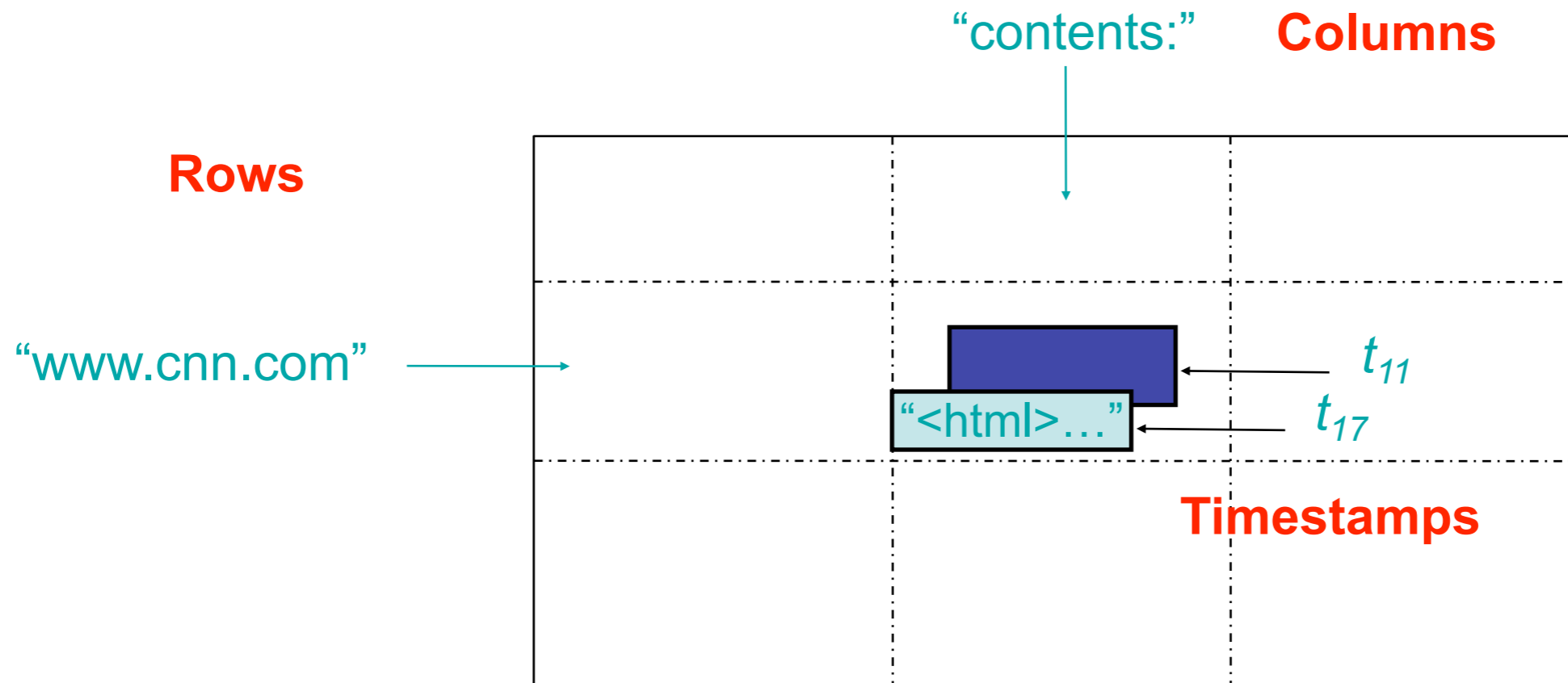
- Distributed multi-dimensional sparse map
 $(row, column, timestamp) \rightarrow cell\ contents$



- Rows are ordered lexicographically
- Good match for most of our applications

BigTable: Basic Data Model

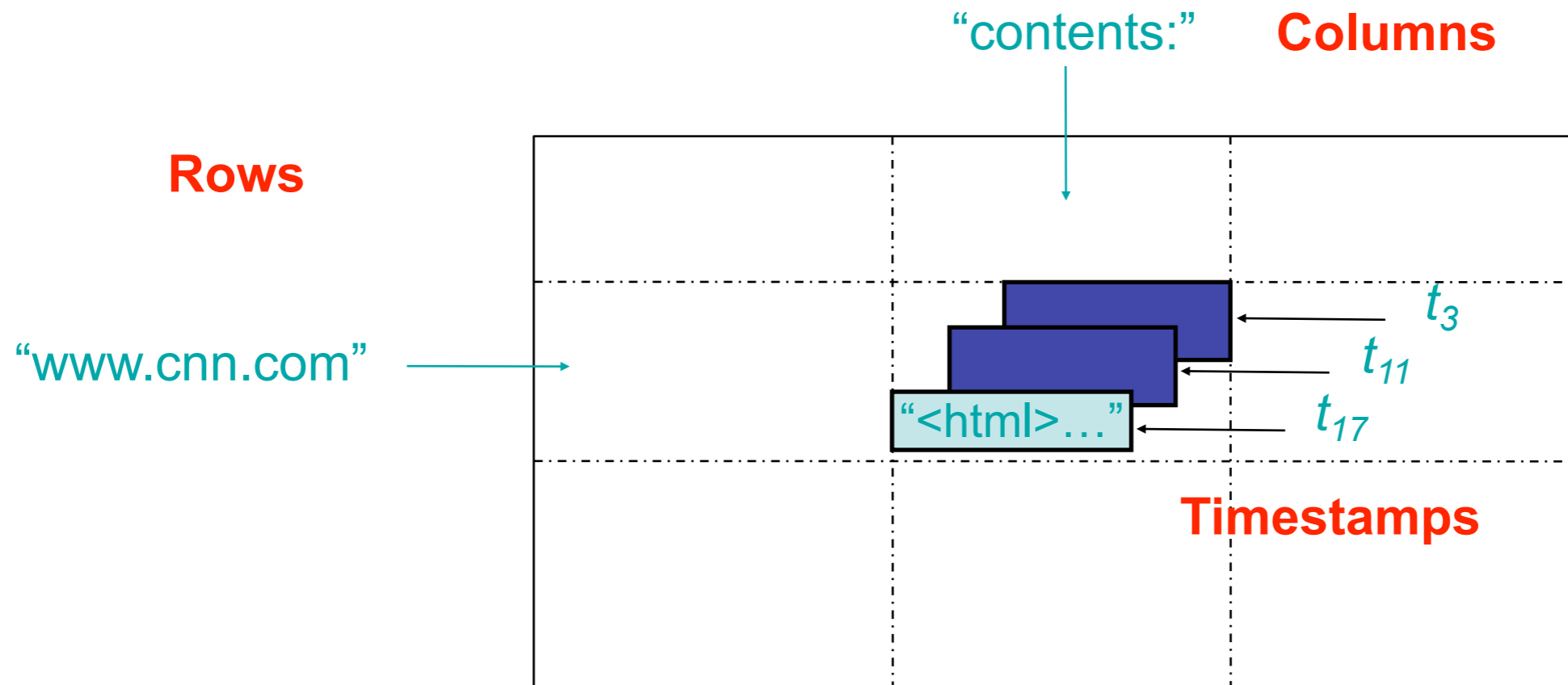
- Distributed multi-dimensional sparse map
 $(row, column, timestamp) \rightarrow cell\ contents$



- Rows are ordered lexicographically
- Good match for most of our applications

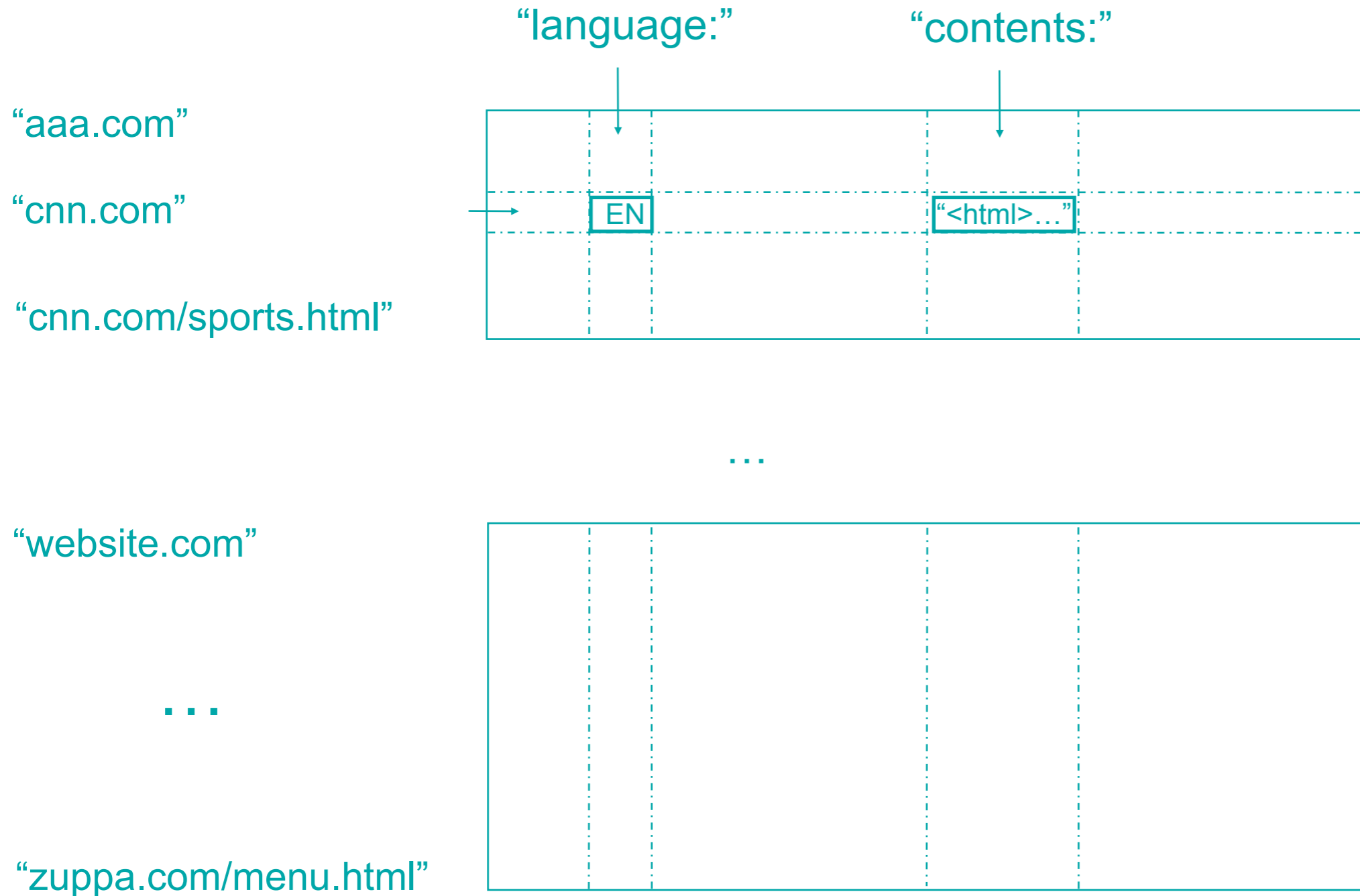
BigTable: Basic Data Model

- Distributed multi-dimensional sparse map
 $(row, column, timestamp) \rightarrow cell\ contents$

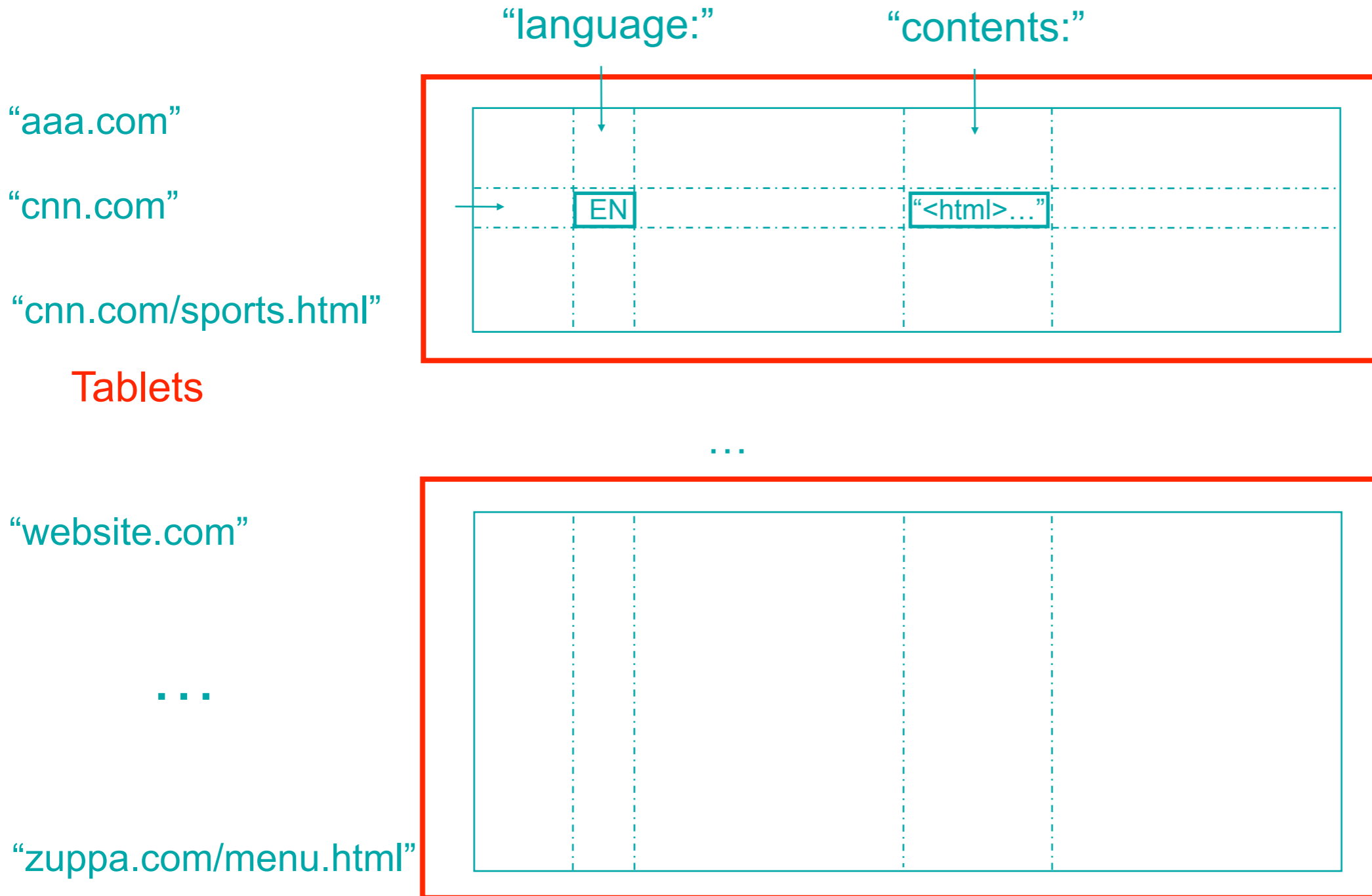


- Rows are ordered lexicographically
- Good match for most of our applications

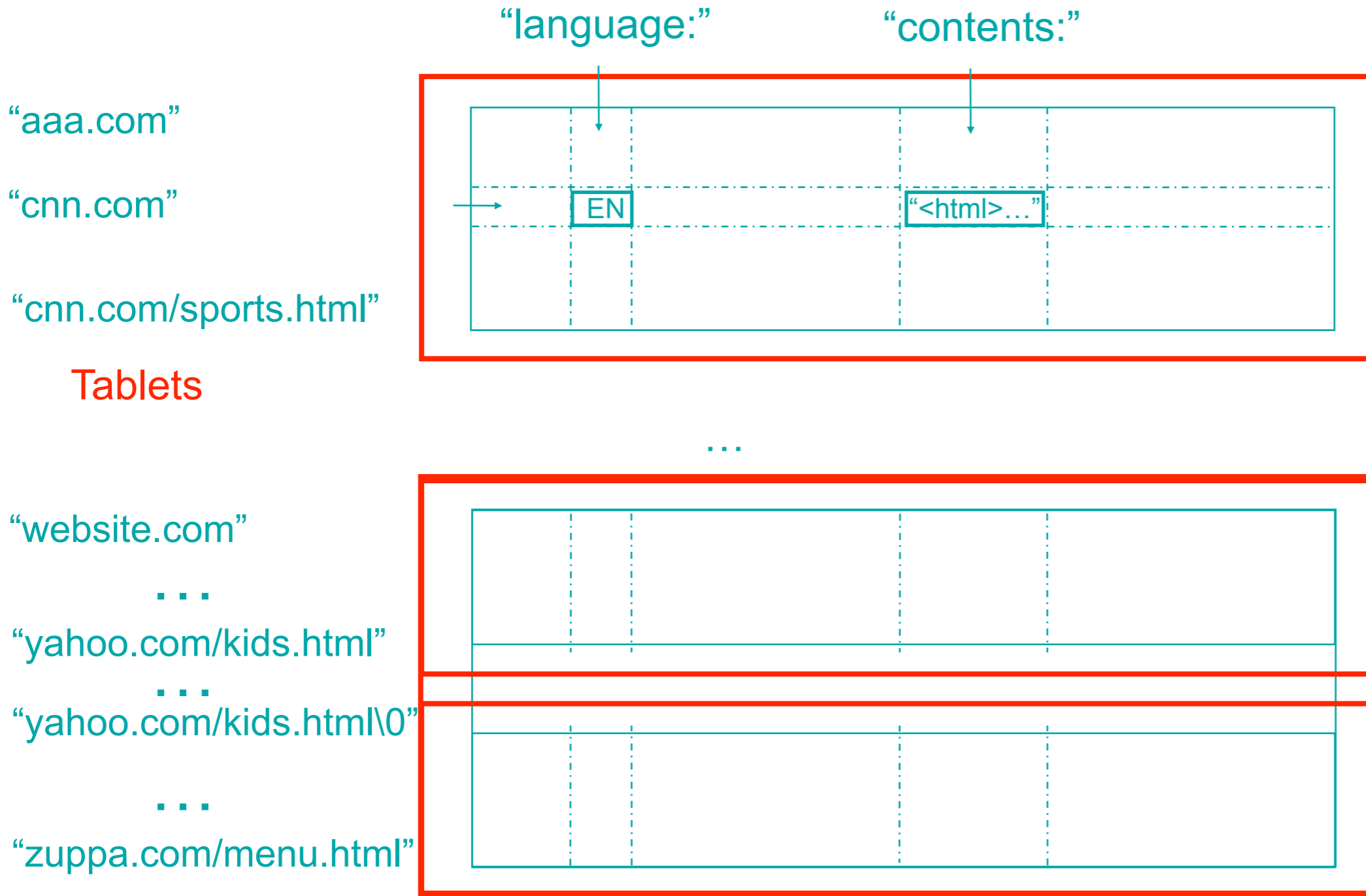
Tablets & Splitting



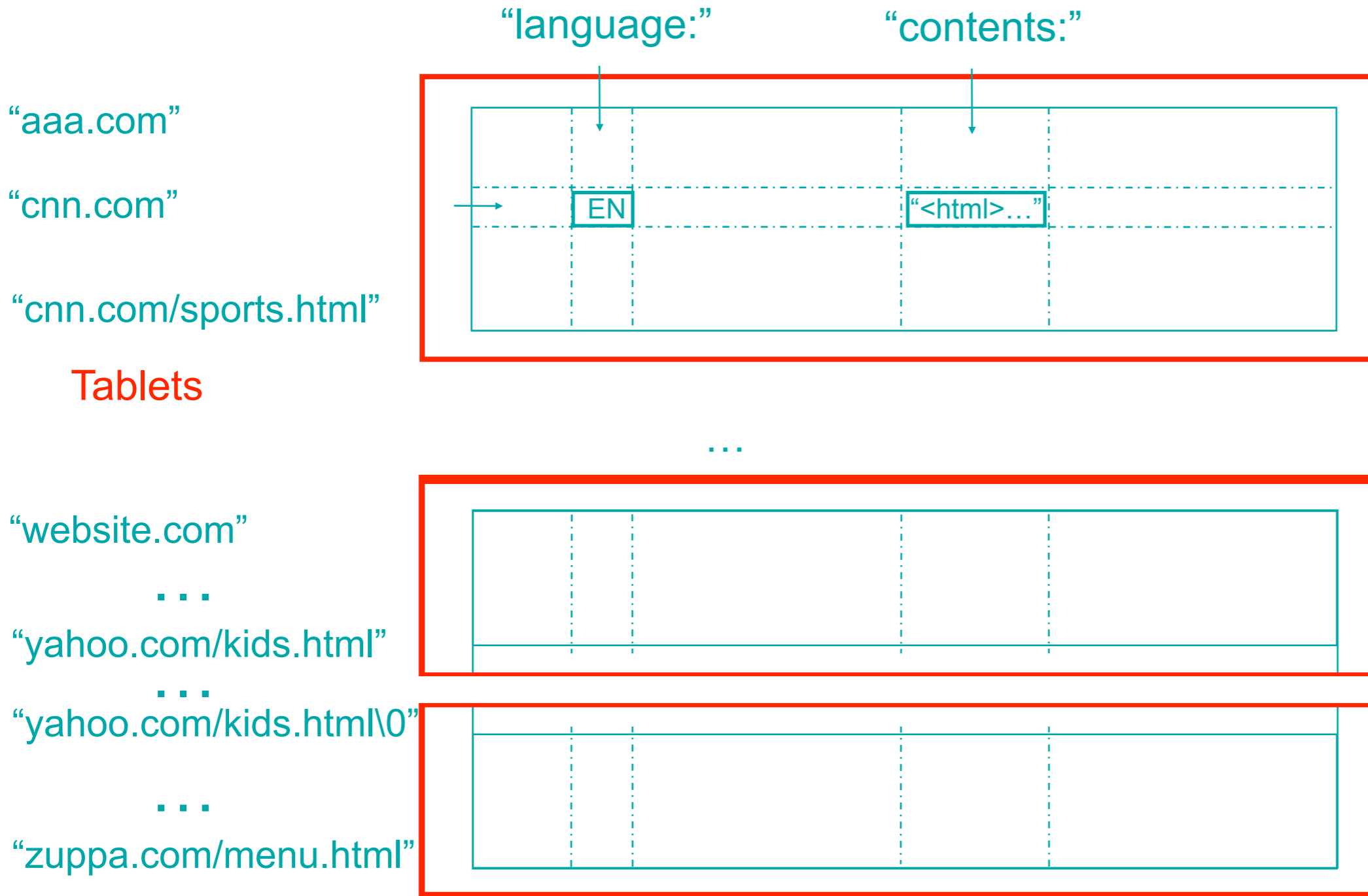
Tablets & Splitting



Tablets & Splitting



Tablets & Splitting



BigTable System Structure

Bigtable Cell

Bigtable master

Bigtable tablet server

Bigtable tablet server

...

Bigtable tablet server

BigTable System Structure

Bigtable Cell

Bigtable master

performs metadata ops +
load balancing

Bigtable tablet server

Bigtable tablet server

...

Bigtable tablet server

BigTable System Structure

Bigtable Cell

Bigtable master

performs metadata ops +
load balancing

Bigtable tablet server

serves data

Bigtable tablet server

serves data

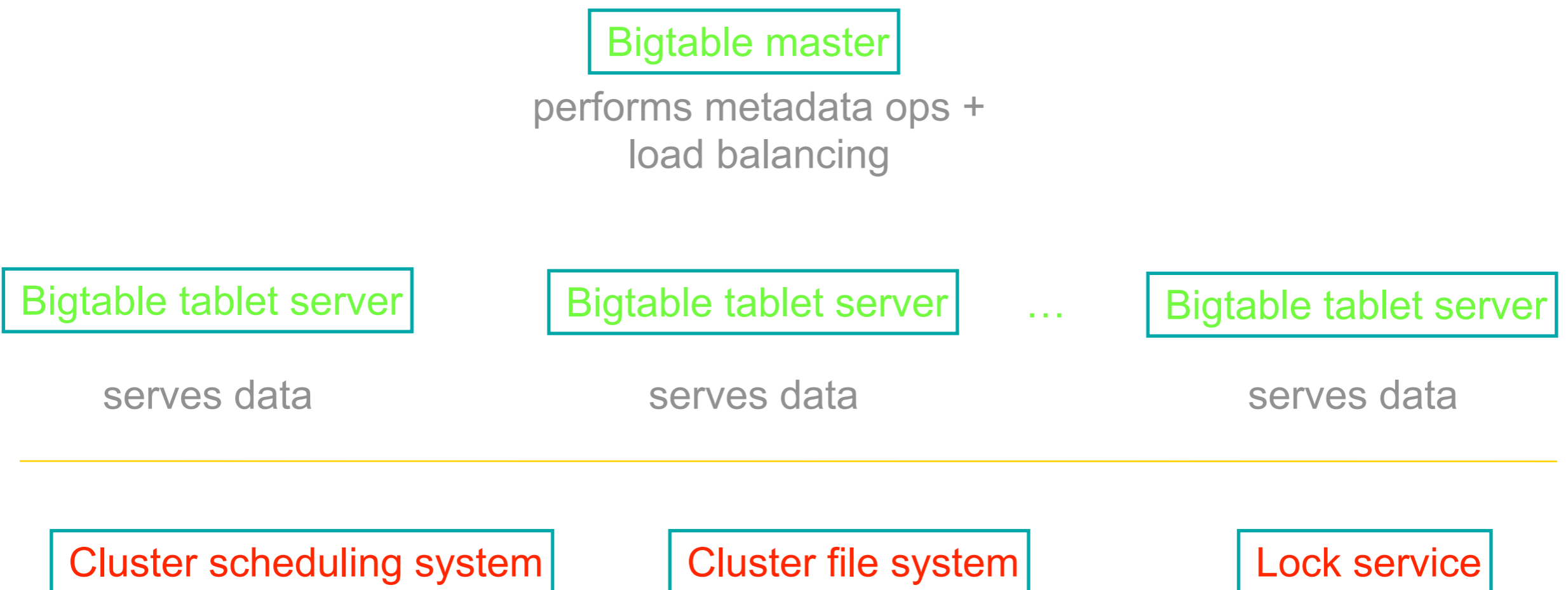
...

Bigtable tablet server

serves data

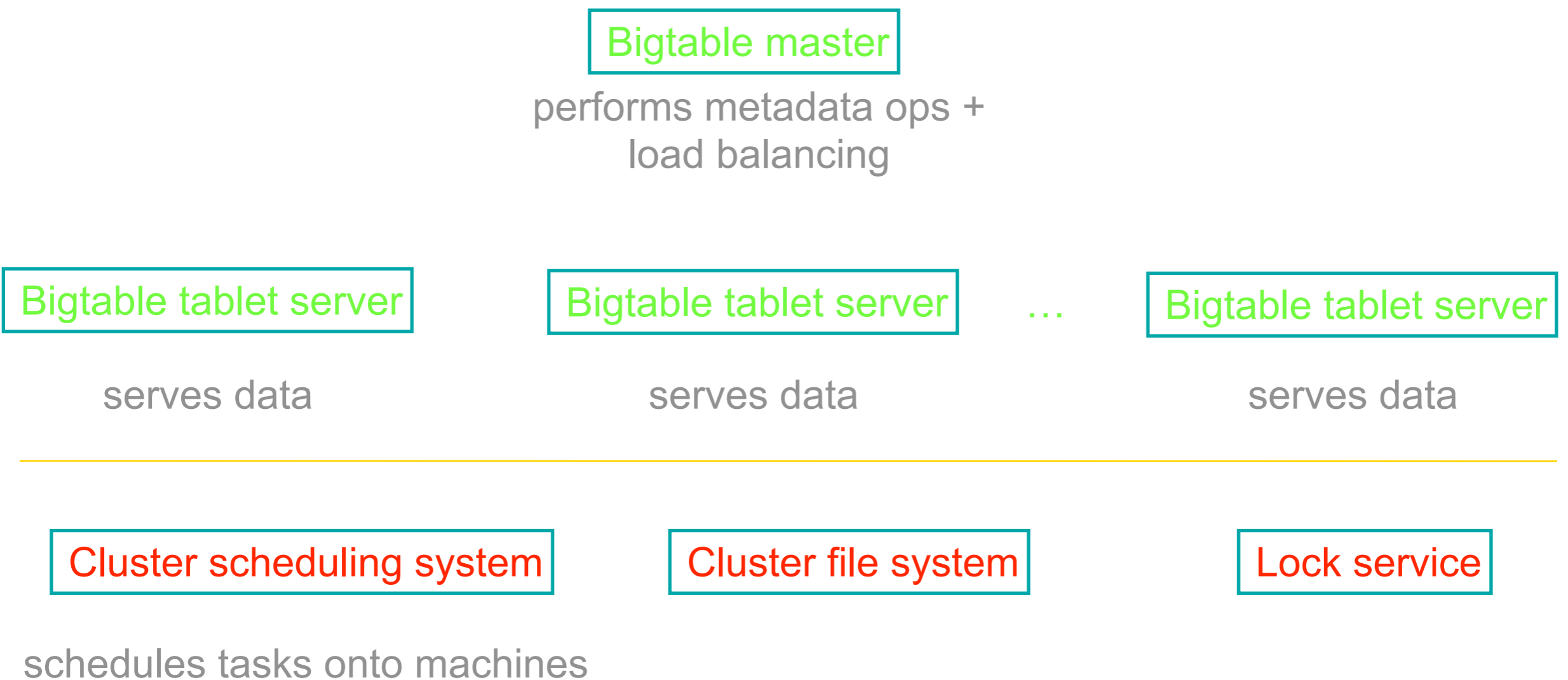
BigTable System Structure

Bigtable Cell



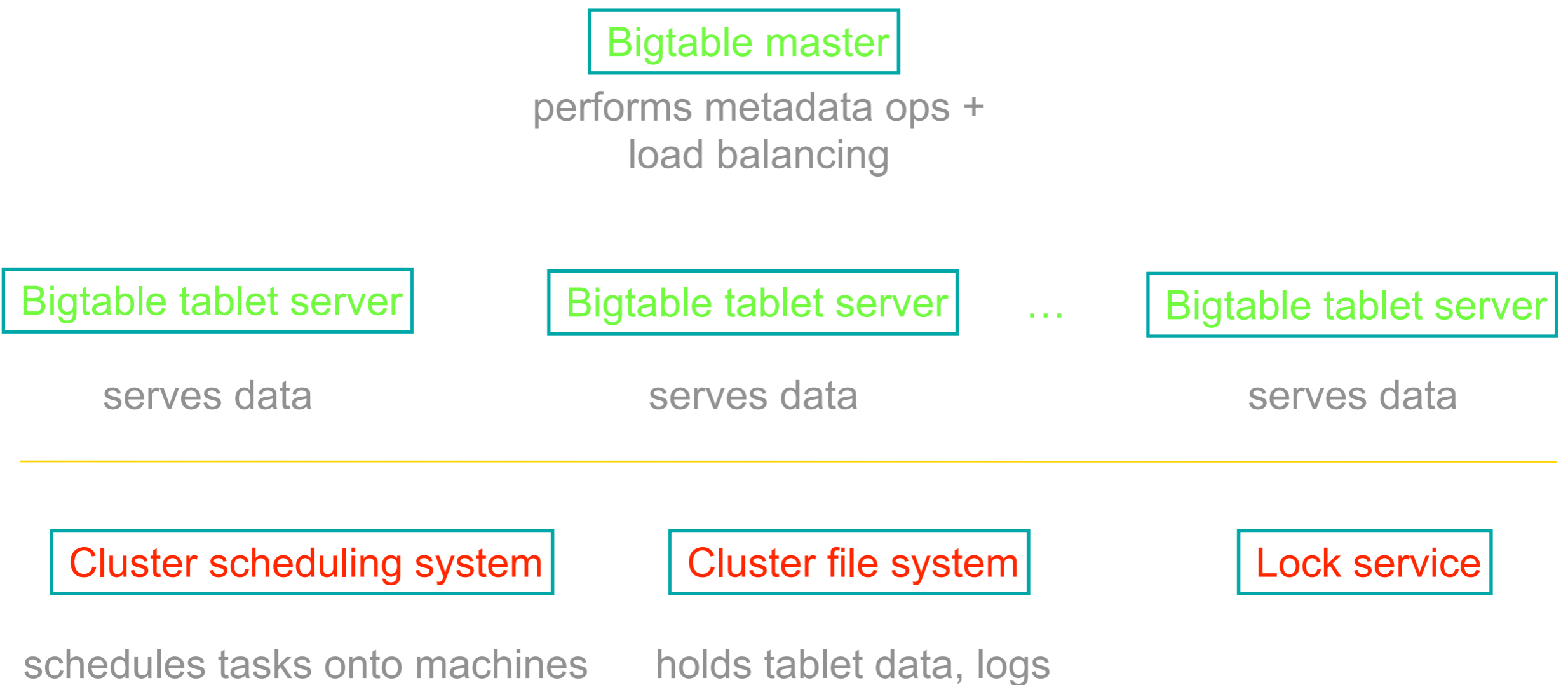
BigTable System Structure

Bigtable Cell



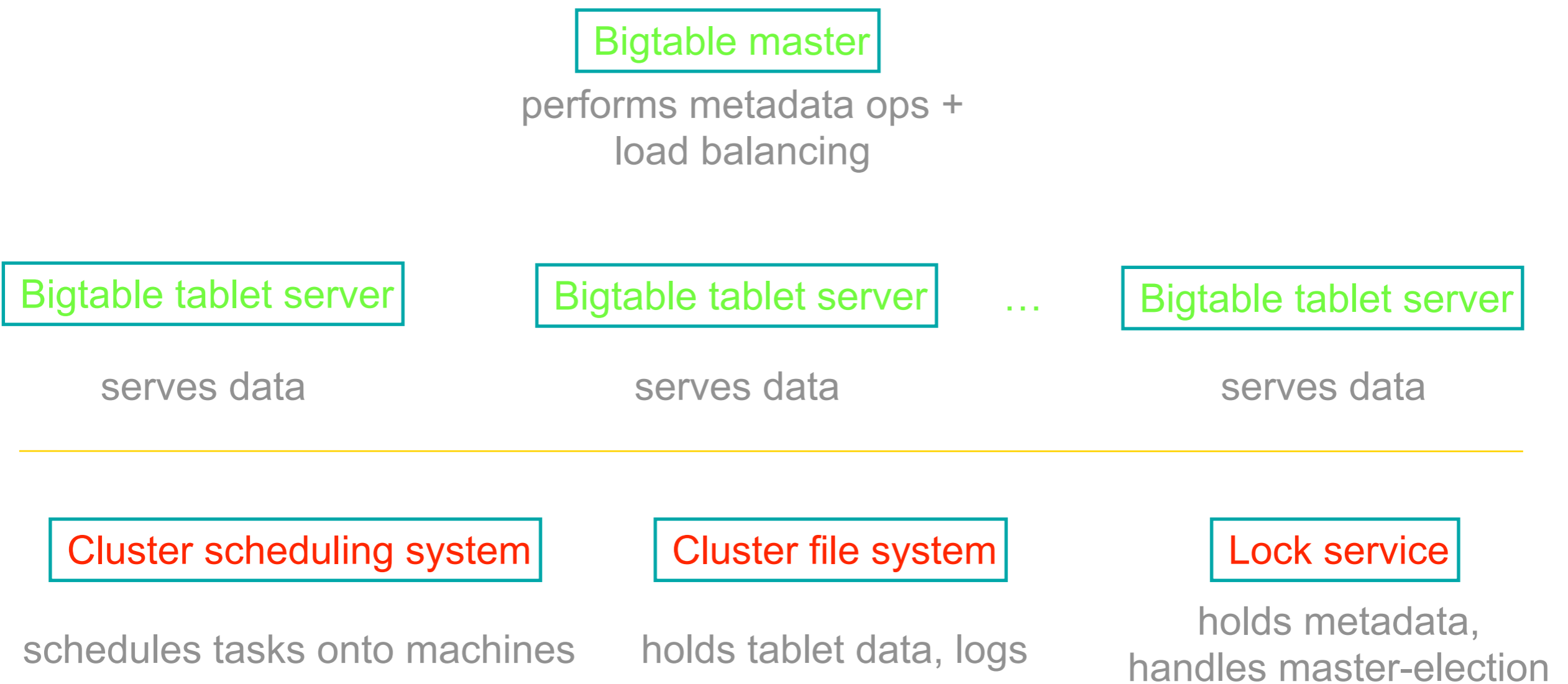
BigTable System Structure

Bigtable Cell



BigTable System Structure

Bigtable Cell



BigTable System Structure

Bigtable Cell

Bigtable client

Bigtable client
library

Bigtable master

performs metadata ops +
load balancing

Bigtable tablet server

serves data

Bigtable tablet server

serves data

...

Bigtable tablet server

serves data

Cluster scheduling system

schedules tasks onto machines

Cluster file system

holds tablet data, logs

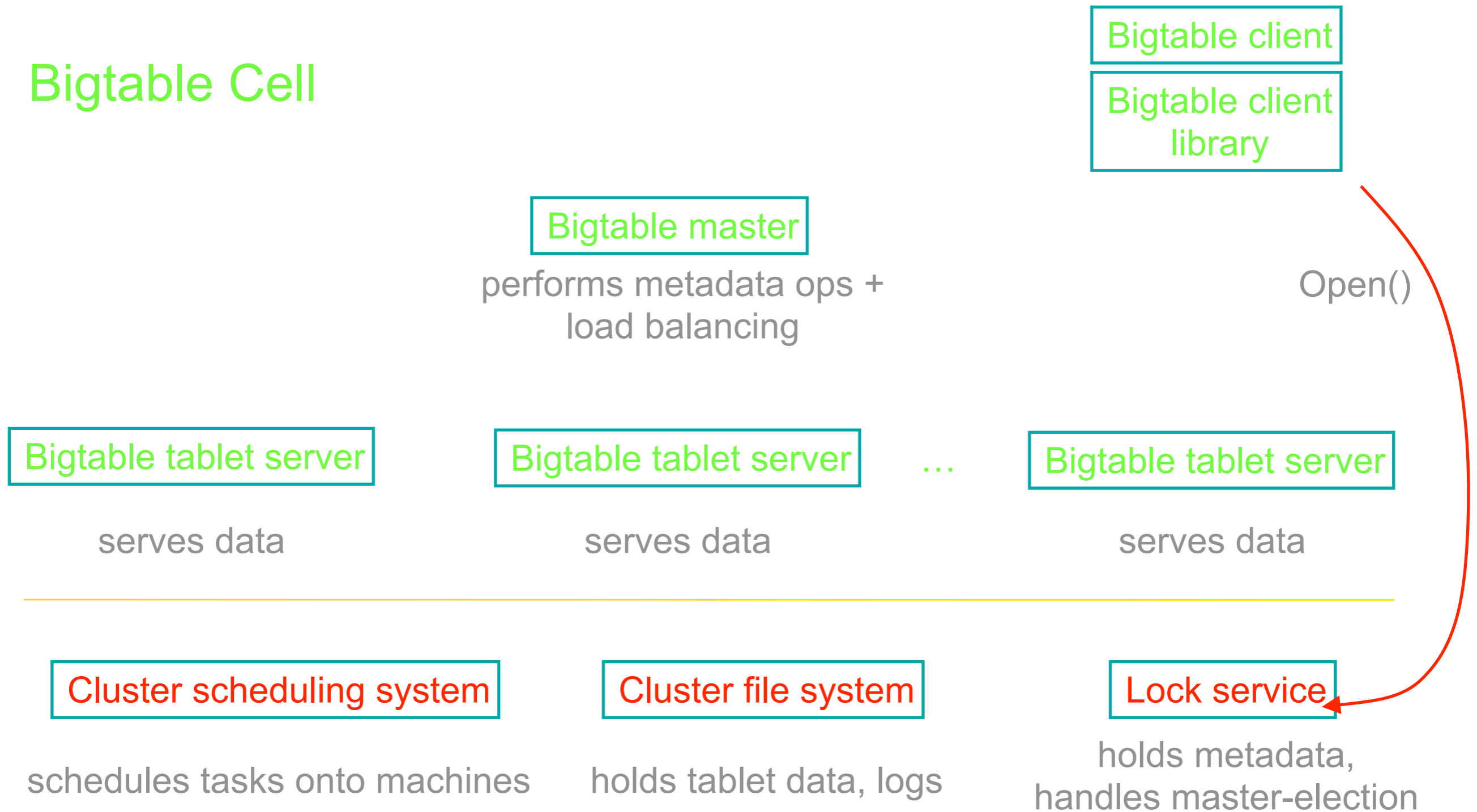
Lock service

holds metadata,
handles master-election



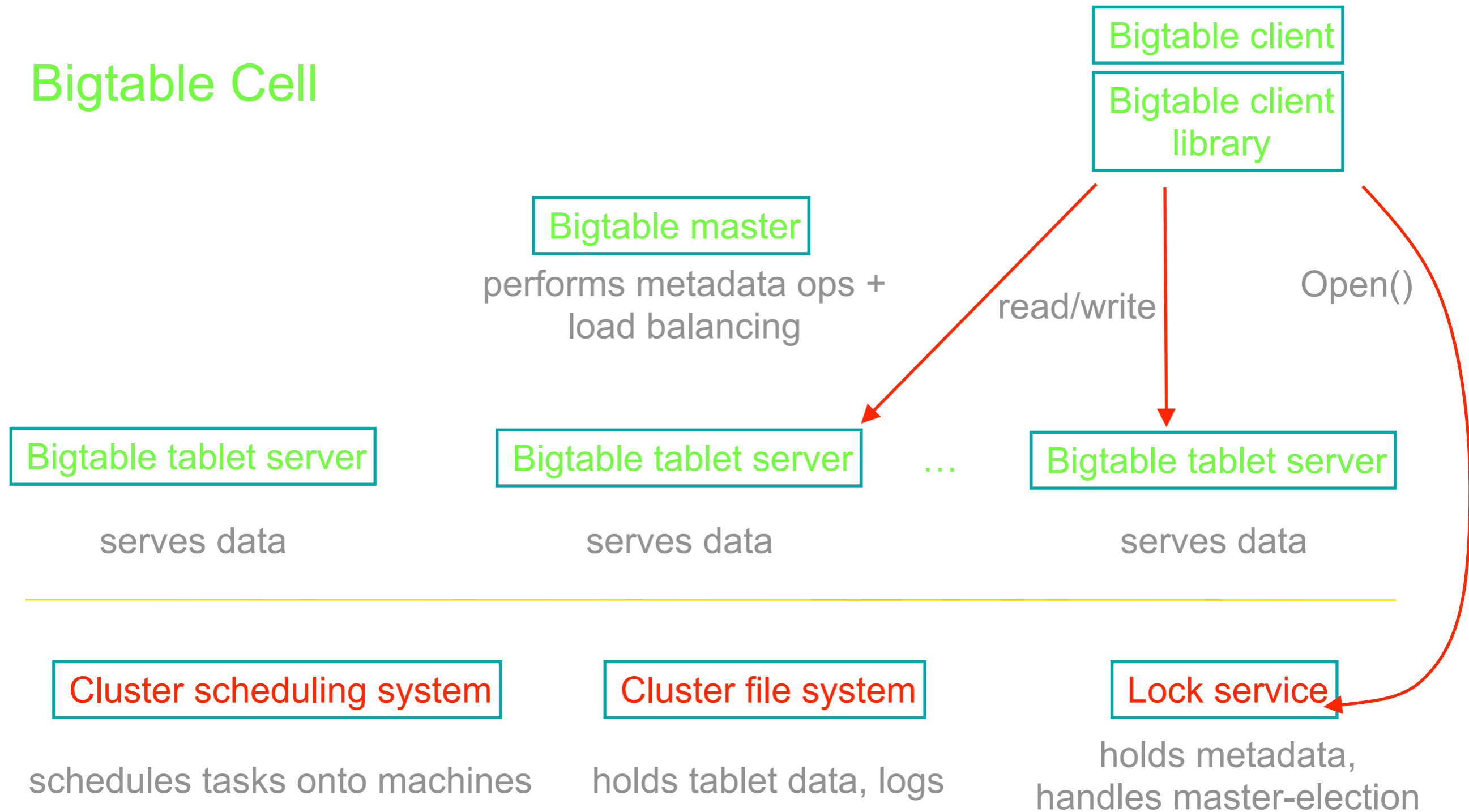
BigTable System Structure

Bigtable Cell



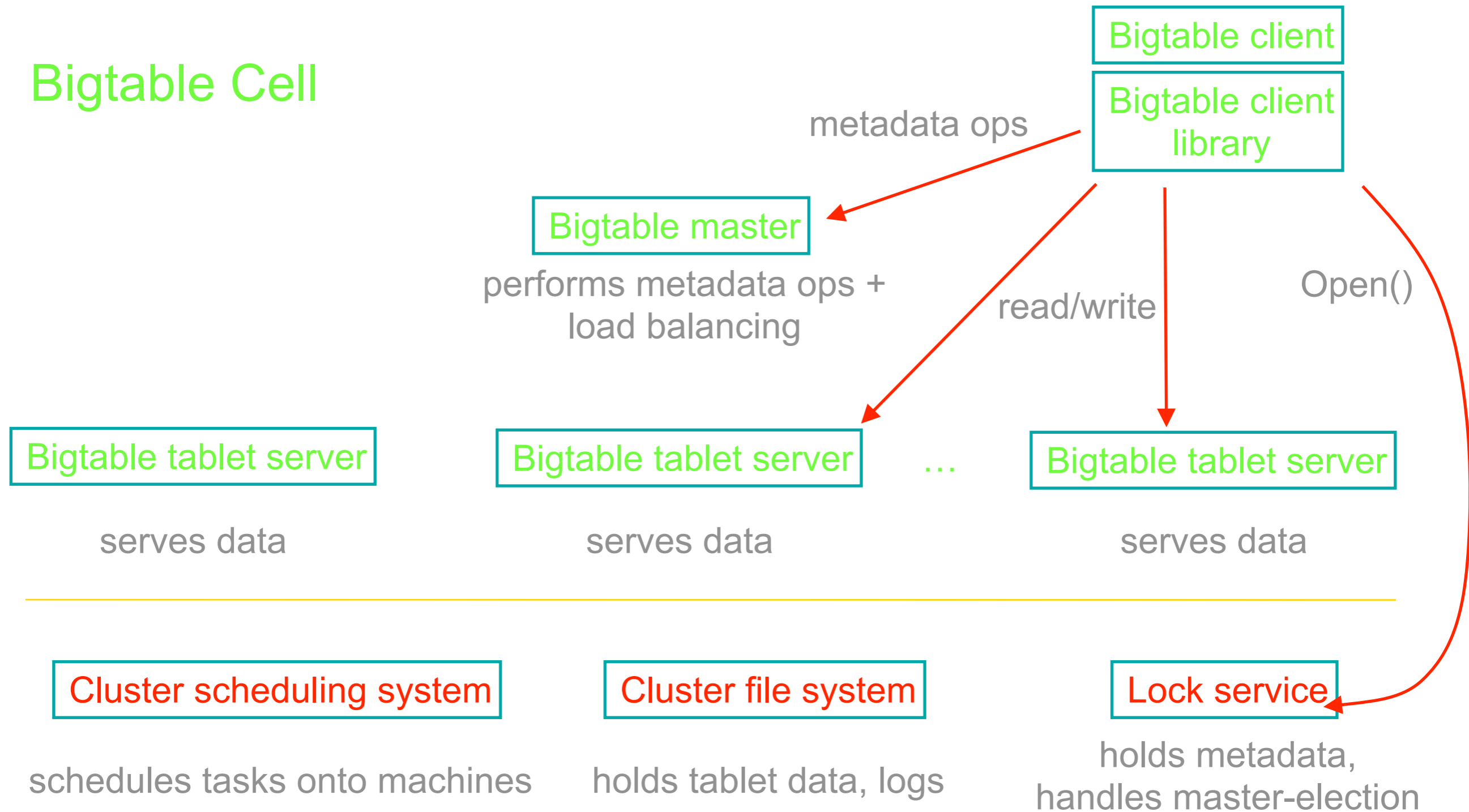
BigTable System Structure

Bigtable Cell



BigTable System Structure

Bigtable Cell



BigTable Status

- Production use for 100s of projects:
 - Crawling/indexing pipeline, Google Maps/Google Earth/Streetview, Search History, Google Print, Google+, Blogger, ...
- Currently 500+ BigTable clusters
- Largest cluster:
 - 100s PB data; sustained: 30M ops/sec; 100+ GB/s I/O
- Many asynchronous processes updating different pieces of information
 - no distributed transactions, no cross-row joins
 - initial design was just in a single cluster
 - follow-on work added eventual consistency across many geographically distributed BigTable instances



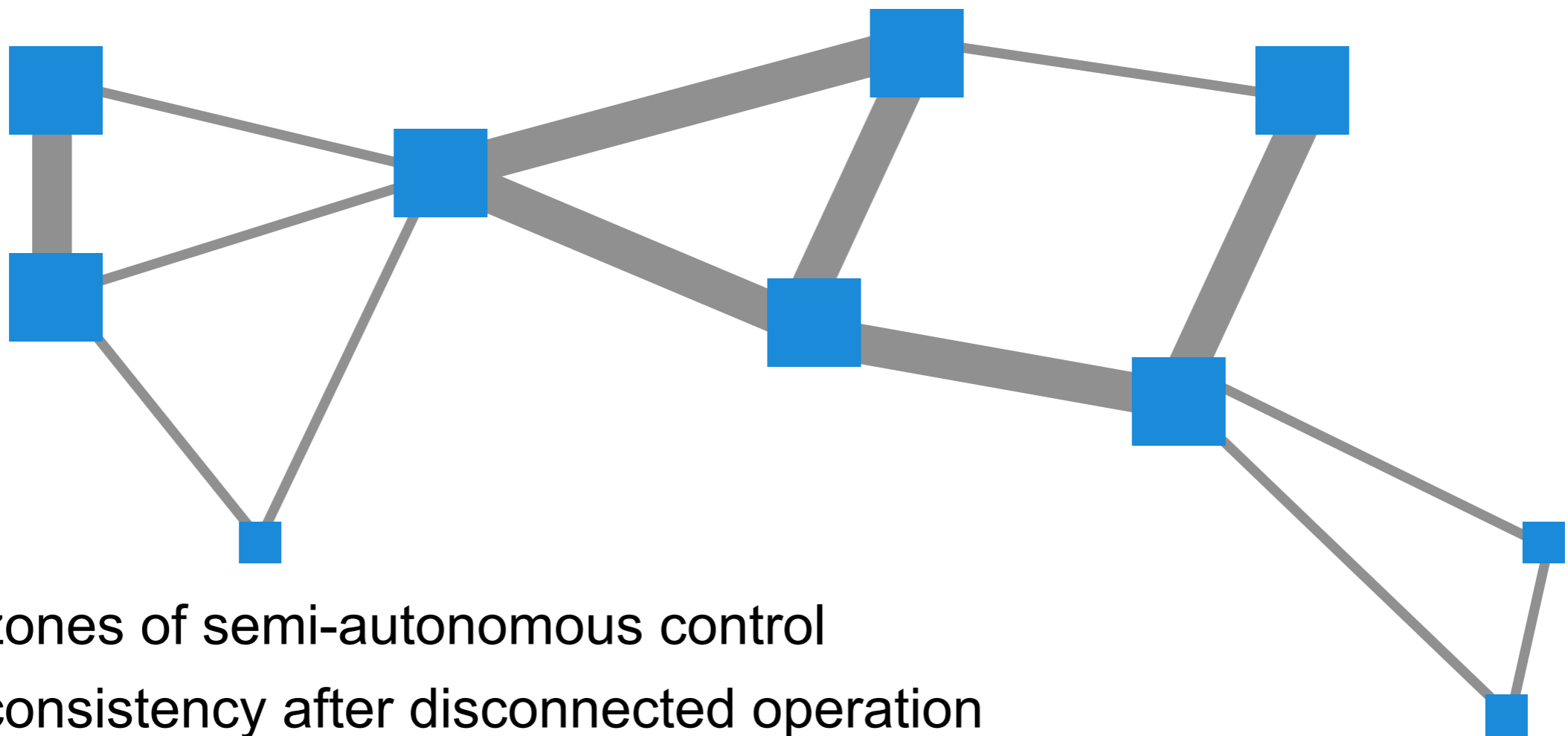
Spanner

- Storage & computation system that runs across many datacenters
 - single global namespace
 - names are independent of location(s) of data
 - **fine-grained replication configurations**
 - support **mix of strong and weak consistency across datacenters**
 - **Strong consistency** implemented with Paxos across tablet replicas
 - Full support for **distributed transactions** across directories/machines
 - much more automated operation
 - automatically changes replication based on constraints and usage patterns
 - automated allocation of resources across entire fleet of machines



Design Goals for Spanner

- Future scale: $\sim 10^5$ to 10^7 machines, $\sim 10^{13}$ directories, $\sim 10^{18}$ bytes of storage, spread at 100s to 1000s of locations around the world



- zones of semi-autonomous control
- consistency after disconnected operation
- users specify high-level desires:
 - “99%ile latency for accessing this data should be <50ms”*
 - “Store this data on at least 2 disks in EU, 2 in U.S. & 1 in Asia”*

Spanner Lessons

- Several variations of eventual client API
- Started to develop with many possible customers in mind, but no particular customer we were working closely with
- Eventually we worked closely with Google ads system as initial customer
 - first real customer was very demanding (real \$\$): good and bad
- Different API than BigTable
 - Harder to move users with existing heavy BigTable usage



Designing & Building Infrastructure

Identify common problems, and build software systems to address them in a general way

- Important to not try to be all things to all people
 - Clients might be demanding 8 different things
 - Doing 6 of them is easy
 - ...handling 7 of them requires real thought
 - ...dealing with all 8 usually results in a worse system
 - more complex, compromises other clients in trying to satisfy everyone

Designing & Building Infrastructure (cont)

Don't build infrastructure just for its own sake:

- Identify common needs and address them
- Don't imagine unlikely potential needs that aren't really there

Best approach: **use your own infrastructure (especially at first!)**

- (much more rapid feedback about what works, what doesn't)

If not possible, at least work very closely with initial client team

- ideally **sit within 50 feet of each other**
- keep other potential clients needs in mind, but **get system working via close collaboration with first client first**

Thanks!

Further reading:

- Ghemawat, Gobioff, & Leung. *Google File System*, SOSP 2003.
- Barroso, Dean, & Hölzle. *Web Search for a Planet: The Google Cluster Architecture*, IEEE Micro, 2003.
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- Chang, Dean, Ghemawat, Hsieh, Wallach, Burrows, Chandra, Fikes, & Gruber. *Bigtable: A Distributed Storage System for Structured Data*, OSDI 2006.
- Corbett et al. *Spanner: Google's Globally Distributed Database*, OSDI 2012.
- Burrows. *The Chubby Lock Service for Loosely-Coupled Distributed Systems*. OSDI 2006.
- Pinheiro, Weber, & Barroso. *Failure Trends in a Large Disk Drive Population*. FAST 2007.
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- Schroeder, Pinheiro, & Weber. *DRAM Errors in the Wild: A Large-Scale Field Study*. SEGMENTRICS'09.
- Protocol Buffers. <http://code.google.com/p/protobuf/>

See: <http://research.google.com/papers.html>

<http://research.google.com/people/jeff>





Challenges in Building Large-Scale Information Retrieval Systems

Jeff Dean

Google Senior Fellow

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Why Work on Retrieval Systems?

- Challenging blend of science and engineering
 - Many interesting, unsolved problems
 - Spans many areas of CS:
 - architecture, distributed systems, algorithms, compression, information retrieval, machine learning, UI, etc.
 - Scale far larger than most other systems
- Small teams can create systems used by hundreds of millions

Retrieval System Dimensions

- Must balance engineering tradeoffs between:
 - number of documents indexed
 - queries / sec
 - index freshness/update rate
 - query latency
 - information kept about each document
 - complexity/cost of scoring/retrieval algorithms
- Engineering difficulty roughly equal to the product of these parameters
- All of these affect overall performance, and performance per \$

1999 vs. 2014

- # docs: ~70M to many billion **~100X**
- queries processed/day: **~1000X**
- per doc info in index: **~3X**
- update latency: months to minutes **~10000X**
- avg. query latency: <1s to <0.15s **~6X**

- More machines * faster machines: **~1000X**

Constant Change

- Parameters change over time
 - often by many orders of magnitude
- Right design at X may be very wrong at $10X$ or $100X$
 - ... design for $\sim 10X$ growth, but plan to rewrite before $\sim 100X$
- Continuous evolution:
 - 7 significant revisions in last 10 years
 - often rolled out without users realizing we've made major changes

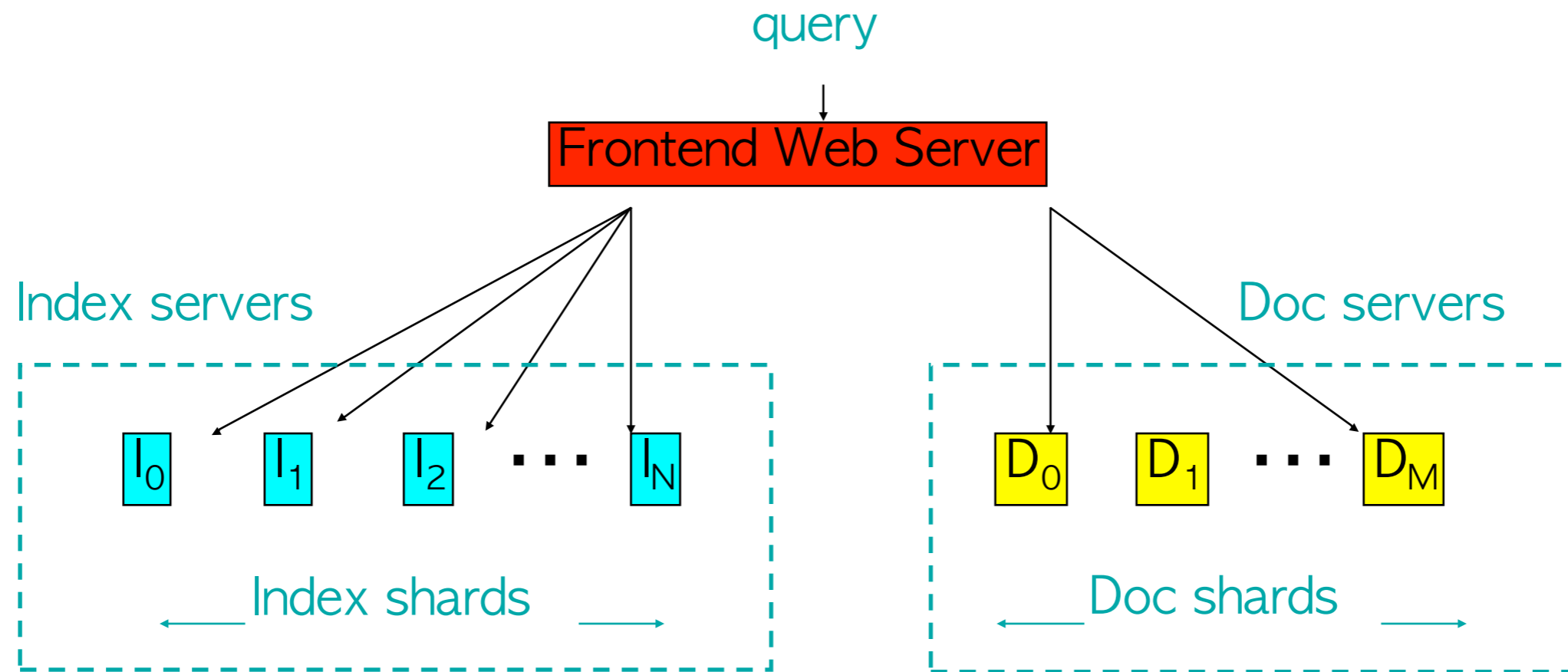
Rest of Talk

- Evolution of Google's search systems
 - several gens of crawling/indexing/serving systems
 - brief description of supporting infrastructure
 - Joint work with many, many people
- Interesting directions and challenges

“Google” Circa 1997 (google.stanford.edu)



Research Project, circa 1997



Ways of Index Partitioning

- **By doc:** each shard has index for subset of docs
 - pro: each shard can process queries independently
 - pro: easy to keep additional per-doc information
 - pro: network traffic (requests/responses) small
 - con: query has to be processed by each shard
 - con: $O(K*N)$ disk seeks for K word query on N shards

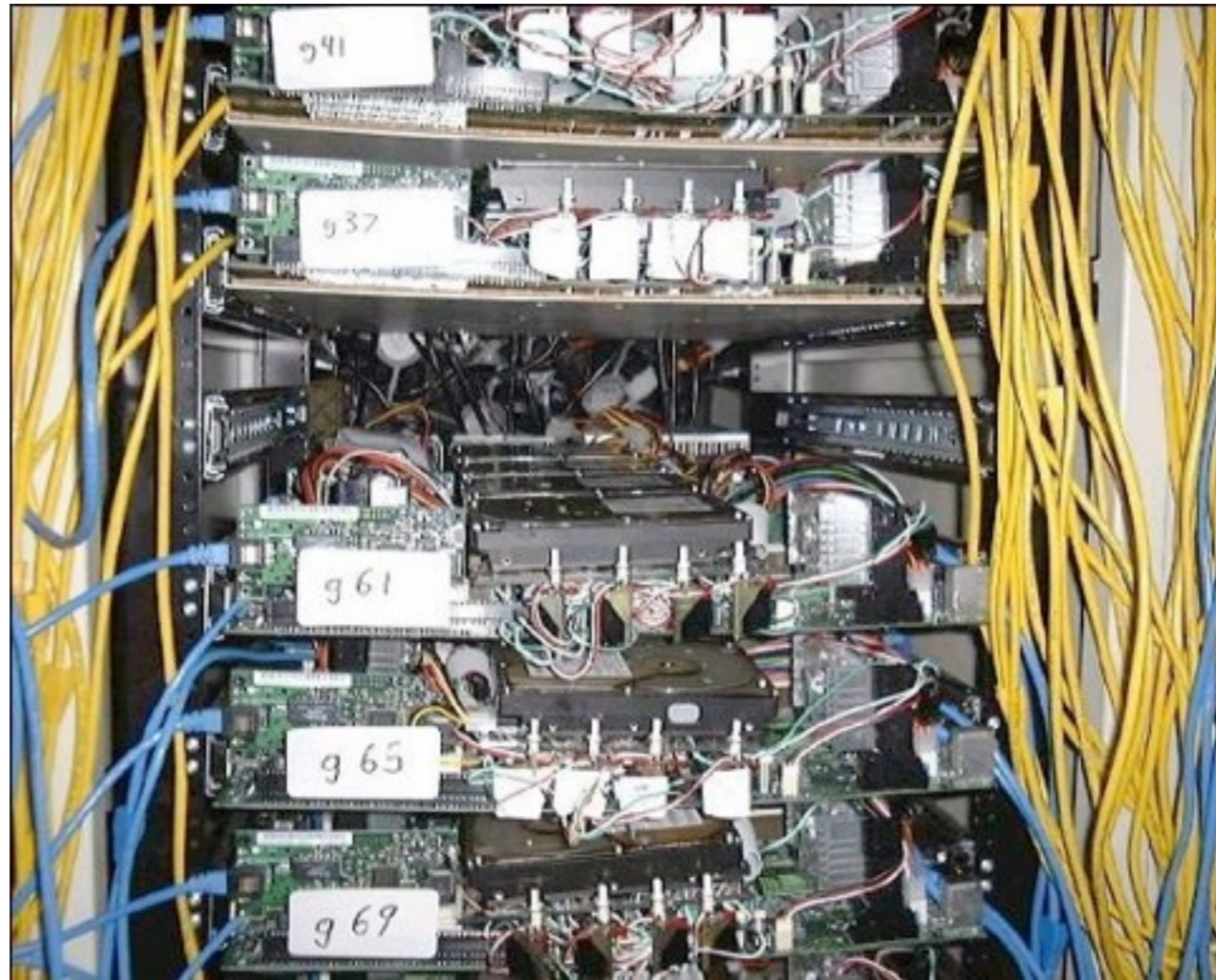
In our computing environment, **by doc makes more sense**

- **By word:** shard has subset of words for all docs
 - pro: K word query => handled by at most K shards
 - pro: $O(K)$ disk seeks for K word query
 - con: much higher network bandwidth needed
 - data about each word for each matching doc must be collected in one place
 - con: harder to have per-doc information

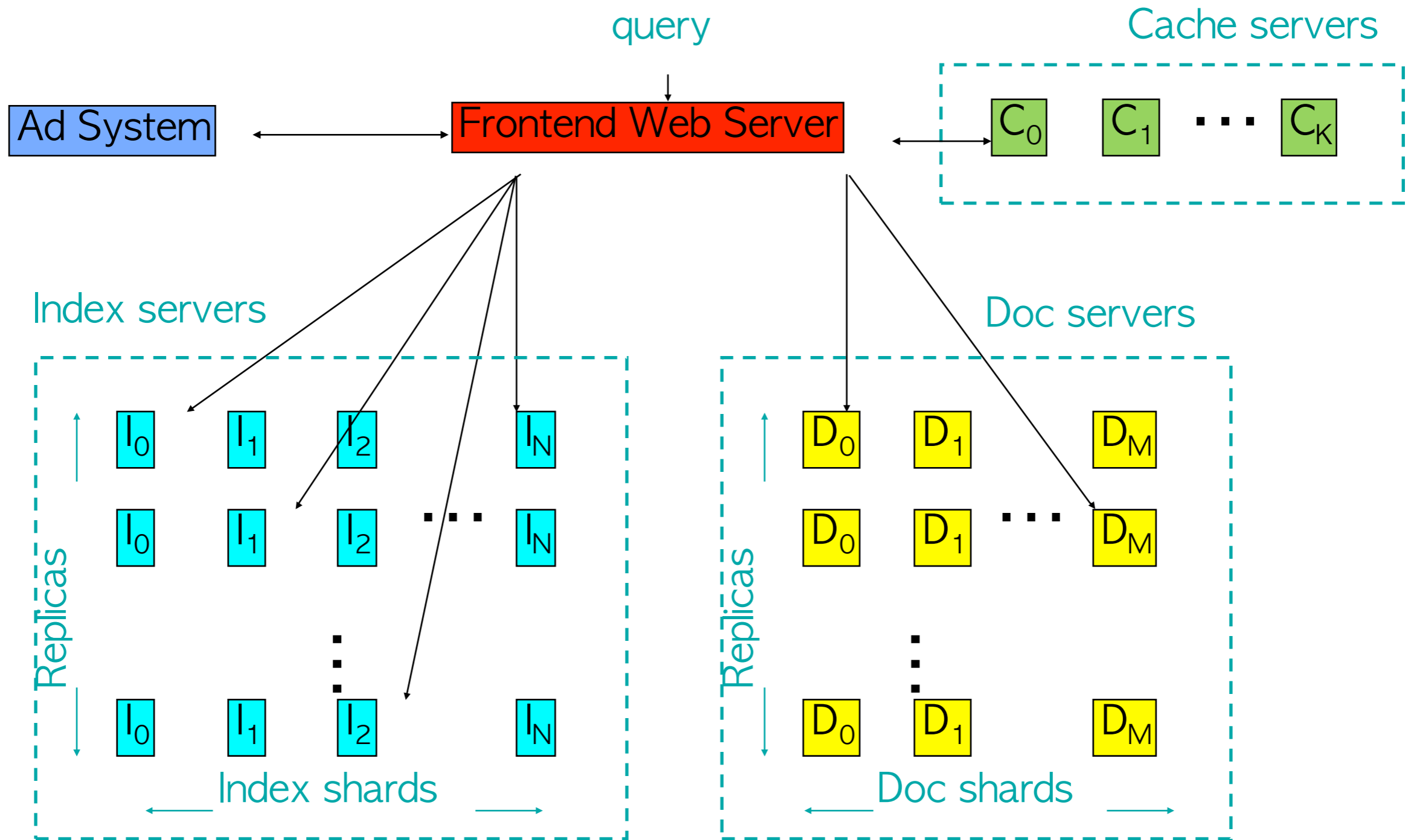
Basic Principles

- Documents assigned small integer ids (docids)
 - good if smaller for higher quality/more important docs
- Index Servers:
 - given (query) return sorted list of (score, docid, ...)
 - partitioned (“sharded”) by docid
 - index shards are replicated for capacity
 - cost is $O(\# \text{ queries} * \# \text{ docs in index})$
- Doc Servers
 - given (docid, query) generate (title, snippet)
 - map from docid to full text of docs on disk
 - also partitioned by docid
 - cost is $O(\# \text{ queries})$

“Corkboards” (1999)



Serving System, circa 1999



Caching

- Cache servers:
 - cache both index results and doc snippets
 - hit rates typically 30-60%
 - depends on frequency of index updates, mix of query traffic, level of personalization, etc
- Main benefits:
 - **performance!** 10s of machines do work of 100s or 1000s
 - reduce query latency on hits
 - queries that hit in cache tend to be both popular and expensive (common words, lots of documents to score, etc.)
- Beware: **big latency spike/capacity drop when index updated or cache flushed**

Crawling (circa 1998-1999)

- Simple batch crawling system
 - start with a few URLs
 - crawl pages
 - extract links, add to queue
 - stop when you have enough pages
- Concerns:
 - don't hit any site too hard
 - prioritizing among uncrawled pages
 - one way: continuously compute PageRank on changing graph
 - maintaining uncrawled URL queue efficiently
 - one way: keep in a partitioned set of servers
 - dealing with machine failures

Indexing (circa 1998-1999)

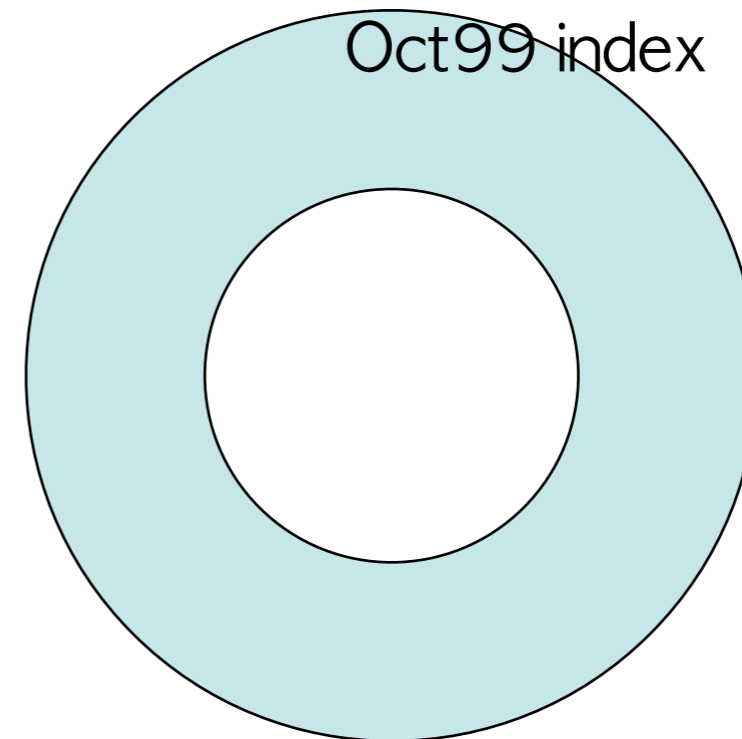
- Simple batch indexing system
 - Based on simple unix tools
 - No real checkpointing, so machine failures painful
 - No checksumming of raw data, so hardware bit errors caused problems
 - Exacerbated by early machines having no ECC, no parity
 - Sort 1 TB of data without parity: ends up "mostly sorted"
 - Sort it again: "mostly sorted" another way
- “Programming with adversarial memory”
 - Led us to develop a file abstraction that stored checksums of small records and could skip and resynchronize after corrupted records

Index Updates (circa 1998-1999)

- 1998-1999: Index updates (~once per month):
 - Wait until traffic is low
 - Take some replicas offline
 - Copy new index to these replicas
 - Start new frontends pointing at updated index and serve some traffic from there

Index Updates (circa 1998-1999)

- Index server disk:
 - outer part of disk gives higher disk bandwidth



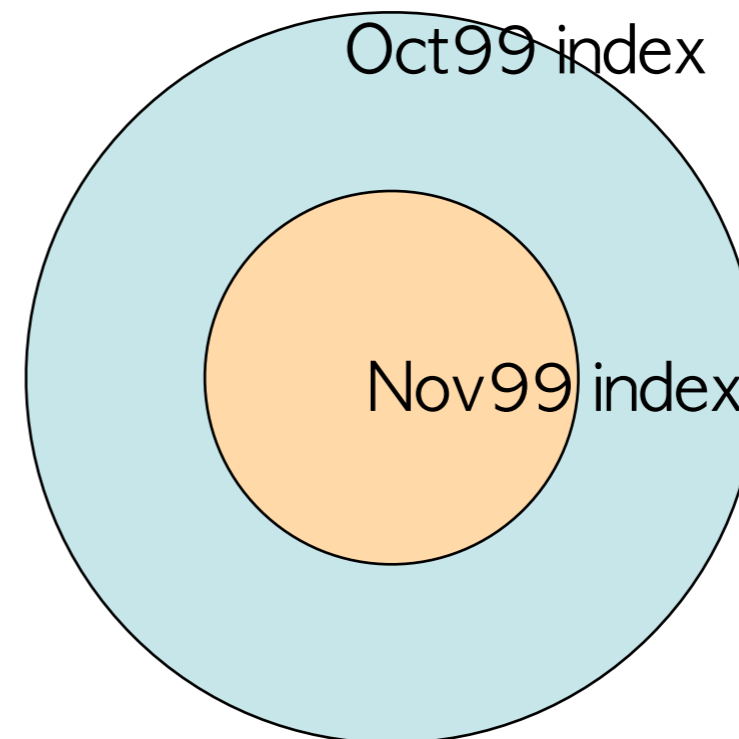
Index Updates (circa 1998-1999)

- Index server disk:

- outer part of disk gives higher disk bandwidth

1. Copy new index to inner half of disk
(while still serving old index)

2. Restart to use new index

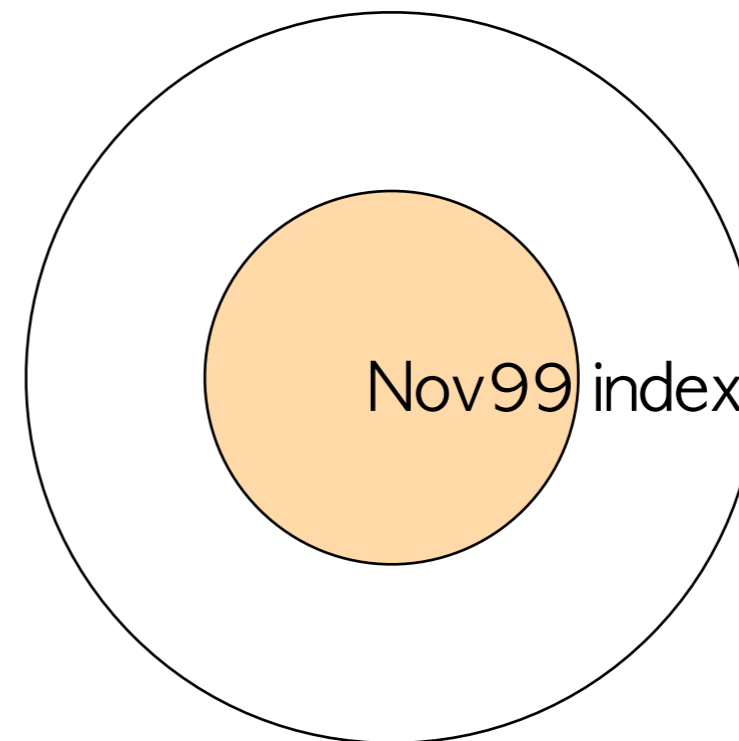


Index Updates (circa 1998-1999)

- Index server disk:

- outer part of disk gives higher disk bandwidth

1. Copy new index to inner half of disk
(while still serving old index)
2. Restart to use new index
3. Wipe old index

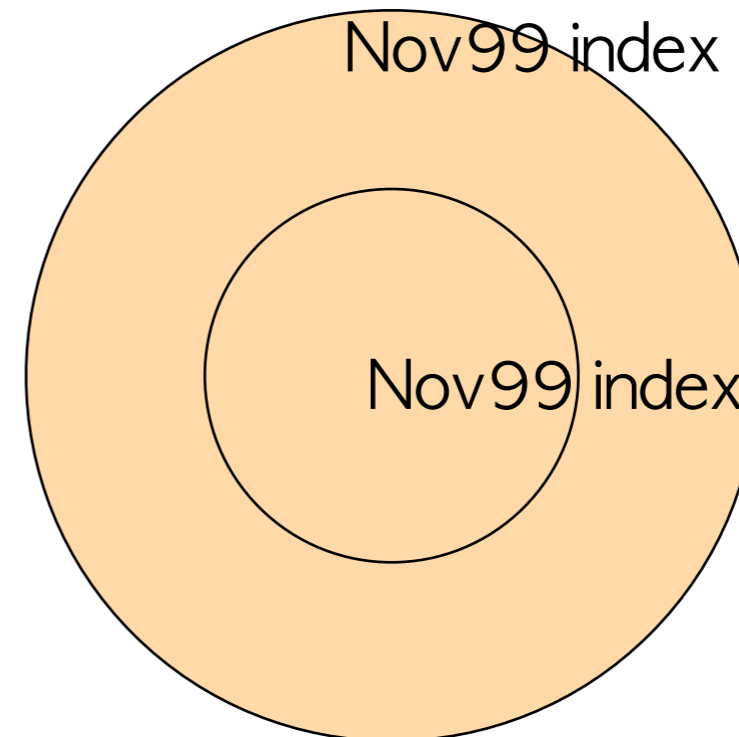


Index Updates (circa 1998-1999)

- Index server disk:

- outer part of disk gives higher disk bandwidth

1. Copy new index to inner half of disk
(while still serving old index)
2. Restart to use new index
3. Wipe old index
4. Re-copy new index to faster half of disk

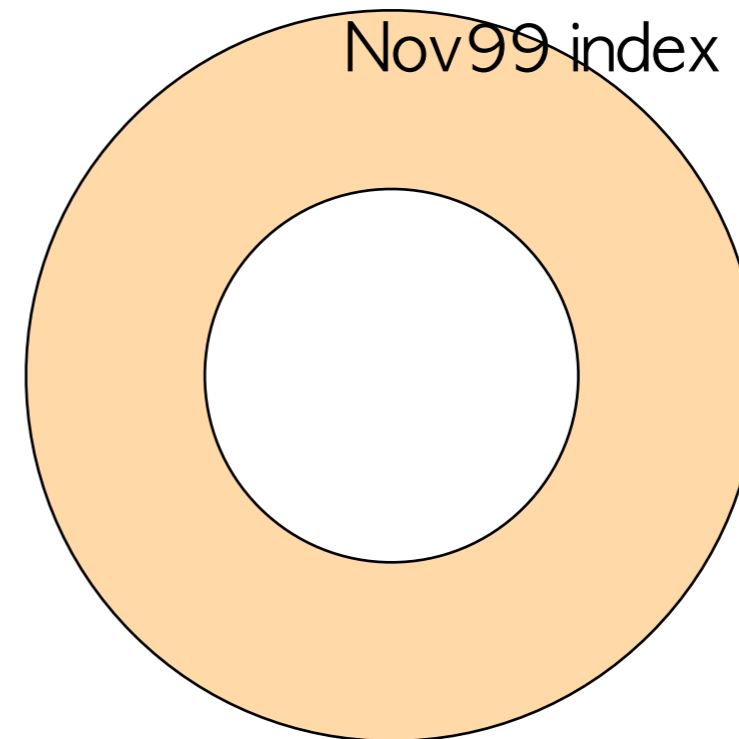


Index Updates (circa 1998-1999)

- Index server disk:

- outer part of disk gives higher disk bandwidth

1. Copy new index to inner half of disk (while still serving old index)
2. Restart to use new index
3. Wipe old index
4. Re-copy new index to faster half of disk
5. Wipe first copy of new index

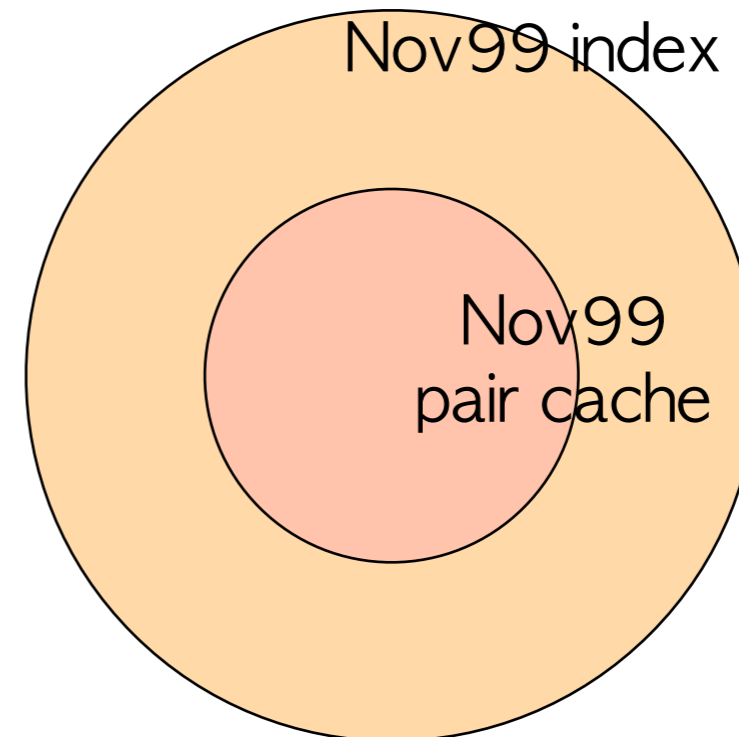


Index Updates (circa 1998-1999)

- **Index server disk:**

- outer part of disk gives higher disk bandwidth

1. Copy new index to inner half of disk (while still serving old index)
2. Restart to use new index
3. Wipe old index
4. Re-copy new index to faster half of disk
5. Wipe first copy of new index
6. Inner half now free for building various performance improving data structures



Pair cache: pre-intersected pairs of posting lists for commonly co-occurring query terms (e.g. “new” and “york”, or “barcelona” and “restaurants”)

Google Data Center (2000)



Google (new data center 2001)



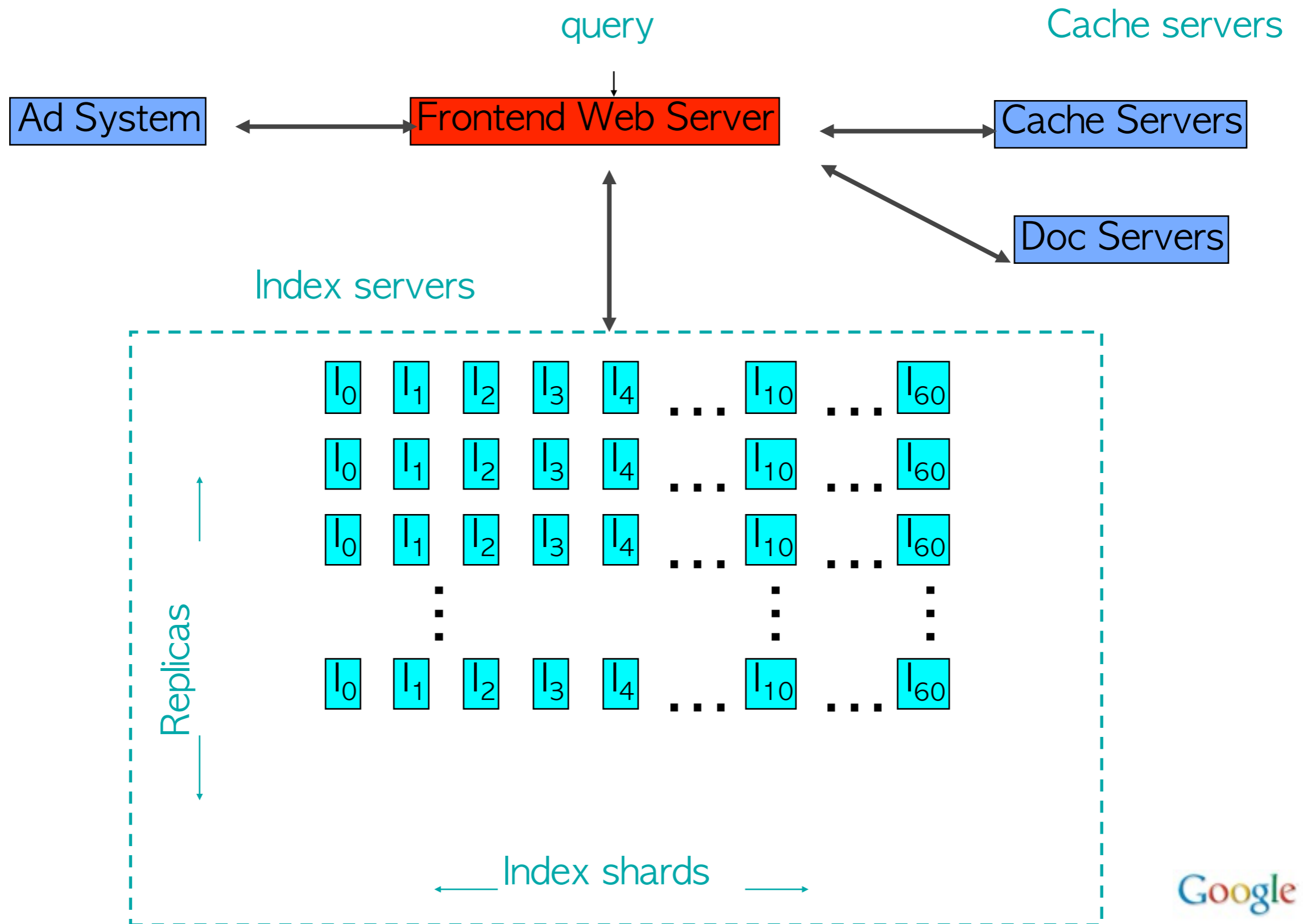
Google Data Center (3 days later)



Increasing Index Size and Query Capacity

- Huge increases in index size in '99, '00, '01, ...
 - From ~50M pages to more than 1000M pages
- At same time as huge traffic increases
 - ~20% growth per month in 1999, 2000, ...
 - ... plus major new partners (e.g. Yahoo in July 2000 doubled traffic overnight)
- Performance of index servers was paramount
 - Deploying more machines continuously, but...
 - Needed ~10-30% software-based improvement every month

Dealing with Growth



Implications

- Shard response time influenced by:
 - # of disk seeks that must be done
 - amount of data to be read from disk
- Big performance improvements possible with:
 - better disk scheduling
 - improved index encoding

Index Encoding circa 1997-1999

- Original encoding ('97) was very simple:

WORD → docid+nhits:32b hit: 16b hit: 16b ... docid+nhits:32b hit: 16b

- hit: position plus attributes (font size, title, etc.)

- Eventually added skip tables for large posting lists

- Simple, byte aligned format

- cheap to decode, but not very compact

- ... required lots of disk bandwidth

Encoding Techniques

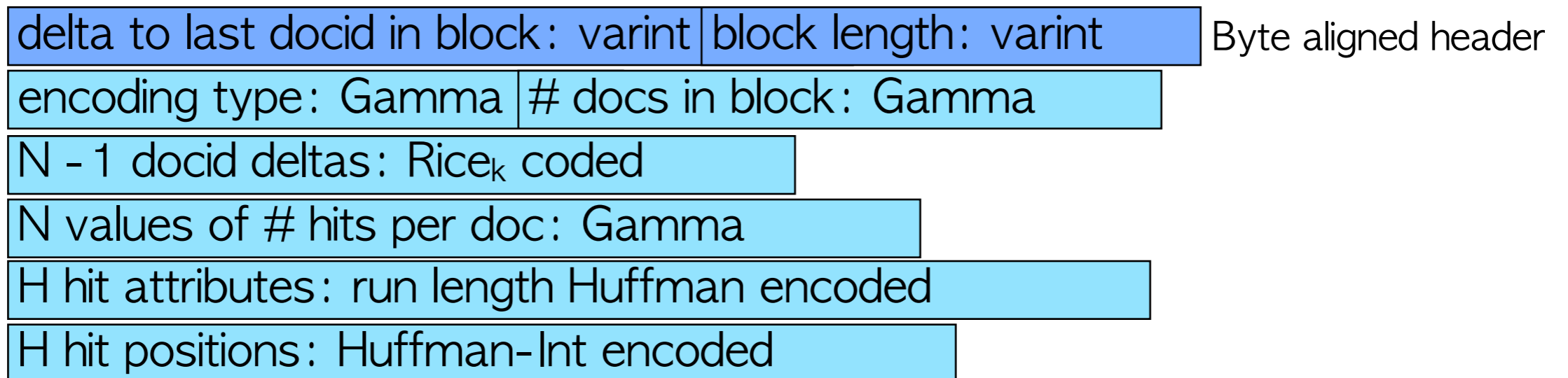
- Bit-level encodings:
 - **Unary**: N '1's followed by a '0'
 - **Gamma**: $\log_2(N)$ in unary, then $\text{floor}(\log_2(N))$ bits
 - **Rice_K**: $\text{floor}(N / 2^K)$ in unary, then $N \bmod 2^K$ in K bits
 - special case of **Golomb** codes where base is power of 2
 - **Huffman-Int**: like Gamma, except $\log_2(N)$ is Huffman coded instead of encoded w/ Unary
- Byte-aligned encodings:
 - **varint**: 7 bits per byte with a continuation bit
 - 0-127: 1 byte, 128-4095: 2 bytes, ...
 - ...

Block-Based Index Format

- Block-based, variable-len format reduced both space and CPU



Block format (with N documents and H hits):

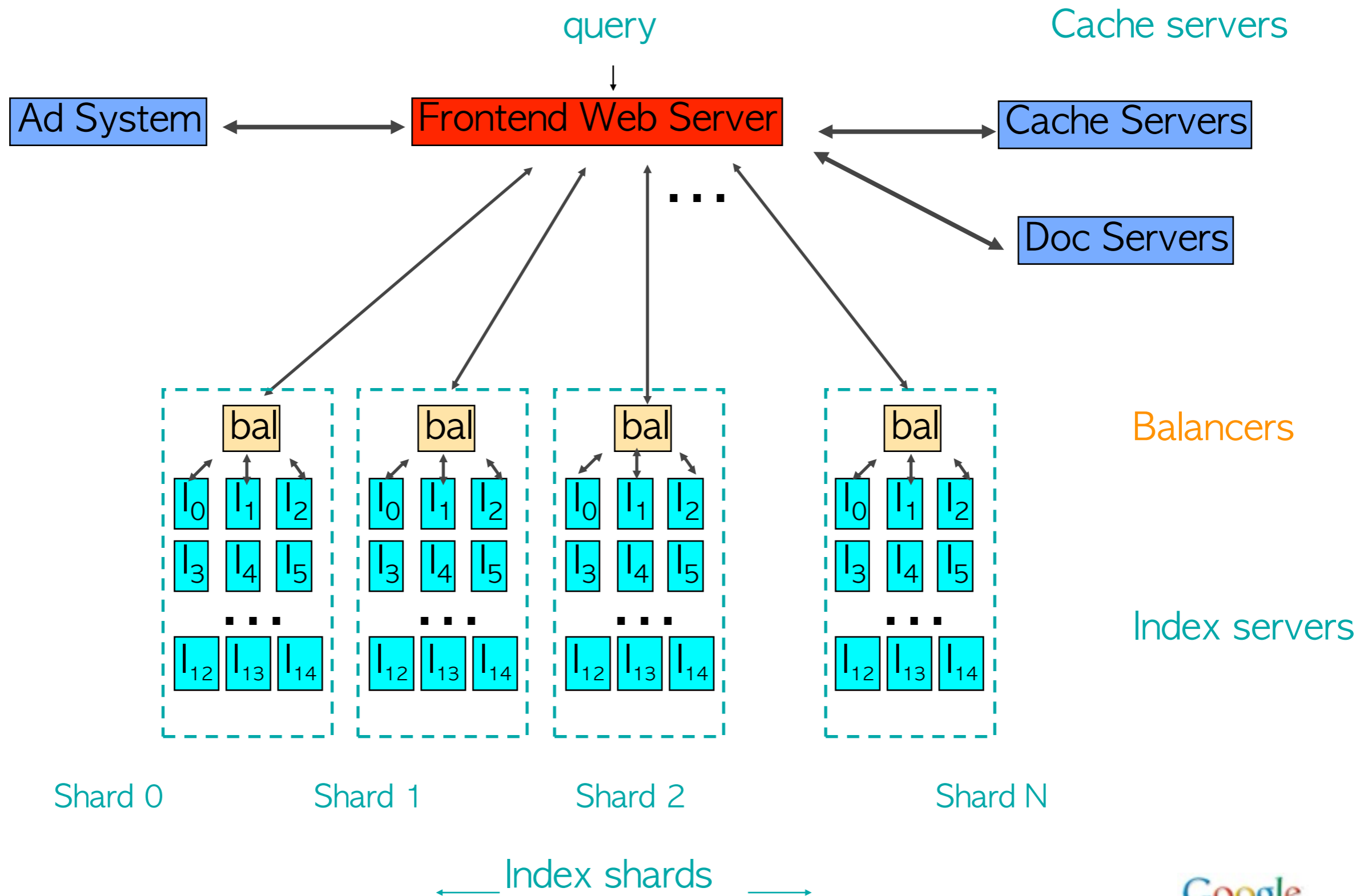


- Reduced index size by ~30%, plus much faster to decode

Implications of Ever-Wider Sharding

- Must add shards to keep response time low as index size increases
- ... but query cost increases with # of shards
 - typically ≥ 1 disk seek / shard / query term
 - even for very rare terms
- As # of replicas increases, total amount of memory available increases
 - Eventually, have enough memory to hold an **entire copy of the index in memory**
 - radically changes many design parameters

Early 2001: In-Memory Index



In-Memory Indexing Systems

- Many positives:
 - big increase in throughput
 - big decrease in latency
 - especially at the tail: expensive queries that previously needed GBs of disk I/O became much faster
 - e.g. ["circle of life"]
- Some issues:
 - Variance**: touch 1000s of machines, not dozens
 - e.g. randomized cron jobs caused us trouble for a while
 - Availability**: 1 or few replicas of each doc's index data
 - Queries of death that kill all the backends at once: **very bad**
 - Availability of index data when machine failed (esp for important docs):
replicate important docs

Google's Computational Environment Today

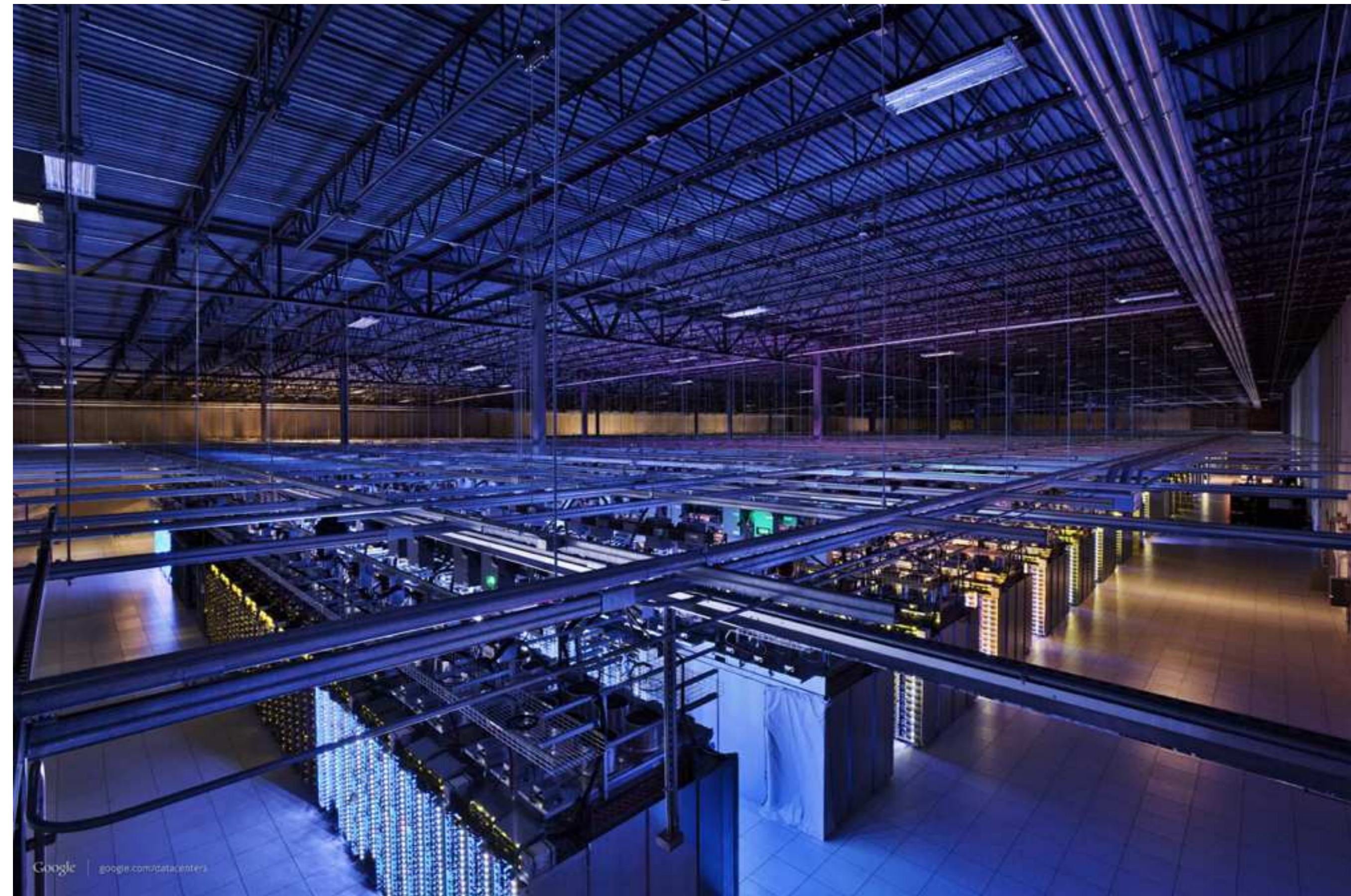
- Many datacenters around the world



Zooming In...



Zooming In...



Lots of machines...



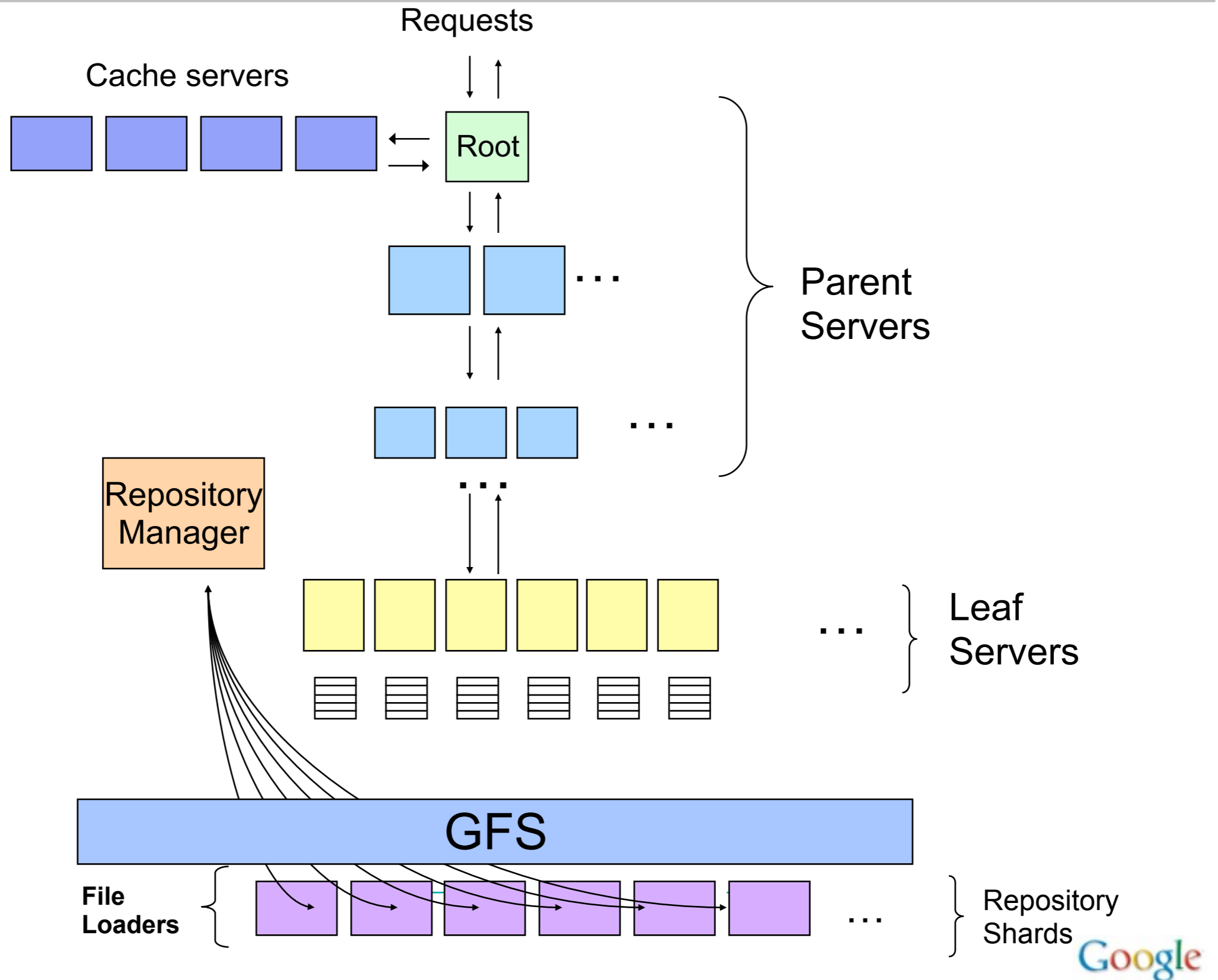
Save a bit of power: turn out the lights...



Cool..



Serving Design, 2004 edition



New Index Format

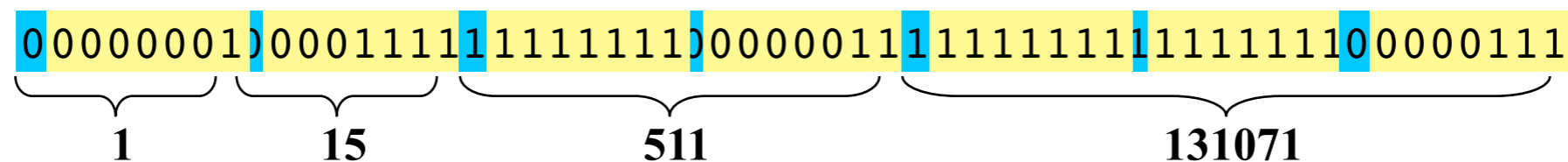
- **Block index format used two-level scheme:**
 - Each hit was encoded as (docid, word position in doc) pair
 - Docid deltas encoded with Rice encoding
 - Very good compression (originally designed for disk-based indices), but slow/CPU-intensive to decode
- **New format: single flat position space**
 - Data structures on side keep track of doc boundaries
 - Posting lists are just lists of delta-encoded positions
 - Need to be compact (can't afford 32 bit value per occurrence)
 - ... but need to be very fast to decode

Byte-Aligned Variable-length Encodings

- Varint encoding:

- 7 bits per byte with continuation bit

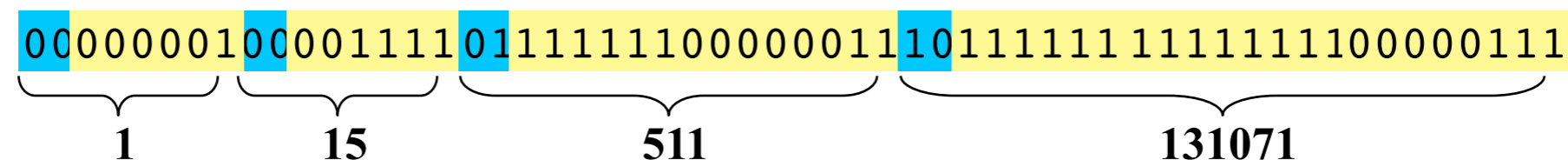
- Con: Decoding requires lots of branches/shifts/masks



- Idea: Encode byte length as low 2 bits

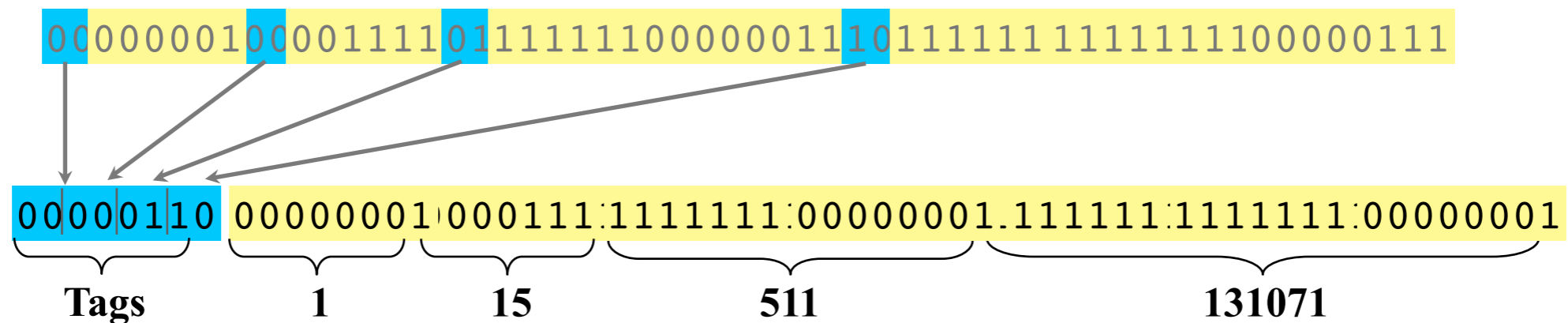
- Better: fewer branches, shifts, and masks

- Con: Limited to 30-bit values, still some shifting to decode

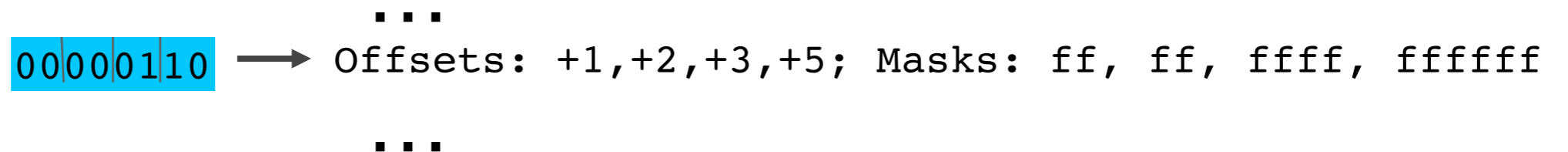


Group Varint Encoding

- Idea: encode groups of 4 values in 5-17 bytes
 - Pull out 4 2-bit binary lengths into single byte prefix

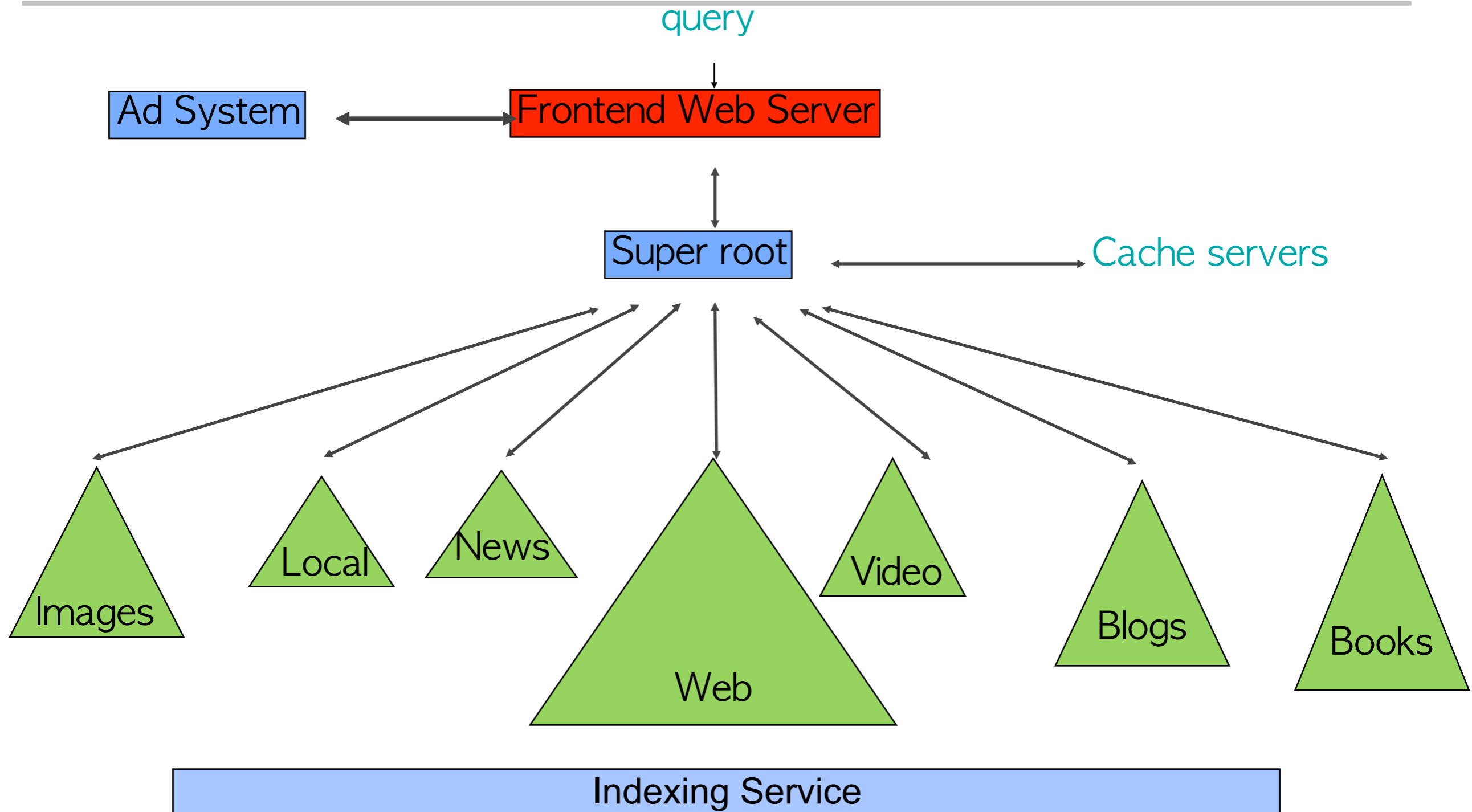


- Decode: Load prefix byte and use value to lookup in 256-entry table:



- Much faster than alternatives:
 - 7-bit-per-byte varint: decode ~180M numbers/second
 - 30-bit Varint w/ 2-bit length: decode ~240M numbers/second
 - Group varint: decode ~400M numbers/second

2007: Universal Search



Index that? Just a minute!

- Low-latency crawling and indexing is tough
 - crawl heuristics: what pages should be crawled?
 - crawling system: need to crawl pages quickly
 - indexing system: depends on global data
 - PageRank, anchor text of pages that point to the page, etc.
 - must have online approximations for these global properties
 - serving system: must be prepared to accept updates while serving requests
 - very different data structures than batch update serving system

Often use hybrid systems (1+2):

1. Very fast update system, but with modest capacity (high \$\$\$/doc/query)
2. Slower updating system, but with huge capacity and relatively immutable data structures (low \$/doc/query)

Understanding Text

Query

[car parts for sale]

Document 1

... car parking available for a small fee.
... parts of our floor model inventory for sale.

Document 2

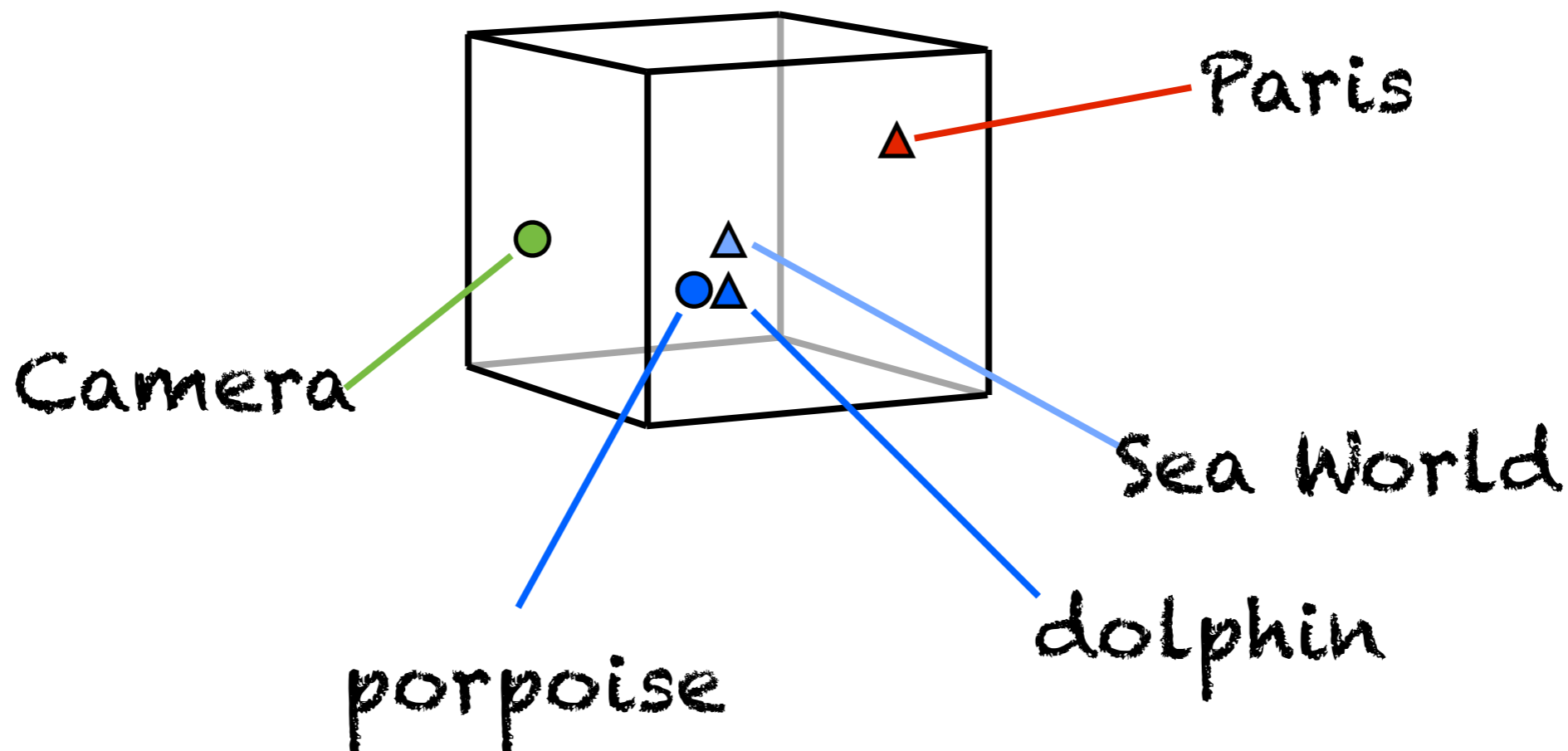
Selling all kinds of automobile and pickup truck parts, engines, and transmissions.



- Embeddings & Neural Nets
- How we use them
- What's next?

N-dimensional Embeddings

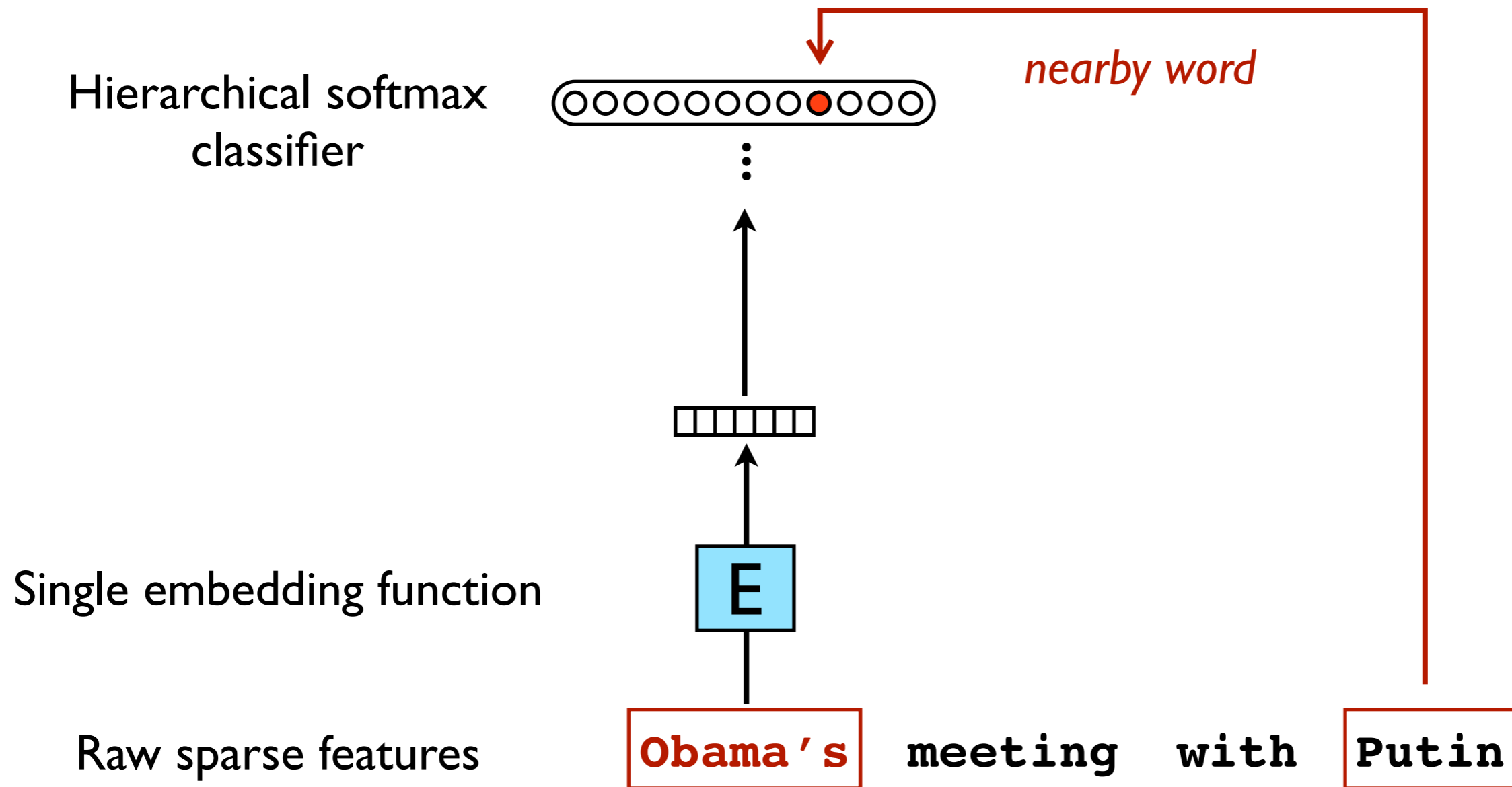
3-D embedding space



Embedding Function: A look-up-table that maps sparse features into dense floating point vectors.

Usually use many more dimensions than 3 (e.g. 1000-D embeddings)

Skipgram Text Model



Mikolov, Chen, Corrado and Dean. *Efficient Estimation of Word Representations in Vector Space*, <http://arxiv.org/abs/1301.3781>

Open source implementation: <https://code.google.com/p/word2vec/>

Nearest neighbors in language embeddings space are closely related semantically.

- Trained language model on Wikipedia corpus.

tiger shark

bull shark
blacktip shark
shark
oceanic whitetip shark
sandbar shark
dusky shark
blue shark
requiem shark
great white shark
lemon shark

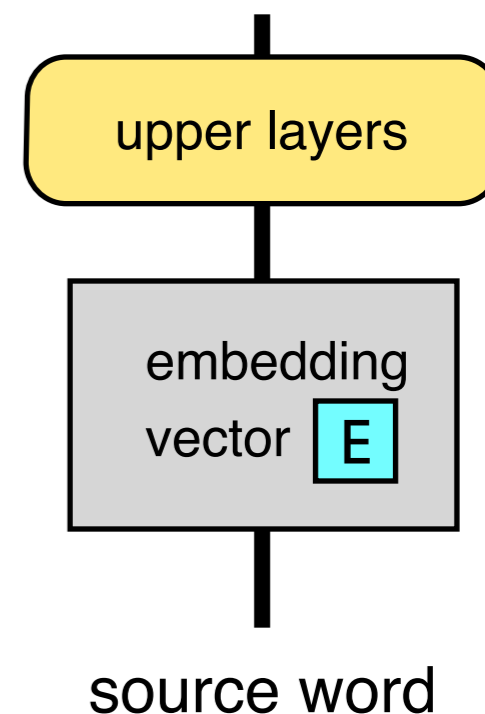
car

cars
muscle car
sports car
compact car
autocar
automobile
pickup truck
racing car
passenger car
dealership

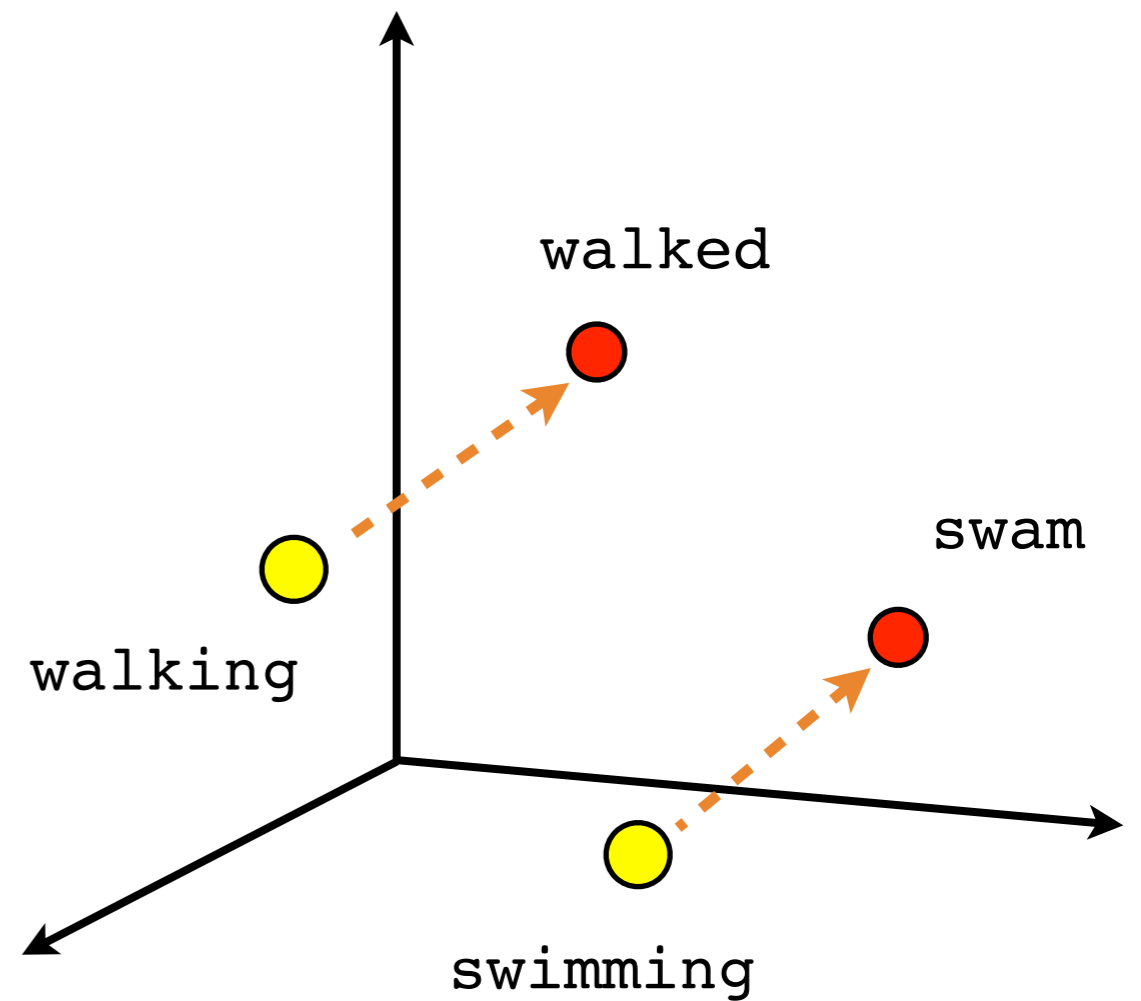
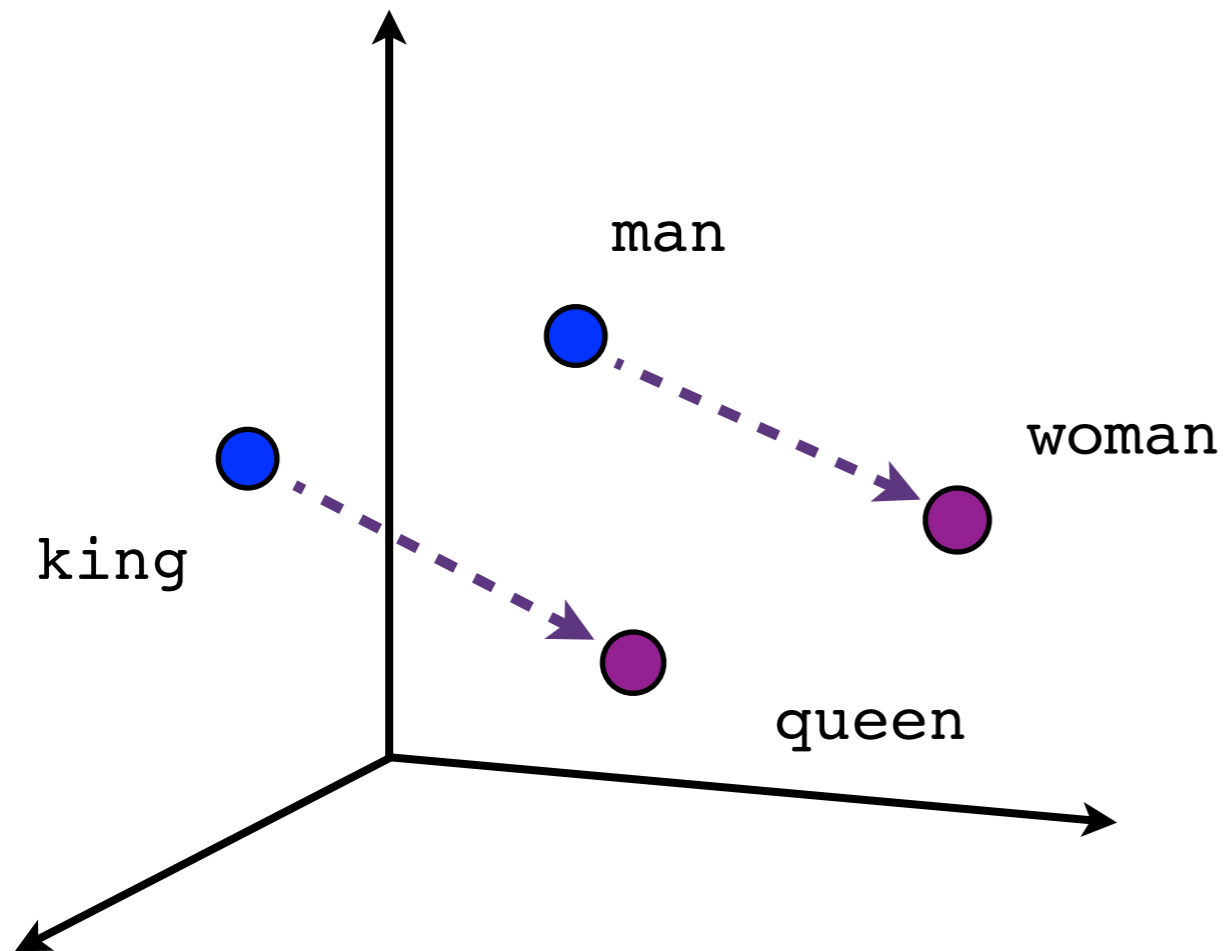
new york

new york city
brooklyn
long island
syracuse
manhattan
washington
bronx
yonkers
poughkeepsie
new york state

nearby words



Embeddings are Powerful





Solving Analogies

- Embedding vectors trained for the language modeling task have very interesting properties (especially the skip-gram model).

$$E(\textit{hotter}) - E(\textit{hot}) \approx E(\textit{bigger}) - E(\textit{big})$$

$$E(\textit{Rome}) - E(\textit{Italy}) \approx E(\textit{Berlin}) - E(\textit{Germany})$$



Solving Analogies

- Embedding vectors trained for the language modeling task have very interesting properties (especially the skip-gram model).

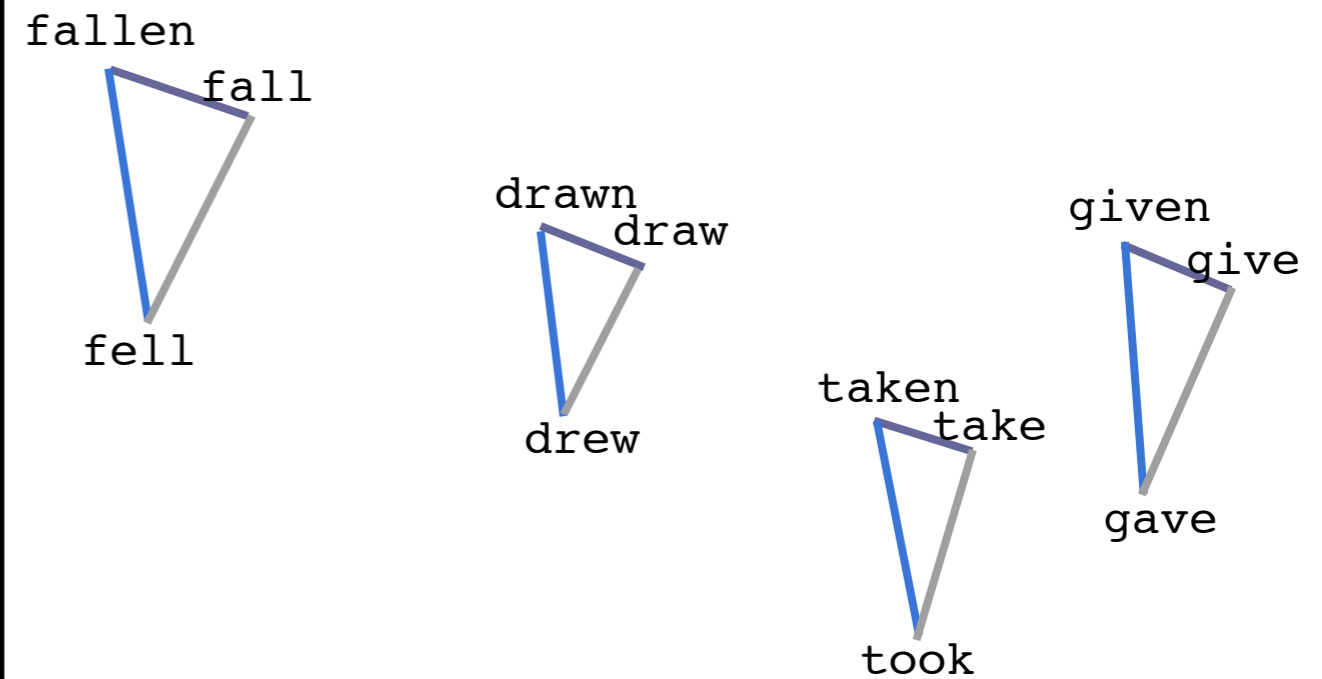
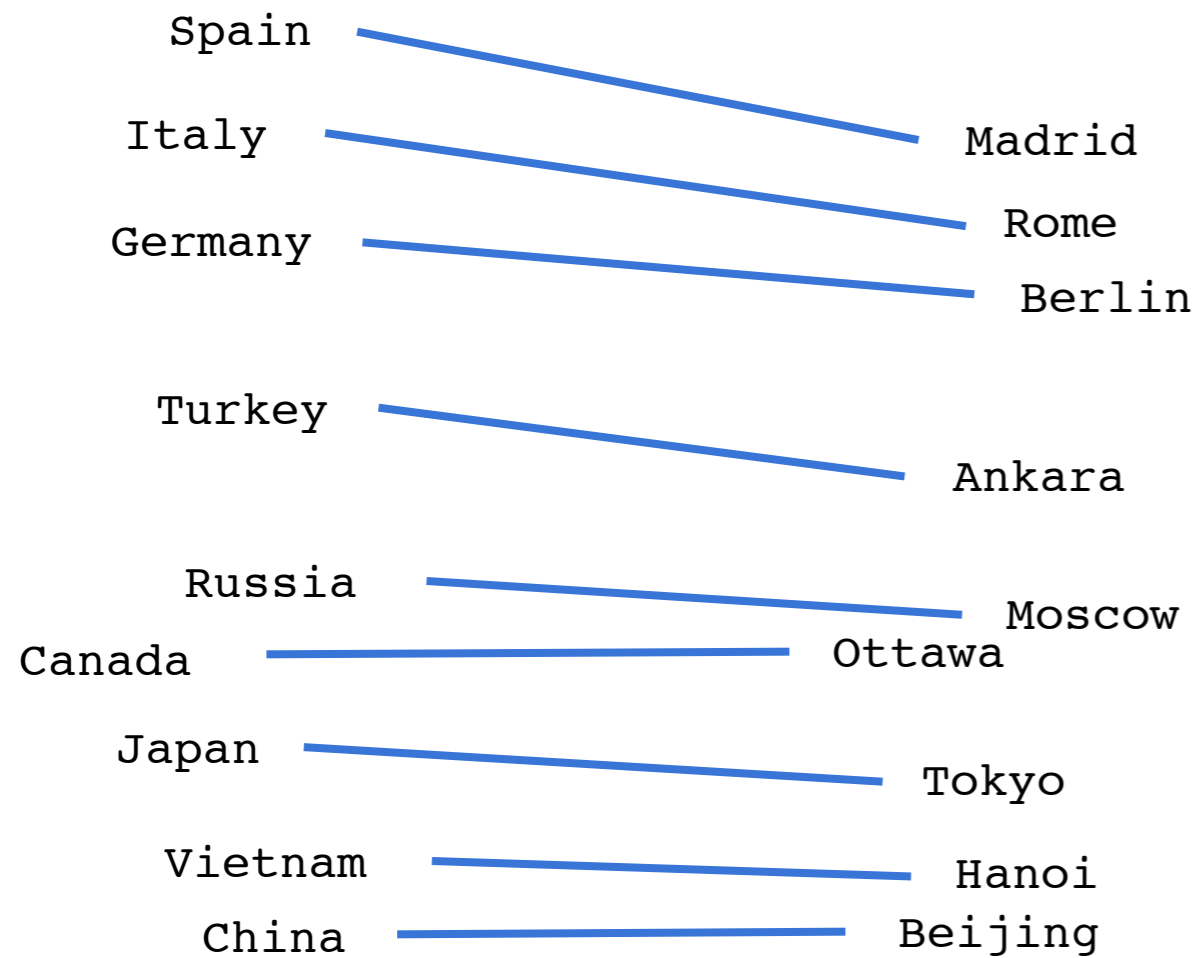
$$E(\textit{hotter}) - E(\textit{hot}) + E(\textit{big}) \approx E(\textit{bigger})$$

$$E(\textit{Rome}) - E(\textit{Italy}) + E(\textit{Germany}) \approx E(\textit{Berlin})$$

Skip-gram model w/ 640 dimensions trained on 6B words of news text achieves 57% accuracy for analogy-solving test set.

Details in: *Efficient Estimation of Word Representations in Vector Space*. Mikolov, Chen, Corrado and Dean. NIPS 2013.

Embeddings are Powerful

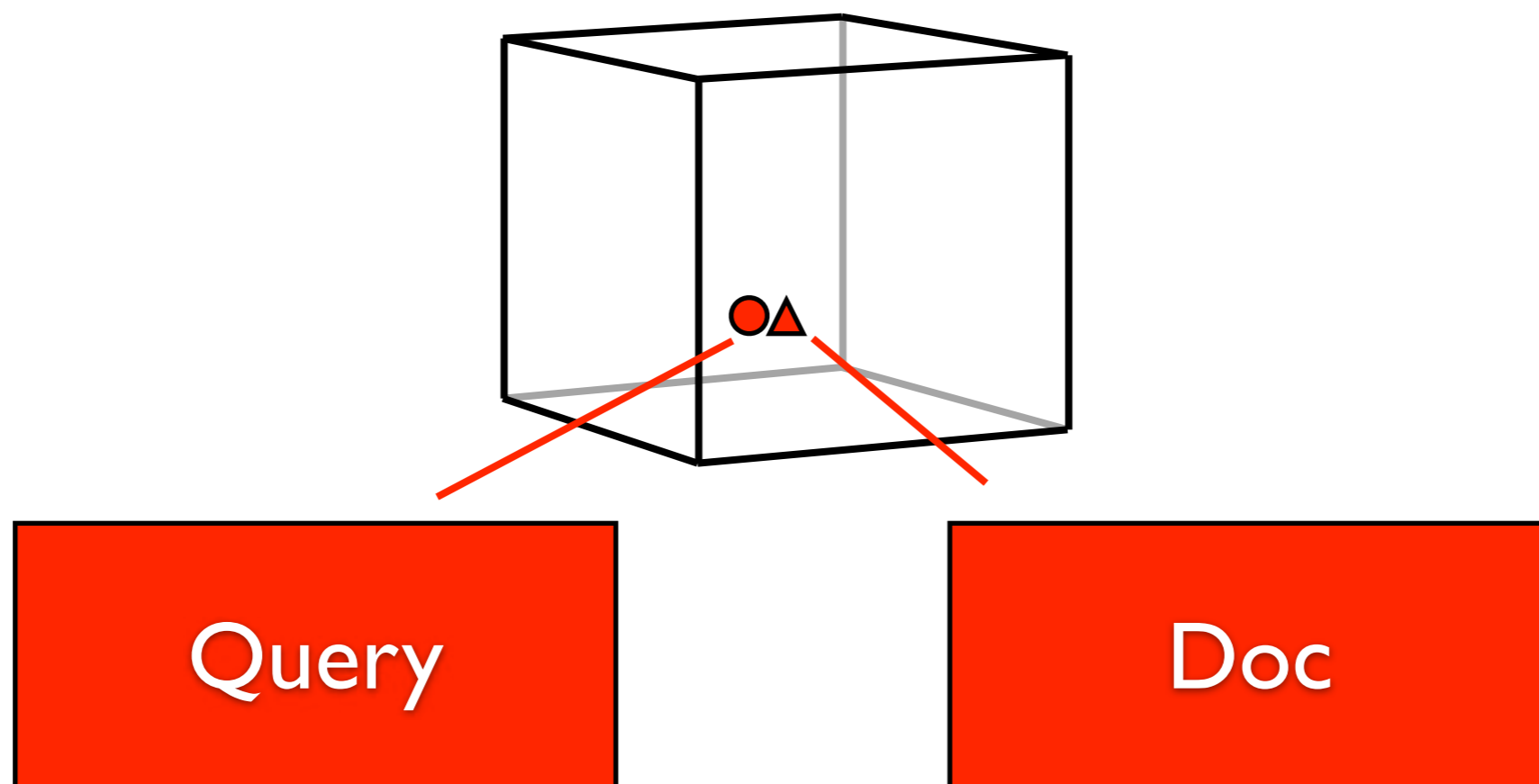


N-dimensional Embeddings

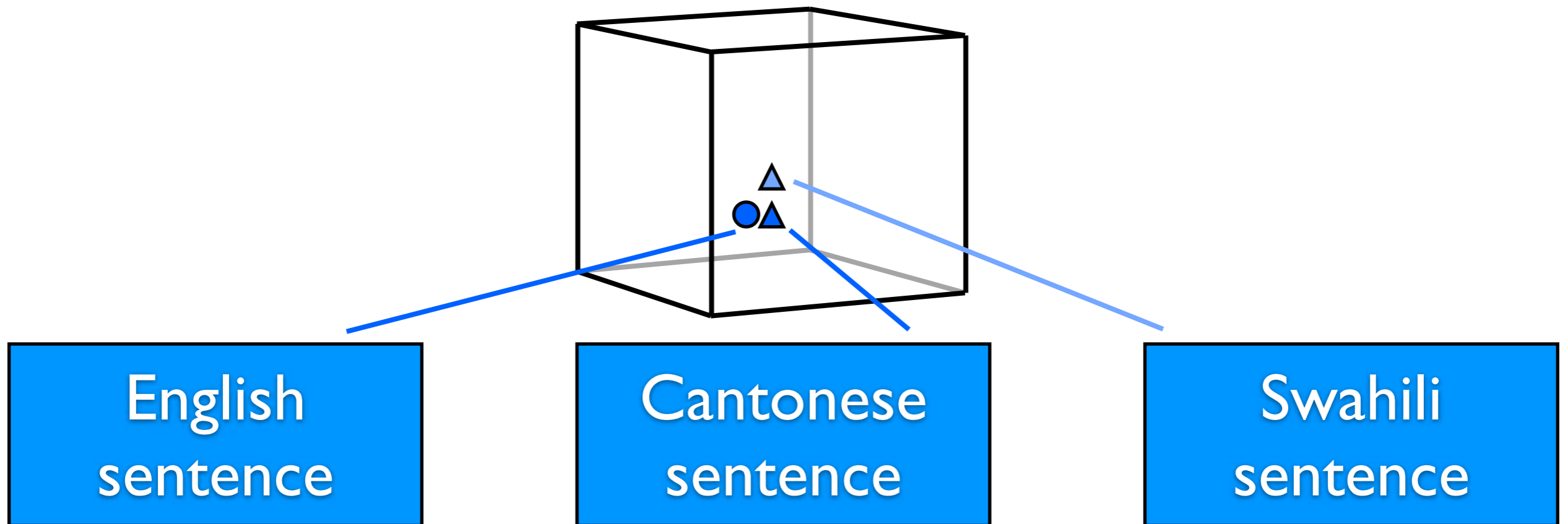
Plenty of applications:

- Machine Translation
- Synonym handling
- Sentiment analysis
- Ads
- Semantic visual models
- Entity disambiguation

Embedding Longer Pieces of Text

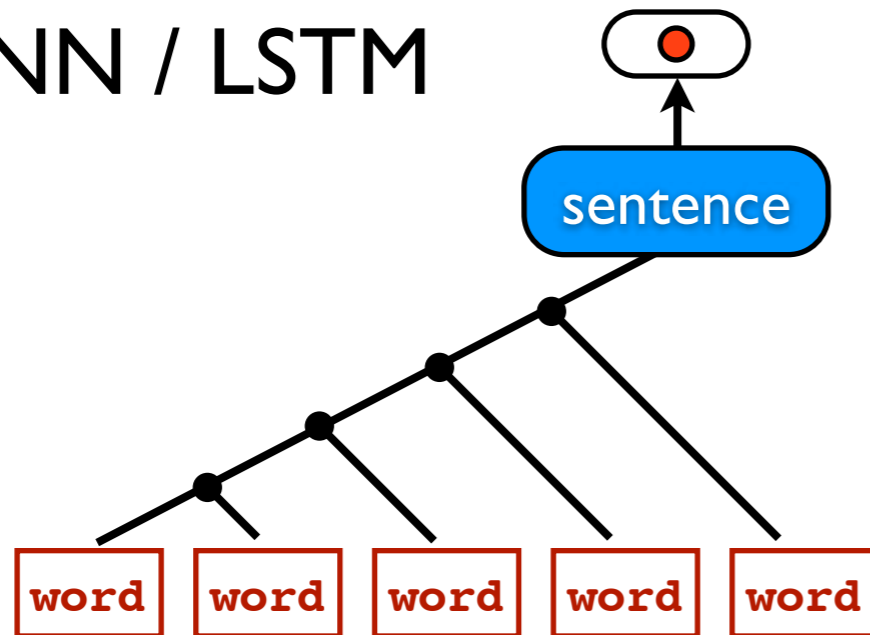


Embedding Longer Pieces of Text

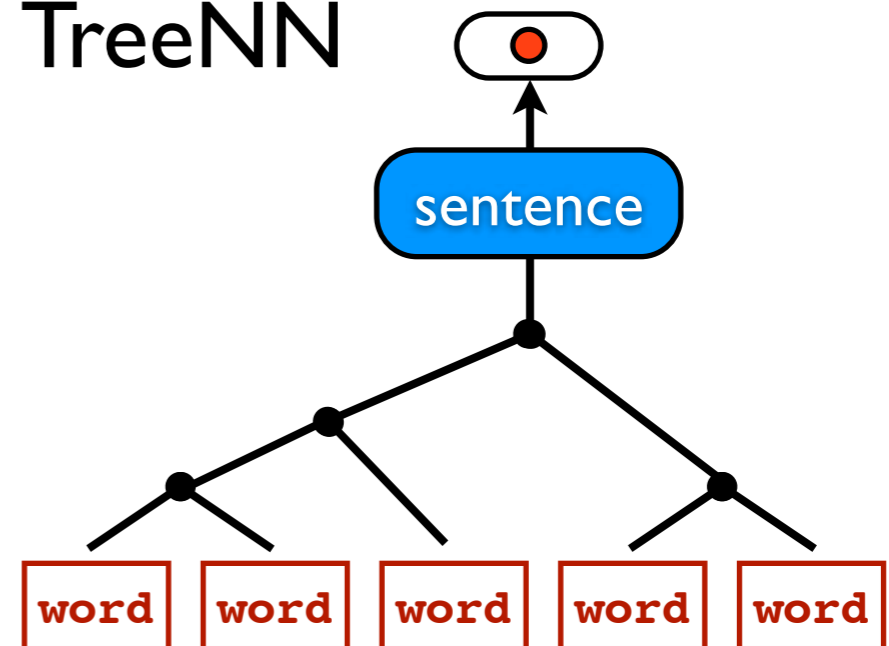


Embedding Longer Pieces of Text

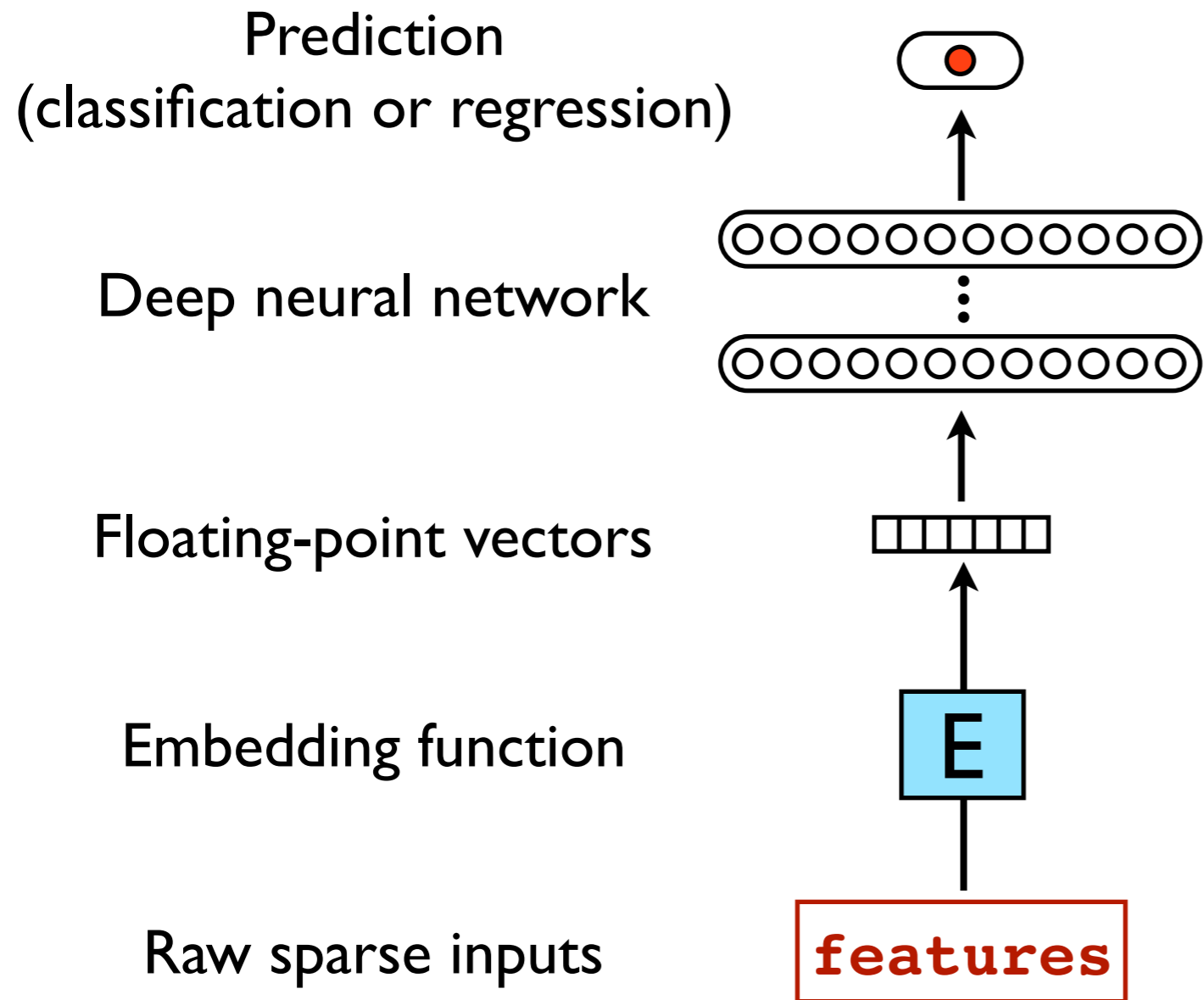
RNN / LSTM



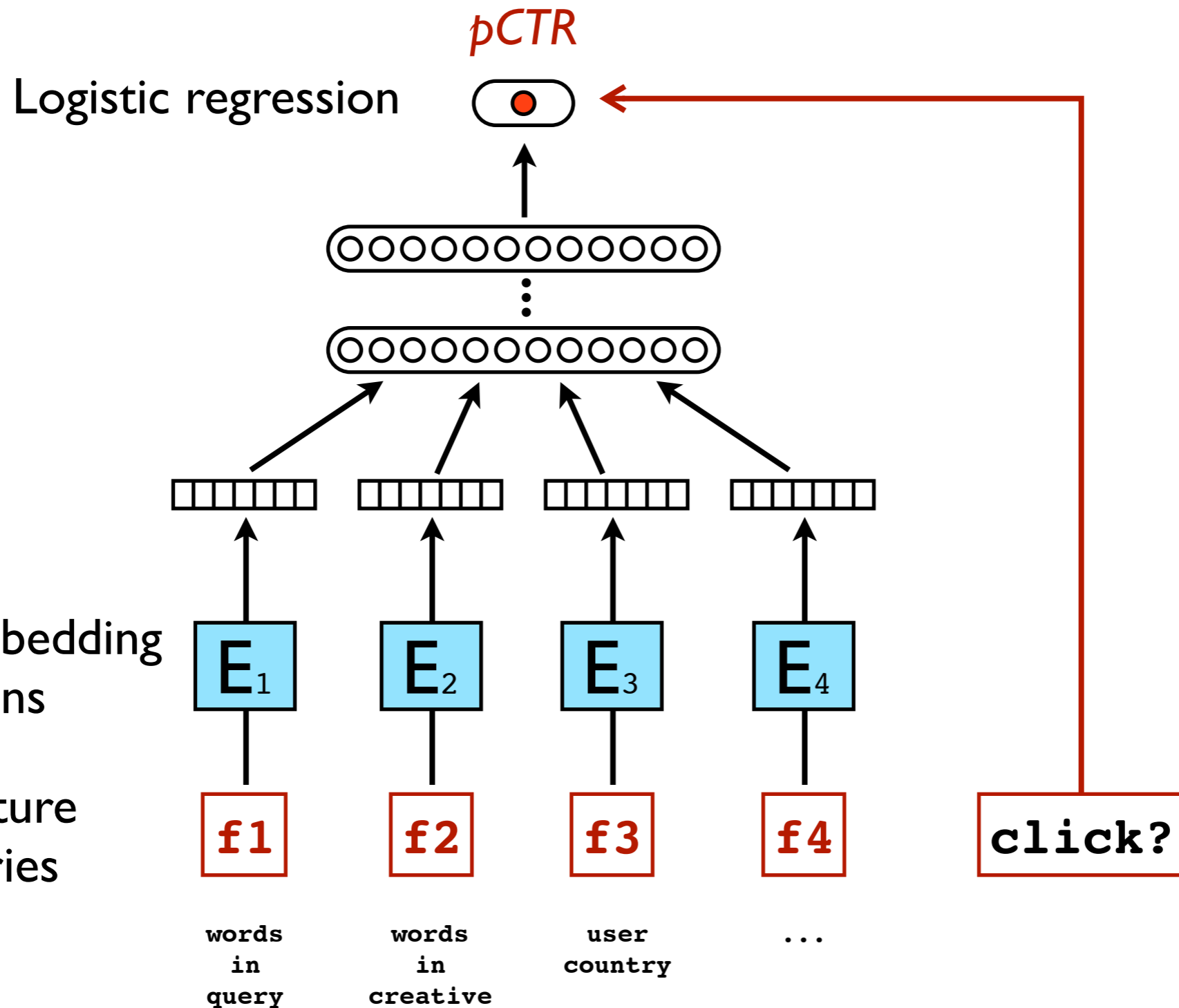
TreeNN



Using Embeddings in Larger Neural Models



Predicting clicks



Embeddings and Neural Nets Show Considerable Promise

In Conclusion...

- Designing and building large-scale retrieval systems is a challenging, fun endeavor
 - new problems require continuous evolution
 - work benefits many users
 - new retrieval techniques often require new systems

- Thanks for your attention!

Thanks! Questions...?

- Further reading:

Ghemawat, Gobioff, & Leung. *Google File System*, SOSP 2003.

Barroso, Dean, & Hölzle. *Web Search for a Planet: The Google Cluster Architecture*, IEEE Micro, 2003.

Dean & Ghemawat. *MapReduce: Simplified Data Processing on Large Clusters*, OSDI 2004.

Chang, Dean, Ghemawat, Hsieh, Wallach, Burrows, Chandra, Fikes, & Gruber. *Bigtable: A Distributed Storage System for Structured Data*, OSDI 2006.

Brants, Popat, Xu, Och, & Dean. *Large Language Models in Machine Translation*, EMNLP 2007.

Mikolov, Chen, Corrado and Dean. *Efficient Estimation of Word Representations in Vector Space*, <http://arxiv.org/abs/1301.3781>

Dean, Corrado, et al. , *Large Scale Distributed Deep Networks*, NIPS 2012.

- These and many more available at:

<http://labs.google.com/papers.html>

<http://research.google.com/people/jeff>

Understanding LLM

PA154 Language Modeling ()

Pavel Rychlý

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28 February 2024

LLM = Large Language Models

- new term, big hype
- big expectations (AGI)
- little understanding

Language

- not normal distribution (Zipf's)
 - many rare events
- ambiguous words
- variable - changing, sublanguages

Symbolic processing

ambiguous, variable, rare events leads to:

- hard for symbolic manipulations
- multiple words for same meaning
- same word for multiple meanings

Word embeddings

- words represented as vectors
 - one word = vector of 500 numbers
- similar words - closer vectors
 - not important
- dimensions can represent different features

Word features

- grammatical
 - part of speech, number, gender
- syntactic
 - used with “in”/“at”, always with a particle
- semantic
 - positive sentiment, movement meaning, fruits
- style
 - formal, colloquial
- domain
 - math, biology
- form

Word features

- features are not independent
 - math – scientific
 - used with “in” – noun
 - in capital form – proper noun
- features are not discrete
- each feature correspond to a (set of) dimension
- most features are valid for only small set of words
 - most words have (almost) 0 for most features
- multiple meanings = union of features

Phrase/sentence embeddings

- vector space is very big
 - just 2 values (0,1) in each dimension = 2^{500} combinations, 10^{50}
- same vector space for phrases
 - average of words
 - different words with same meanings – same embedding Czech president, president of the Czech Republic
- sentences, paragraphs, documents, . . .

Neurons

- input: vector
- output: number in $\langle 0,1 \rangle$
- $\sigma(x * w + b)$
- linear classifier
- hyperplane cutting the vector space
- selects one feature

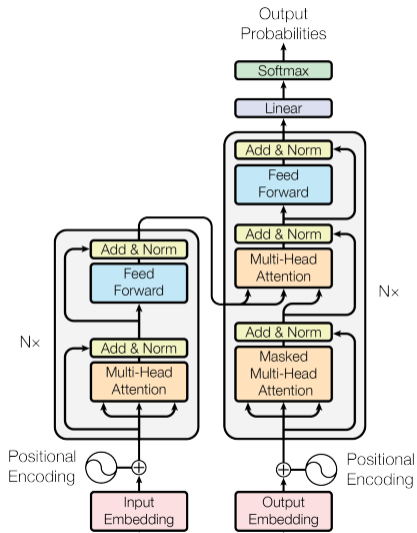
Neuron networks

- second layer can implement and/or operators
- grouping of features
 - all 10 features
 - 5 out of 10 features
- cutting the (original) vector space by several hyperplanes
 - regions in the vector space

Transformers

- *Attention Is All You Need* paper
 - attentions are important, but there other important components
- encoder/decoder
- layers of same structure with different parameters
- input: list of tokens (words)
- output depends on model

Transformers



BERT - encoder only

- output: vector (embedding) for each token
- each layer:
 - attention
 - feed forward network (2 layers)
 - direct links

Direct links

- $\text{LayerNorm}(x + \text{Sublayer}(x))$
- adding some information into original embedding
- for each token separately
- changing the original token embedding by small steps
- some part of the original information is preserved

Analogy

- for each token we have stream
- sending information/signal down the stream
- each layer can make a small transformation
 - adding information from context
 - decreasing/increasing importance of a feature

Feed forward

- first layer
 - single neuron selects a feature
 - result: vector of features
- second layer
 - select feature combinations
 - transforms them into word vector space

Attention

- highlights some features from context
- multi head = more features in single step
- transforms them into word vector space

GPT - decoder only

- auto-regressive decoder
- the last token is generating new token

Summary

- transformer is a flow of information
- starts with word embeddings
- adding/changing features – moving in the vector space
- all vectors are in the same vector space

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 18: Latent Semantic Indexing Handout version

Petr Sojka, Hinrich Schütze et al.

Faculty of Informatics, Masaryk University, Brno
Center for Information and Language Processing, University of Munich

2024-03-27

(compiled on 2024-06-10 14:16:42)

Overview

- 1 Latent semantic indexing
- 2 Dimensionality reduction
- 3 LSI in information retrieval
- 4 Clustering

Take-away today

- Latent Semantic Indexing (LSI) / Singular Value Decomposition: The math
- SVD used for dimensionality reduction
- LSI: SVD in information retrieval
- LSI as clustering
- gensim: Topic modelling for humans (practical use of LSI et al.)

Recall: Term-document matrix

| | Anthony and Cleopatra | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth |
|-----------|-----------------------------|------------------|----------------|--------|---------|---------|
| anthony | 5.25 | 3.18 | 0.0 | 0.0 | 0.0 | 0.35 |
| brutus | 1.21 | 6.10 | 0.0 | 1.0 | 0.0 | 0.0 |
| caesar | 8.59 | 2.54 | 0.0 | 1.51 | 0.25 | 0.0 |
| calpurnia | 0.0 | 1.54 | 0.0 | 0.0 | 0.0 | 0.0 |
| cleopatra | 2.85 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| mercy | 1.51 | 0.0 | 1.90 | 0.12 | 5.25 | 0.88 |
| worser | 1.37 | 0.0 | 0.11 | 4.15 | 0.25 | 1.95 |
| ... | | | | | | |

This matrix is the basis for computing [the similarity between documents and queries](#).

Today: Can we transform this matrix, so that we get a [better measure of similarity](#) between documents and queries?



Latent semantic indexing: Overview

- We will **decompose** the term-document matrix into a product of matrices.
- The particular decomposition we'll use: **singular value decomposition** (SVD).
- SVD: $C = U\Sigma V^T$ (where C = term-document matrix)
- We will then use the SVD to compute a **new, improved term-document matrix** C' .
- We'll get **better similarity** values out of C' (compared to C).
- Using SVD for this purpose is called **latent semantic indexing** or LSI. □

Example of $C = U\Sigma V^T$: The matrix C

| C | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|
| ship | 1 | 0 | 1 | 0 | 0 | 0 |
| boat | 0 | 1 | 0 | 0 | 0 | 0 |
| ocean | 1 | 1 | 0 | 0 | 0 | 0 |
| wood | 1 | 0 | 0 | 1 | 1 | 0 |
| tree | 0 | 0 | 0 | 1 | 0 | 1 |

This is a standard term-document matrix.

Actually, we use a non-weighted matrix here to simplify the example. □

Example of $C = U\Sigma V^T$: The matrix U

| U | 1 | 2 | 3 | 4 | 5 |
|-------|-------|-------|-------|-------|-------|
| ship | -0.44 | -0.30 | 0.57 | 0.58 | 0.25 |
| boat | -0.13 | -0.33 | -0.59 | 0.00 | 0.73 |
| ocean | -0.48 | -0.51 | -0.37 | 0.00 | -0.61 |
| wood | -0.70 | 0.35 | 0.15 | -0.58 | 0.16 |
| tree | -0.26 | 0.65 | -0.41 | 0.58 | -0.09 |

One row per term, one column per $\min(M, N)$ where M is the number of terms and N is the number of documents.

This is an **orthonormal matrix**: (i) Row vectors have unit length. (ii) Any two distinct row vectors are orthogonal to each other.

Think of the dimensions as “semantic” dimensions that capture distinct topics like politics, sports, economics. 2 = land/water

Each number u_{ij} in the matrix indicates how strongly related term i is to the topic represented by semantic dimension j . □

Example of $C = U\Sigma V^T$: The matrix Σ

| Σ | 1 | 2 | 3 | 4 | 5 |
|----------|------|------|------|------|------|
| 1 | 2.16 | 0.00 | 0.00 | 0.00 | 0.00 |
| 2 | 0.00 | 1.59 | 0.00 | 0.00 | 0.00 |
| 3 | 0.00 | 0.00 | 1.28 | 0.00 | 0.00 |
| 4 | 0.00 | 0.00 | 0.00 | 1.00 | 0.00 |
| 5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.39 |

This is a **square, diagonal matrix** of dimensionality $\min(M, N) \times \min(M, N)$.

The diagonal consists of the **singular values** of C .

The magnitude of the singular value measures the **importance of the corresponding semantic dimension**.

We'll make use of this by **omitting unimportant dimensions**. □

Example of $C = U\Sigma V^T$: The matrix V^T

| V^T | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|
| 1 | -0.75 | -0.28 | -0.20 | -0.45 | -0.33 | -0.12 |
| 2 | -0.29 | -0.53 | -0.19 | 0.63 | 0.22 | 0.41 |
| 3 | 0.28 | -0.75 | 0.45 | -0.20 | 0.12 | -0.33 |
| 4 | 0.00 | 0.00 | 0.58 | 0.00 | -0.58 | 0.58 |
| 5 | -0.53 | 0.29 | 0.63 | 0.19 | 0.41 | -0.22 |

One column per document, one row per $\min(M, N)$ where M is the number of terms and N is the number of documents.

Again: This is an **orthonormal matrix**: (i) Column vectors have unit length. (ii) Any two distinct column vectors are orthogonal to each other.

These are again the semantic dimensions from matrices U and Σ that capture distinct topics like politics, sports, economics.

Each number v_{ij} in the matrix indicates how strongly related document i is to the topic represented by semantic dimension

Example of $C = U\Sigma V^T$: All four matrices Recall unreduced decomposition $C = U\Sigma V^T$ Exercise: Why can this be viewed as soft clustering?

| C | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 | | | | | |
|-------|-------|-------|-------|-------|-------|----------|------|------|------|------|------|
| ship | 1 | 0 | 1 | 0 | 0 | 0 | | | | | |
| boat | 0 | 1 | 0 | 0 | 0 | 0 | | | | | |
| ocean | 1 | 1 | 0 | 0 | 0 | 0 | = | | | | |
| wood | 1 | 0 | 0 | 1 | 1 | 0 | | | | | |
| tree | 0 | 0 | 0 | 1 | 0 | 1 | | | | | |
| U | 1 | 2 | 3 | 4 | 5 | Σ | 1 | 2 | 3 | 4 | 5 |
| ship | -0.44 | -0.30 | 0.57 | 0.58 | 0.25 | 1 | 2.16 | 0.00 | 0.00 | 0.00 | 0.00 |
| boat | -0.13 | -0.33 | -0.59 | 0.00 | 0.73 | 2 | 0.00 | 1.59 | 0.00 | 0.00 | 0.00 |
| ocean | -0.48 | -0.51 | -0.37 | 0.00 | -0.61 | 3 | 0.00 | 0.00 | 1.28 | 0.00 | 0.00 |
| wood | -0.70 | 0.35 | 0.15 | -0.58 | 0.16 | 4 | 0.00 | 0.00 | 0.00 | 1.00 | 0.00 |
| tree | -0.26 | 0.65 | -0.41 | 0.58 | -0.09 | 5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.39 |
| V^T | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 | | | | | |
| 1 | -0.75 | -0.28 | -0.20 | -0.45 | -0.33 | -0.12 | | | | | |
| 2 | -0.29 | -0.53 | -0.19 | 0.63 | 0.22 | 0.41 | | | | | |
| 3 | 0.28 | -0.75 | 0.45 | -0.20 | 0.12 | -0.33 | | | | | |
| 4 | 0.00 | 0.00 | 0.58 | 0.00 | -0.58 | 0.58 | | | | | |
| 5 | -0.53 | 0.29 | 0.63 | 0.19 | 0.41 | -0.22 | | | | | |

LSI is decomposition of C into a representation of the terms, a representation of the documents and a representation of the importance of the "semantic" dimensions. □

LSI: Summary

- We've decomposed the term-document matrix C into a product of three matrices: $U\Sigma V^T$.
- The term matrix U – consists of one (row) vector for each term
- The document matrix V^T – consists of one (column) vector for each document
- The singular value matrix Σ – diagonal matrix with singular values, reflecting importance of each dimension
- Next: Why are we doing this? □

Exercise

| V^T | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|
| 1 | -0.75 | -0.28 | -0.20 | -0.45 | -0.33 | -0.12 |
| 2 | -0.29 | -0.53 | -0.19 | 0.63 | 0.22 | 0.41 |
| 3 | 0.28 | -0.75 | 0.45 | -0.20 | 0.12 | -0.33 |
| 4 | 0.00 | 0.00 | 0.58 | 0.00 | -0.58 | 0.58 |
| 5 | -0.53 | 0.29 | 0.63 | 0.19 | 0.41 | -0.22 |

Verify that the first document has unit length.

Verify that the first two documents are orthogonal.

$$0.75^2 + 0.29^2 + 0.28^2 + 0.00^2 + 0.53^2 = 1.0059$$

$$\begin{aligned} & -0.75 * -0.28 + -0.29 * -0.53 + 0.28 * -0.75 + 0.00 * 0.00 + \\ & -0.53 * 0.29 = 0 \end{aligned}$$

How we use the SVD in LSI

- Key property: Each singular value tells us how important its dimension is.
- By setting less important dimensions to zero, we keep the important information, but get rid of the “details”.
- These details may
 - be **noise** – in that case, reduced LSI is a better representation because it is less noisy.
 - **make things dissimilar that should be similar** – again, the reduced LSI representation is a better representation because it represents similarity better.
- Analogy for “fewer details is better”
 - Image of a blue flower
 - Image of a yellow flower
 - Omitting color makes it easier to see the similarity



Reducing the dimensionality to 2

| U | 1 | 2 | 3 | 4 | 5 | |
|------------|-------|-------|-------|-------|-------|-------|
| ship | -0.44 | -0.30 | 0.00 | 0.00 | 0.00 | |
| boat | -0.13 | -0.33 | 0.00 | 0.00 | 0.00 | |
| ocean | -0.48 | -0.51 | 0.00 | 0.00 | 0.00 | |
| wood | -0.70 | 0.35 | 0.00 | 0.00 | 0.00 | |
| tree | -0.26 | 0.65 | 0.00 | 0.00 | 0.00 | |
| Σ_2 | 1 | 2 | 3 | 4 | 5 | |
| 1 | 2.16 | 0.00 | 0.00 | 0.00 | 0.00 | |
| 2 | 0.00 | 1.59 | 0.00 | 0.00 | 0.00 | |
| 3 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | |
| 4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | |
| 5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | |
| V^T | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
| 1 | -0.75 | -0.28 | -0.20 | -0.45 | -0.33 | -0.12 |
| 2 | -0.29 | -0.53 | -0.19 | 0.63 | 0.22 | 0.41 |
| 3 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |

Actually, we only zero out singular values in Σ . This has the effect of setting the corresponding dimensions in U and V^T to zero when computing the product $C = U\Sigma V^T$. \square

Reducing the dimensionality to 2

| C_2 | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 | | | | | |
|-------|-------|-------|-------|-------|-------|------------|------|------|------|------|------|
| ship | 0.85 | 0.52 | 0.28 | 0.13 | 0.21 | -0.08 | | | | | |
| boat | 0.36 | 0.36 | 0.16 | -0.20 | -0.02 | -0.18 | | | | | |
| ocean | 1.01 | 0.72 | 0.36 | -0.04 | 0.16 | -0.21 | | | | | |
| wood | 0.97 | 0.12 | 0.20 | 1.03 | 0.62 | 0.41 | | | | | |
| tree | 0.12 | -0.39 | -0.08 | 0.90 | 0.41 | 0.49 | | | | | |
| U | 1 | 2 | 3 | 4 | 5 | Σ_2 | 1 | 2 | 3 | 4 | 5 |
| ship | -0.44 | -0.30 | 0.57 | 0.58 | 0.25 | 1 | 2.16 | 0.00 | 0.00 | 0.00 | 0.00 |
| boat | -0.13 | -0.33 | -0.59 | 0.00 | 0.73 | 2 | 0.00 | 1.59 | 0.00 | 0.00 | 0.00 |
| ocean | -0.48 | -0.51 | -0.37 | 0.00 | -0.61 | 3 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| wood | -0.70 | 0.35 | 0.15 | -0.58 | 0.16 | 4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| tree | -0.26 | 0.65 | -0.41 | 0.58 | -0.09 | 5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| V^T | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 | | | | | |
| 1 | -0.75 | -0.28 | -0.20 | -0.45 | -0.33 | -0.12 | | | | | |
| 2 | -0.29 | -0.53 | -0.19 | 0.63 | 0.22 | 0.41 | | | | | |
| 3 | 0.28 | -0.75 | 0.45 | -0.20 | 0.12 | -0.33 | | | | | |
| 4 | 0.00 | 0.00 | 0.58 | 0.00 | -0.58 | 0.58 | | | | | |
| 5 | -0.53 | 0.29 | 0.63 | 0.19 | 0.41 | -0.22 | | | | | |



Example of $C = U\Sigma V^T$: All four matrices Recall unreduced decomposition $C = U\Sigma V^T$ Exercise: Why can this be viewed as soft clustering?

| C | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 | | | | | |
|-------|-------|-------|-------|-------|-------|----------|------|------|------|------|------|
| ship | 1 | 0 | 1 | 0 | 0 | 0 | | | | | |
| boat | 0 | 1 | 0 | 0 | 0 | 0 | | | | | |
| ocean | 1 | 1 | 0 | 0 | 0 | 0 | = | | | | |
| wood | 1 | 0 | 0 | 1 | 1 | 0 | | | | | |
| tree | 0 | 0 | 0 | 1 | 0 | 1 | | | | | |
| U | 1 | 2 | 3 | 4 | 5 | Σ | 1 | 2 | 3 | 4 | 5 |
| ship | -0.44 | -0.30 | 0.57 | 0.58 | 0.25 | 1 | 2.16 | 0.00 | 0.00 | 0.00 | 0.00 |
| boat | -0.13 | -0.33 | -0.59 | 0.00 | 0.73 | 2 | 0.00 | 1.59 | 0.00 | 0.00 | 0.00 |
| ocean | -0.48 | -0.51 | -0.37 | 0.00 | -0.61 | 3 | 0.00 | 0.00 | 1.28 | 0.00 | 0.00 |
| wood | -0.70 | 0.35 | 0.15 | -0.58 | 0.16 | 4 | 0.00 | 0.00 | 0.00 | 1.00 | 0.00 |
| tree | -0.26 | 0.65 | -0.41 | 0.58 | -0.09 | 5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.39 |
| V^T | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 | | | | | |
| 1 | -0.75 | -0.28 | -0.20 | -0.45 | -0.33 | -0.12 | | | | | |
| 2 | -0.29 | -0.53 | -0.19 | 0.63 | 0.22 | 0.41 | | | | | |
| 3 | 0.28 | -0.75 | 0.45 | -0.20 | 0.12 | -0.33 | | | | | |
| 4 | 0.00 | 0.00 | 0.58 | 0.00 | -0.58 | 0.58 | | | | | |
| 5 | -0.53 | 0.29 | 0.63 | 0.19 | 0.41 | -0.22 | | | | | |

LSI is decomposition of C into a representation of the terms, a representation of the documents and a representation of the importance of the “semantic” dimensions. □

Original matrix C vs. reduced $C_2 = U\Sigma_2V^T$

| C | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|
| ship | 1 | 0 | 1 | 0 | 0 | 0 |
| boat | 0 | 1 | 0 | 0 | 0 | 0 |
| ocean | 1 | 1 | 0 | 0 | 0 | 0 |
| wood | 1 | 0 | 0 | 1 | 1 | 0 |
| tree | 0 | 0 | 0 | 1 | 0 | 1 |

| C_2 | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|
| ship | 0.85 | 0.52 | 0.28 | 0.13 | 0.21 | -0.08 |
| boat | 0.36 | 0.36 | 0.16 | -0.20 | -0.02 | -0.18 |
| ocean | 1.01 | 0.72 | 0.36 | -0.04 | 0.16 | -0.21 |
| wood | 0.97 | 0.12 | 0.20 | 1.03 | 0.62 | 0.41 |
| tree | 0.12 | -0.39 | -0.08 | 0.90 | 0.41 | 0.49 |

We can view C_2 as a **two-dimensional** representation of the matrix C . We have performed a **dimensionality reduction** to two dimensions.



Exercise

| C | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|
| ship | 1 | 0 | 1 | 0 | 0 | 0 |
| boat | 0 | 1 | 0 | 0 | 0 | 0 |
| ocean | 1 | 1 | 0 | 0 | 0 | 0 |
| wood | 1 | 0 | 0 | 1 | 1 | 0 |
| tree | 0 | 0 | 0 | 1 | 0 | 1 |

Compute the similarity between d_2 and d_3 for the original matrix and for the reduced matrix.

| C_2 | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|
| ship | 0.85 | 0.52 | 0.28 | 0.13 | 0.21 | -0.08 |
| boat | 0.36 | 0.36 | 0.16 | -0.20 | -0.02 | -0.18 |
| ocean | 1.01 | 0.72 | 0.36 | -0.04 | 0.16 | -0.21 |
| wood | 0.97 | 0.12 | 0.20 | 1.03 | 0.62 | 0.41 |
| tree | 0.12 | -0.39 | -0.08 | 0.90 | 0.41 | 0.49 |

Why the reduced matrix C_2 is better than C

| C | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|
| ship | 1 | 0 | 1 | 0 | 0 | 0 |
| boat | 0 | 1 | 0 | 0 | 0 | 0 |
| ocean | 1 | 1 | 0 | 0 | 0 | 0 |
| wood | 1 | 0 | 0 | 1 | 1 | 0 |
| tree | 0 | 0 | 0 | 1 | 0 | 1 |

| C_2 | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|
| ship | 0.85 | 0.52 | 0.28 | 0.13 | 0.21 | -0.08 |
| boat | 0.36 | 0.36 | 0.16 | -0.20 | -0.02 | -0.18 |
| ocean | 1.01 | 0.72 | 0.36 | -0.04 | 0.16 | -0.21 |
| wood | 0.97 | 0.12 | 0.20 | 1.03 | 0.62 | 0.41 |
| tree | 0.12 | -0.39 | -0.08 | 0.90 | 0.41 | 0.49 |

Similarity of d_2 and d_3 in the original space: 0.

Similarity of d_2 and d_3 in the reduced space:

$$0.52 * 0.28 + 0.36 * 0.16 + 0.72 * 0.36 + 0.12 * 0.20 + -0.39 * -0.08 \approx 0.52$$

“boat” and “ship” are semantically similar. The “reduced” similarity measure reflects this.

What property of the SVD reduction is responsible for improved similarity? □

Exercise: Compute matrix product

| C_2 | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 | | | | | | |
|-------|-------|-------|-------|-------|-------|-------|------------|------|------|------|------|------|
| ship | 0.09 | 0.16 | 0.06 | -0.19 | -0.07 | -0.12 | | | | | | |
| boat | 0.10 | 0.17 | 0.06 | -0.21 | -0.07 | -0.14 | | | | | | |
| ocean | 0.15 | 0.27 | 0.10 | -0.32 | -0.11 | -0.21 | | | | | | |
| wood | -0.10 | -0.19 | -0.07 | 0.22 | 0.08 | 0.14 | | | | | | |
| tree | -0.19 | -0.34 | -0.12 | 0.41 | 0.14 | 0.27 | | | | | | |
| U | | | | | | | | | | | | |
| | 1 | 2 | 3 | 4 | 5 | | Σ_2 | 1 | 2 | 3 | 4 | 5 |
| ship | -0.44 | -0.30 | 0.57 | 0.58 | 0.25 | | 1 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| boat | -0.13 | -0.33 | -0.59 | 0.00 | 0.73 | | 2 | 0.00 | 1.59 | 0.00 | 0.00 | 0.00 |
| ocean | -0.48 | -0.51 | -0.37 | 0.00 | -0.61 | | 3 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| wood | -0.70 | 0.35 | 0.15 | -0.58 | 0.16 | | 4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| tree | -0.26 | 0.65 | -0.41 | 0.58 | -0.09 | | 5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| V^T | | | | | | | | | | | | |
| | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 | | | | | | |
| 1 | -0.75 | -0.28 | -0.20 | -0.45 | -0.33 | -0.12 | | | | | | |
| 2 | -0.29 | -0.53 | -0.19 | 0.63 | 0.22 | 0.41 | | | | | | |
| 3 | 0.28 | -0.75 | 0.45 | -0.20 | 0.12 | -0.33 | | | | | | |
| 4 | 0.00 | 0.00 | 0.58 | 0.00 | -0.58 | 0.58 | | | | | | |
| 5 | -0.53 | 0.29 | 0.63 | 0.19 | 0.41 | -0.22 | | | | | | |

????????=

Why we use LSI in information retrieval

- LSI takes documents that are semantically similar (= talk about the same topics), ...
- ...but are not similar in the vector space (because they use different words) ...
- ...and re-represents them in a reduced vector space ...
- ...in which they have higher similarity.
- Thus, LSI addresses the problems of **synonymy** and **semantic relatedness**.
- Standard vector space: Synonyms contribute nothing to document similarity.
- Desired effect of LSI: Synonyms contribute strongly to document similarity. □

How LSI addresses synonymy and semantic relatedness

- The dimensionality reduction forces us to omit a lot of “detail”.
- We have to map different words (= different dimensions of the full space) to the same dimension in the reduced space.
- The “cost” of mapping synonyms to the same dimension is much less than the cost of collapsing unrelated words.
- SVD selects the “least costly” mapping (see below).
- Thus, it will map synonyms to the same dimension.
- But it will avoid doing that for unrelated words. □

LSI: Comparison to other approaches

- Recap: **Relevance feedback** and **query expansion** are used to **increase recall** in information retrieval – if query and documents have no terms in common.
 - (or, more commonly, too few terms in common for a high similarity score)
- LSI **increases recall and hurts precision**.
- Thus, it addresses the same problems as (pseudo) relevance feedback and query expansion . . .
- . . . and it has the same problems. □

Implementation

- Compute SVD of term-document matrix
- Reduce the space and compute reduced document representations
- Map the query into the reduced space $\vec{q}_k = \Sigma_k^{-1} U_k^T \vec{q}$.
- This follows from: $C_k = U_k \Sigma_k V_k^T \Rightarrow \Sigma_k^{-1} U_k^T C_k = V_k^T$
- Compute similarity of q_k with all reduced documents in V_k .
- Output ranked list of documents as usual
- Exercise: What is the fundamental problem with this approach?



Optimality

- SVD is **optimal** in the following sense.
- Keeping the k largest singular values and setting all others to zero gives you the optimal approximation of the original matrix C . **Eckart-Young theorem**
- Optimal: no other matrix of the same rank (= with the same underlying dimensionality) approximates C better.
- Measure of approximation is Frobenius norm:
$$\|C\|_F = \sqrt{\sum_i \sum_j c_{ij}^2}$$
- So LSI uses the “best possible” matrix.
- There is only one best possible matrix – unique solution (modulo signs).
- Caveat: There is only a tenuous relationship between the Frobenius norm and cosine similarity between documents. □

Data for graphical illustration of LSI

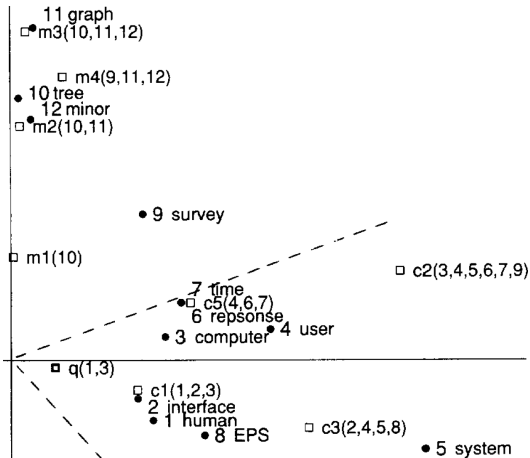
- c_1 Human machine interface for lab abc computer applications
- c_2 A survey of user opinion of computer system response time
- c_3 The EPS user interface management system
- c_4 System and human system engineering testing of EPS
- c_5 Relation of user perceived response time to error measurement
- m_1 The generation of random binary unordered trees
- m_2 The intersection graph of paths in trees
- m_3 Graph minors IV Widths of trees and well quasi ordering
- m_4 Graph minors A survey

The matrix C

| | c1 | c2 | c3 | c4 | c5 | m1 | m2 | m3 | m4 |
|-----------|----|----|----|----|----|----|----|----|----|
| human | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| interface | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| computer | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| user | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| system | 0 | 1 | 1 | 2 | 0 | 0 | 0 | 0 | 0 |
| response | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| time | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| EPS | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| survey | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| trees | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 |
| graph | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 |
| minors | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |



Graphical illustration of LSI: Plot of C_2



2-dimensional plot of C_2 (scaled dimensions). Circles = terms. Open squares = documents (component terms in parentheses). q = query “human computer interaction”.

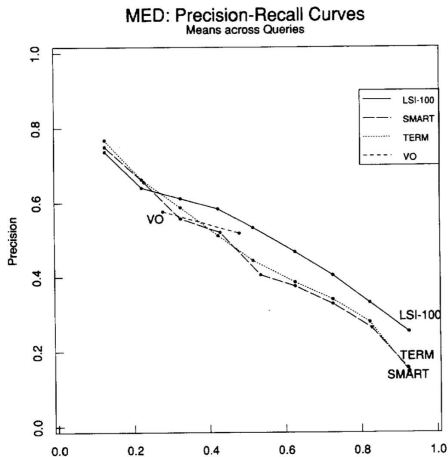
The dotted cone represents the region whose points are within a cosine of .9 from q . All documents about human-computer documents (c1-c5) are near q , even c3/c5 although they share no terms. None of the graph theory documents (m1-m4) are near q .



Exercise

What happens when we rank documents according to cosine similarity in the original vector space? What happens when we rank documents according to cosine similarity in the reduced vector space?

LSI performs better than vector space on MED collection



LSI-100 = LSI reduced to 100 dimensions; SMART = SMART implementation of vector space model



Example of $C = U\Sigma V^T$: All four matrices Recall unreduced decomposition $C = U\Sigma V^T$ Exercise: Why can this be viewed as soft clustering?

| C | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 | | | | | |
|-------|-------|-------|-------|-------|-------|----------|------|------|------|------|------|
| ship | 1 | 0 | 1 | 0 | 0 | 0 | | | | | |
| boat | 0 | 1 | 0 | 0 | 0 | 0 | | | | | |
| ocean | 1 | 1 | 0 | 0 | 0 | 0 | = | | | | |
| wood | 1 | 0 | 0 | 1 | 1 | 0 | | | | | |
| tree | 0 | 0 | 0 | 1 | 0 | 1 | | | | | |
| U | 1 | 2 | 3 | 4 | 5 | Σ | 1 | 2 | 3 | 4 | 5 |
| ship | -0.44 | -0.30 | 0.57 | 0.58 | 0.25 | 1 | 2.16 | 0.00 | 0.00 | 0.00 | 0.00 |
| boat | -0.13 | -0.33 | -0.59 | 0.00 | 0.73 | 2 | 0.00 | 1.59 | 0.00 | 0.00 | 0.00 |
| ocean | -0.48 | -0.51 | -0.37 | 0.00 | -0.61 | 3 | 0.00 | 0.00 | 1.28 | 0.00 | 0.00 |
| wood | -0.70 | 0.35 | 0.15 | -0.58 | 0.16 | 4 | 0.00 | 0.00 | 0.00 | 1.00 | 0.00 |
| tree | -0.26 | 0.65 | -0.41 | 0.58 | -0.09 | 5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.39 |
| V^T | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 | | | | | |
| 1 | -0.75 | -0.28 | -0.20 | -0.45 | -0.33 | -0.12 | | | | | |
| 2 | -0.29 | -0.53 | -0.19 | 0.63 | 0.22 | 0.41 | | | | | |
| 3 | 0.28 | -0.75 | 0.45 | -0.20 | 0.12 | -0.33 | | | | | |
| 4 | 0.00 | 0.00 | 0.58 | 0.00 | -0.58 | 0.58 | | | | | |
| 5 | -0.53 | 0.29 | 0.63 | 0.19 | 0.41 | -0.22 | | | | | |

LSI is decomposition of C into a representation of the terms, a representation of the documents and a representation of the importance of the "semantic" dimensions. □

Why LSI can be viewed as soft clustering

- Each of the k dimensions of the reduced space is one cluster.
- If the value of the LSI representation of document d on dimension k is x , then x is the soft membership of d in topic k .
- This soft membership can be positive or negative.
- Example: Dimension 2 in our SVD decomposition
- This dimension/cluster corresponds to the water/earth dichotomy.
- “ship”, “boat”, “ocean” have negative values.
- “wood”, “tree” have positive values.
- d_1, d_2, d_3 have negative values (most of their terms are water terms).
- d_4, d_5, d_6 have positive values (all of their terms are earth terms).



Semantic indexing and clustering with Gensim

Gensim: an open-source vector space modeling and topic modeling toolkit, implemented in the Python programming language

Tutorial examples of topic modelling for humans (LSI):

<http://radimrehurek.com/gensim/tut2.html>

DML-CZ similarity example:

<http://dml.cz/handle/10338.dmlcz/500114/SimilarArticles>

cf. papers similar to famous Otakar Borůvka's paper

Go forth and create masterpieces for semantic indexing applications (by gensim, similarly as other 5300+ already did ;-)!

Take-away today

- Latent Semantic Indexing (LSI) / Singular Value Decomposition: The math
- SVD used for dimensionality reduction
- LSI: SVD in information retrieval
- LSI as clustering
- gensim: Topic modelling for humans (practical use of LSI et al.)

Resources

- Chapter 18 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - Original paper on latent semantic indexing by Deerwester et al.
 - Paper on probabilistic LSI by Thomas Hofmann
 - Word space: LSI for words

Topic Similarity in Information Retrieval

Examples and Experience of NLP Centre and LEMMA Projects

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Natural Language Processing Centre, Faculty of Informatics
Masaryk University, Brno, Czech Republic

`sojka@fi.muni.cz`

PV211 Intro to Information Retrieval: LDA

Coping with Information Overload by Filtering of *Big Data*



Life is searching: group **similar** and narrow focus of search in [your] Big Data.

Similarity types: from **plagiarism** (similarity on n -grams, narrative similarity, evolved into <http://theses.cz>) to **thematic, topical similarity**.

Levels of content processing: strings → words and collocations → semantics (word meaning) → information (knowledge).

Grabbing the essence (content) of documents: **topical modelling**.

Zde zadejte hledané slovo nebo slova oddělená čárkou (= operátor ACCRUE) nebo jiným operátorem (lze použít tlačítek Volba operátorů). Slova budou hledána ve všech přípustných tvarech (kromě změny kmenové souhlásky) bez zřetele na velká/malá písmena. Při hledání fráze (např. univerzita karlova) se tato dvě slova zadají neoddělená čárkou. Při hledání slova v přesném tvaru (bez skloňování/časování) se slovo uvede v uvozovkách, např. „VŠE“.

Hledaný text

- Ottova encyklopedie obecných vědomostí® Ottova encyklopedie nové doby
 hledat v plných textech hesel pouze v názvech hesel volný text

Vazby mezi výrazy: ACCRUE (čím více, tím lépe) AND (a) OR (nebo) NOT (ne)

Topical Similarity in Digital Mathematics Library

Similar articles to article

[CHEN, HUANYIN](#)

Strong separativity over exchange rings. (English). Czechoslovak Mathematical Journal, vol. 58 (2008), issue 2, pp. 417-428

[-> Back to article](#)

Method LSI 

[Generalized \$SVS\$ -rings ...](#)



[Exch NUMDAM: Generalized \$SVS\$ -rings and von Neumann regular rings](#)

[Exchange rings in whic...](#)

[Rings which have proje...](#)

[Epimorphisms of regul...](#)

[Von Neumann regular ri...](#)

[A general theory of Fo...](#)

[On \$SVS\$ -rings and unit...](#)

[Extensions of \$SGM\$ -rings](#)

[\$SES\$ -rings and differen...](#)

Method RP 

[Exchange rings with st...](#)

[Generalized \$SVS\$ -rings ...](#)

[Exchange rings in whic...](#)

[Rings which have proje...](#)

[\$S\$ - \$\Omega\$ - \$1\$ -generated u...](#)

[Diagonal reductions of...](#)

[Von Neumann regular ri...](#)

[Steady ideals and rings](#)

[Dualities over compact...](#)

[The p. p. ring and the...](#)

Method TFIDF 

[Exchange rings with st...](#)

[Exchange rings in whic...](#)

[Diagonal reductions of...](#)

[The least separative c...](#)

[Note on the congruenc...](#)

[Extension of measure-l...](#)

[Integration in partial...](#)

[Modularity and distrib...](#)

[On abelian groups by w...](#)

[Extensions of \$SGM\$ -rings](#)

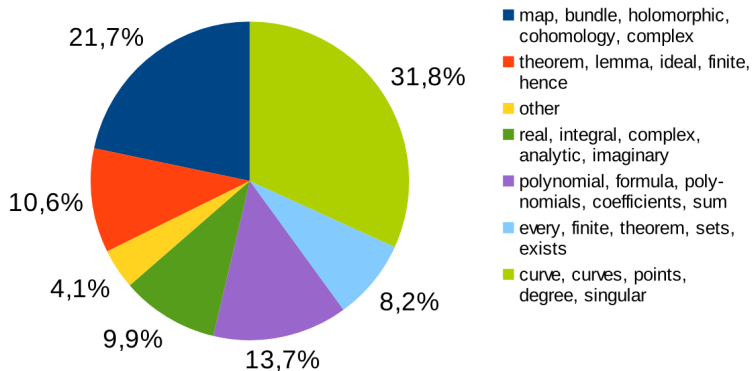
We appreciate your feedback to the methods which determine similarity of articles (e.g. which method is better, ...). Please [contact us](#). It will be helpful for future development.

[-> Back to article](#)

- ▶ 2005, GVP, Radim Řehůřek and Jan Pomikálek
- ▶ 2006, gensim, different machine learning methods as Random Projections, TFIDF word weighting, Latent Semantic Indexing/Analysis, Latent Dirichlet Allocation
- ▶ 50,000+ full-texts on <http://dm1.cz>

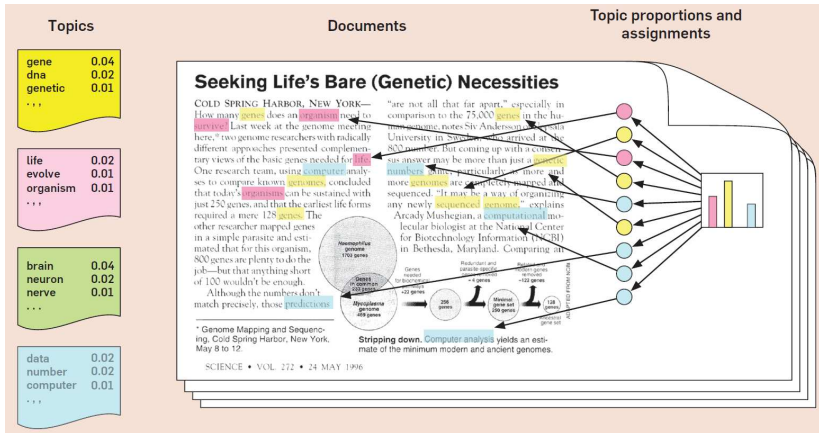
Leading Edge Example: Automated Meaning Picking from Texts

LDA Topics Pie Chart for math.0406240



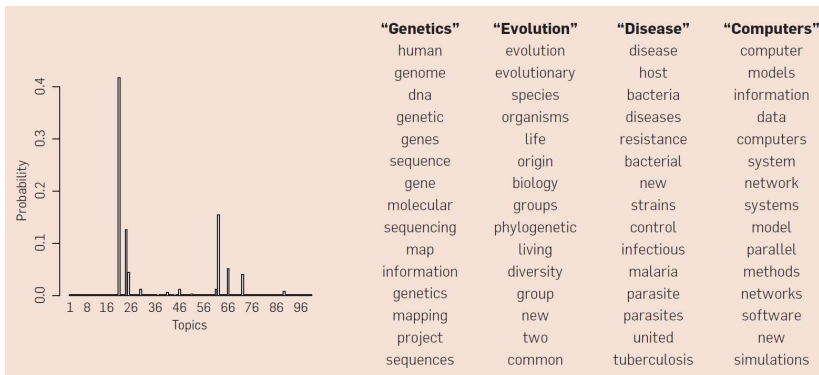
Probabilistic Topical Modelling: Latent Dirichlet Allocation

- ▶ topic: weighted list of words
- ▶ document: weighted list of topics



Topical Modelling: Latent Dirichlet Allocation II

- ▶ all topics computed automatically from document corpora

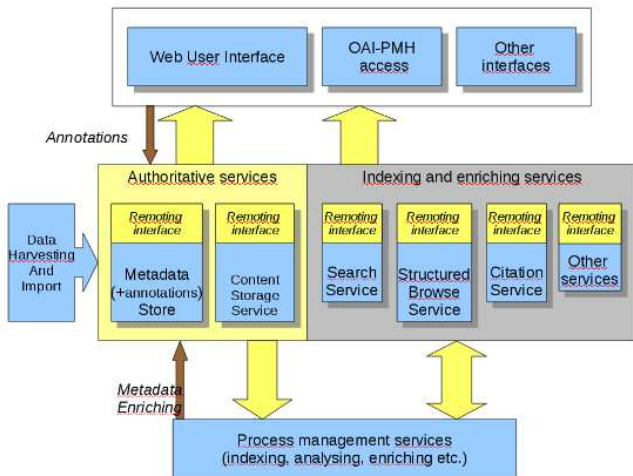


Content Similarity Results in EuDML

Within *European Digital Mathematics Library*, *EuDML*, project EU CIP-ICT-PSP we have developed and delivered technology for **similarity** (gensim), document **conversions** (Braille) and **accessibility** (math OCR), NLP content **normalization** (Mathml2text).

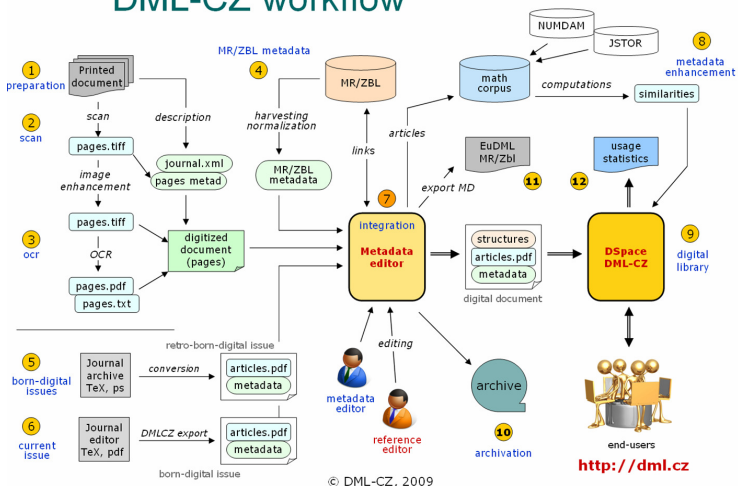
The screenshot shows the EuDML website interface. At the top left is the logo "EuDML" with the tagline "The EUROPEAN DIGITAL MATHEMATICS LIBRARY". To the right, there is a language dropdown menu set to "English (en)", a user name "Jane Doe", and a "Log Out" link. Below this is a search bar with the placeholder text "Title, Author, Keyword, Citation, Date..." and a "Search" button. A dark navigation bar contains links for "Home", "Advanced Search", "Browse by Subject", "Browse by Journals", and "Refs Lookup". The main content area displays a search result for a document titled "On the solution of the differential equation $f(x, y, y^{(1)}, \dots, y^{(n)}) = 0$ ". The author is listed as "Smbat Abian, Arthur B. Brown (1958)" and the journal as "Bollettino dell'Unione Matematica Italiana". A "Similarity:" label is followed by a progress bar that is approximately 75% full. Below this, another result is shown for "Superposition of imbeddings and Fefferman's inequality" by "Miroslav Krbeč, Thomas Schott (1999)", also from "Bollettino dell'Unione Matematica Italiana", with a similar progress bar.

Document engineering and workflows including [Math] OCR.



Digital Library Service Architecture and Workflow (DML-CZ)

DML-CZ workflow



Data Visualization and Representation

Došlý title author

Zobrazení

Přibližit

Proceedings of EQUADIFF 10, Pr...
half-linear equation
Došlý, Ondřej
growth, boundedness
qualitative theory of half-lin...
variational method
Poincaré's identity
Asymptotic behaviour of oscill...
On an asymptotic behaviour of...
exponential stability and expo...
Comparison theorems for nonlin...
Substitution method for g...
A Remark on the Oscillatorines...
Asymptotic properties
On existence of Khneser solutio...
Asymptotic behaviour of the so...

Asymptotic behaviour of osc...

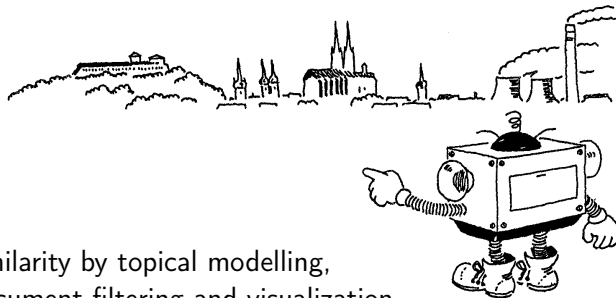
language: eng
title: Asymptotic behaviour of oscillatory solutions of a fourth-order nonlinear differential equation@en
summary: Asymptotic behaviour of oscillatory solutions of the fourth-order nonlinear differential equation with quasiderivates $y^{(4)} + r(t)f(y) = 0$ is studied.@en

Ontologie: /22-rdf-syntax-ns# Perspektiva: DML -12

- ▶ Semantic similarity indexing and search of big (continuous stream of) data. Client (search) and server (indexing) architecture.
- ▶ Developed by NLP lab PG student Radim Řehůřek (awarded in Česká hlava competition in 2011).
- ▶ Leading edge machine learning methods implemented.
- ▶ Used in 60+ local, EU or worldwide projects, 260+ citations.
- ▶ Typical deployment and fine-tuning scenario: expressing data as words (features) → configuration of topic modelling of features → setting of gensim methods and tuning parameters → usage in an application with proper visualization interface.

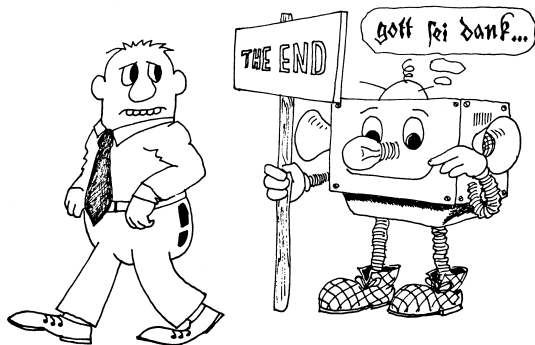
- ▶ most work done by students themselves with agile techniques, XP

Conclusions and Mutual Research Interests



- ▶ similarity by topical modelling, document filtering and visualization
- ▶ semantic, meaning computations and modelling of natural language texts (natural NLP)
- ▶ personal research interests: random walking for disambiguation, math (tree) indexing and similarity

Yes, we can!



Credits: Jiří Franek (illustrations)

- ▶ NLP Centre: <http://nlp.fi.muni.cz/>
- ▶ Topical modelling: <https://mir.fi.muni.cz/gensim/>
- ▶ Math Information Retrieval: <https://mir.fi.muni.cz>
- ▶ DML-CZ project: <http://dml.cz>, <http://project.dml.cz>
- ▶ EuDML project: <http://eudml.cz>,
<http://project.eudml.cz>
- ▶ LEMMA: <http://www.fi.muni.cz/lemma/>

Introduction to **Information Retrieval**

CS276: Information Retrieval and Web Search
Christopher Manning and Pandu Nayak

Lecture 14: Distributed Word Representations
for Information Retrieval

How can we more robustly match a user's search intent?

We want to **understand** a query, not just do String equals()

- If user searches for [Dell notebook battery size], we would like to match documents discussing “Dell laptop battery capacity”
- If user searches for [Seattle motel], we would like to match documents containing “Seattle hotel”

A pure keyword-matching IR system does nothing to help....

Simple facilities that we have already discussed do a bit to help

- Spelling correction
- Stemming / case folding

But we'd like to better **understand** when query/document match

How can we more robustly match a user's search intent?

Query expansion:

- **Relevance feedback** could allow us to capture this if we get near enough to matching documents with these words
- We can also use information on **word similarities**:
 - A manual **thesaurus** of synonyms for query expansion
 - A **measure of word similarity**
 - Calculated from a big document collection
 - Calculated by query log mining (common on the web)

Document expansion:

- Use of **anchor text** may solve this by providing human authored synonyms, but not for new or less popular web pages, or non-hyperlinked collections

Example of manual thesaurus

The screenshot displays the PubMed search interface. At the top left is the NCBI logo, and at the top right is the National Library of Medicine (NLM) logo. Below the logos is a navigation bar with tabs for PubMed, Nucleotide, Protein, Genome, Structure, PopSet, and Taxonomy. The search bar contains the text "Search PubMed for cancer" with "PubMed" in a dropdown menu and "Go" and "Clear" buttons. Below the search bar are links for "Limits", "Preview/Index", "History", "Clipboard", and "Details". On the left side, there is a sidebar with links for "About Entrez", "Text Version", "Entrez PubMed", "Overview", "Help | FAQ", "Tutorial", "New/Noteworthy", "E-Utilities", "PubMed Services", "Journals Database", "MeSH Browser", "Single Citation", and "Matcher". The main content area shows the "PubMed Query:" section with the following query:


```
("neoplasms"[MeSH Terms] OR cancer[Text Word])
```

 At the bottom of the query area are "Search" and "URL" buttons.

Search log query expansion

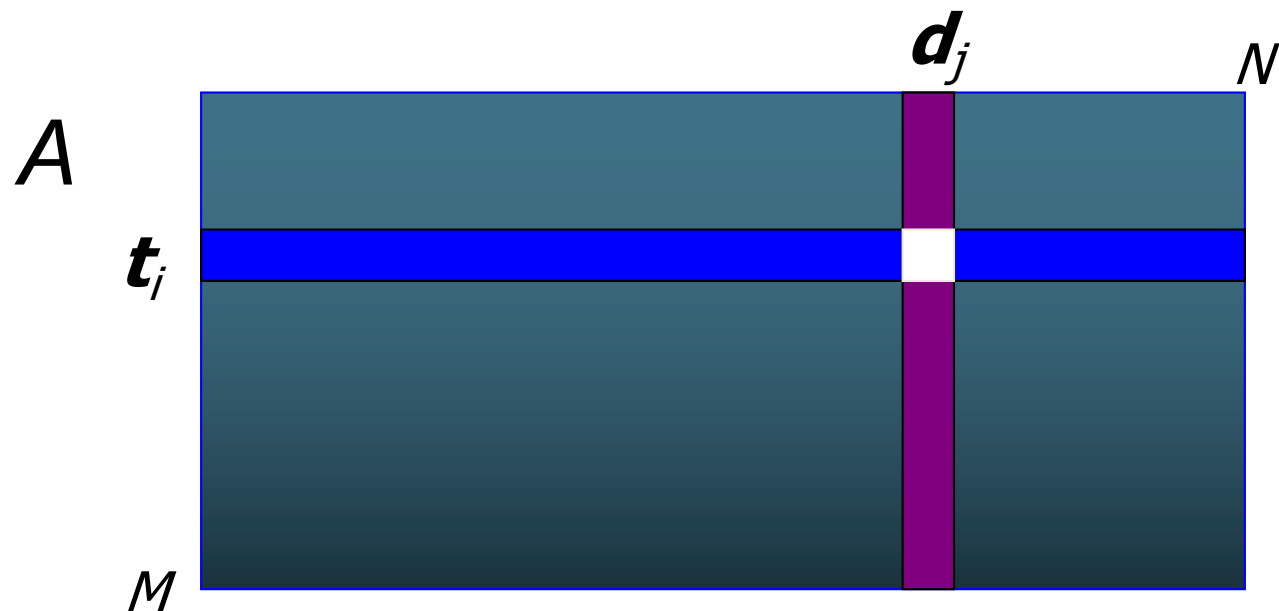
- Context-free query expansion ends up problematic
 - [wet ground] \approx [wet earth]
 - So expand [ground] \Rightarrow [ground earth]
 - But [ground coffee] \neq [earth coffee]
- You can learn query context-specific rewritings from search logs by attempting to identify the same user making a second attempt at the same user need
 - [Hinton word vector]
 - [Hinton word embedding]
- In this context, [vector] \approx [embedding]
 - But not when talking about a *disease vector* or C++!

Automatic Thesaurus Generation

- Attempt to generate a thesaurus automatically by analyzing a collection of documents
- Fundamental notion: similarity between two words
- **Definition 1: Two words are similar if they co-occur with similar words.**
- **Definition 2: Two words are similar if they occur in a given grammatical relation with the same words.**
- You can harvest, peel, eat, prepare, etc. apples and pears, so apples and pears must be similar.
- **Co-occurrence based is more robust, grammatical relations are more accurate.** 

Simple Co-occurrence Thesaurus

- Simplest way to compute one is based on term-term similarities in $C = AA^T$ where A is term-document matrix.
- $w_{i,j}$ = (normalized) weight for (t_i, d_j)



- For each t_i , pick terms with high values in C

What does C contain if A is a term-doc incidence (0/1) matrix?

Automatic thesaurus generation

example ... sort of works

| Word | Nearest neighbors |
|-------------|---|
| absolutely | absurd, whatsoever, totally, exactly, nothing |
| bottomed | dip, copper, drops, topped, slide, trimmed |
| captivating | shimmer, stunningly, superbly, plucky, witty |
| doghouse | dog, porch, crawling, beside, downstairs |
| makeup | repellent, lotion, glossy, sunscreen, skin, gel |
| mediating | reconciliation, negotiate, cease, conciliation |
| keeping | hoping, bring, wiping, could, some, would |
| lithographs | drawings, Picasso, Dali, sculptures, Gauguin |
| pathogens | toxins, bacteria, organisms, bacterial, parasites |
| senses | grasp, psyche, truly, clumsy, naïve, innate |

Too little data (10s of millions of words) treated by **too sparse method**.
 100,000 words = 10^{10} entries in C .

How can we represent term relations?

- With the standard symbolic encoding of terms, each term is a dimension
- Different terms have no inherent similarity
- $\text{motel} [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0]^T$
 $\text{hotel} [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 3 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]^T = 0$
- If query on *hotel* and document has *motel*, then our query and document vectors are **orthogonal**

Can you directly learn term relations?

- Basic IR is scoring on $q^T d$
- No treatment of synonyms; no machine learning
- Can we learn parameters W to rank via $q^T W d$?

"search ranking" q^T

"information retrieval ranking" d

$$\begin{pmatrix} 1 & 0 & 0 & 1 & 0 \\ \text{se} & \text{in} & \text{re} & \text{ra} & \text{or} \end{pmatrix} \begin{pmatrix} 1 & 0.7 & 0.5 & 0 & 0 \\ 0.3 & 1 & 0.2 & 0 & 0 \\ 0.5 & 0.2 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0.7 \\ 0 & 0 & 0 & 0.7 & 1 \end{pmatrix} \begin{pmatrix} 0 \\ 1 \\ 1 \\ 1 \\ 0 \\ \text{se} \\ \text{in} \\ \text{re} = 2.2 \\ \text{ra} \\ \text{or (dering)} \end{pmatrix}$$

- Cf. Query translation models: Berger and Lafferty (1999)
- Problem is again sparsity – W is huge $> 10^{10}$

Is there a better way?

- Idea:
 - Can we learn a dense low-dimensional representation of a word in \mathbb{R}^d such that dot products $u^T v$ express word similarity?
 - We could still if we want to include a “translation” matrix between vocabularies (e.g., cross-language): $u^T W v$
 - But **now W is small!**
 - Supervised Semantic Indexing (Bai et al. *Journal of Information Retrieval* 2009) shows successful use of learning W for information retrieval
- But we'll develop direct similarity in this class

Distributional similarity based representations

- You can get a lot of value by representing a word by means of its neighbors
- “You shall know a word by the company it keeps”
 - (J. R. Firth 1957: 11)
- One of the most successful ideas of modern statistical NLP



...government debt problems turning into **banking** crises as happened in 2009...
...saying that Europe needs unified **banking** regulation to replace the hodgepodge...
...India has just given its **banking** system a shot in the arm...

↖ These words will represent *banking* ↗

Solution: Low dimensional vectors

- The number of topics that people talk about is small (in some sense)
 - Clothes, movies, politics, ...
- Idea: store “most” of the important information in a fixed, small number of dimensions: a dense vector
- Usually 25 – 1000 dimensions
- How to reduce the dimensionality?
 - Go from big, sparse co-occurrence count vector to low dimensional “word embedding”

Traditional Way: Latent Semantic Indexing/Analysis

- Use Singular Value Decomposition (SVD) – kind of like Principal Components Analysis (PCA) for an arbitrary rectangular matrix – or just random projection to find a low-dimensional basis or orthogonal vectors
- Theory is that similarity is preserved as much as possible
- You can actually gain in IR (slightly) by doing LSA, as “noise” of term variation gets replaced by semantic “concepts”
- Somewhat popular in the 1990s [[Deerwester et al. 1990, etc.](#)]
 - But **results were always somewhat iffy** (... it worked sometimes)
 - Hard to implement efficiently in an IR system (dense vectors!)
- Discussed in *IIR* chapter 18, but not discussed further here
 - Not on the exam (!!!)

“NEURAL EMBEDDINGS”

Word meaning is defined in terms of vectors

- We will build a dense vector for each word type, chosen so that it is good at predicting other words appearing in its context

... those other words also being represented by vectors ... it all gets a bit recursive

$$\mathit{banking} = \begin{pmatrix} 0.286 \\ 0.792 \\ -0.177 \\ -0.107 \\ 0.109 \\ -0.542 \\ 0.349 \\ 0.271 \end{pmatrix}$$

Neural word embeddings - visualization



Basic idea of learning neural network word embeddings

- We define a model that aims to predict between a center word w_t and context words in terms of word vectors
- $p(\text{context} | w_t) = \dots$
- which has a loss function, e.g.,
- $J = 1 - p(w_{-t} | w_t)$
- We look at many positions t in a big language corpus
- We keep adjusting the vector representations of words to minimize this loss

Idea: Directly learn low-dimensional word vectors based on ability to predict

- Old idea: Learning representations by back-propagating errors. (Rumelhart et al., 1986)
- A neural probabilistic language model (Bengio et al., 2003)
- NLP (almost) from Scratch (Collobert & Weston, 2008)
- A recent, even simpler and faster model: word2vec (Mikolov et al. 2013) → intro now
- The GloVe model from Stanford (Pennington, Socher, and Manning 2014) connects back to matrix factorization
- Per-token representations: Deep contextual word representations: ELMo, ULMfit, **BERT**

Non-linear
and slow

Fast
bilinear
models

Current
state of
the art

Word2vec is a family of algorithms

[Mikolov et al. 2013]

Predict between every word and its context words!

Two algorithms

- 1. Skip-grams (SG)**

Predict context words given target (position independent)

- 2. Continuous Bag of Words (CBOW)**

Predict target word from bag-of-words context

Two (moderately efficient) training methods

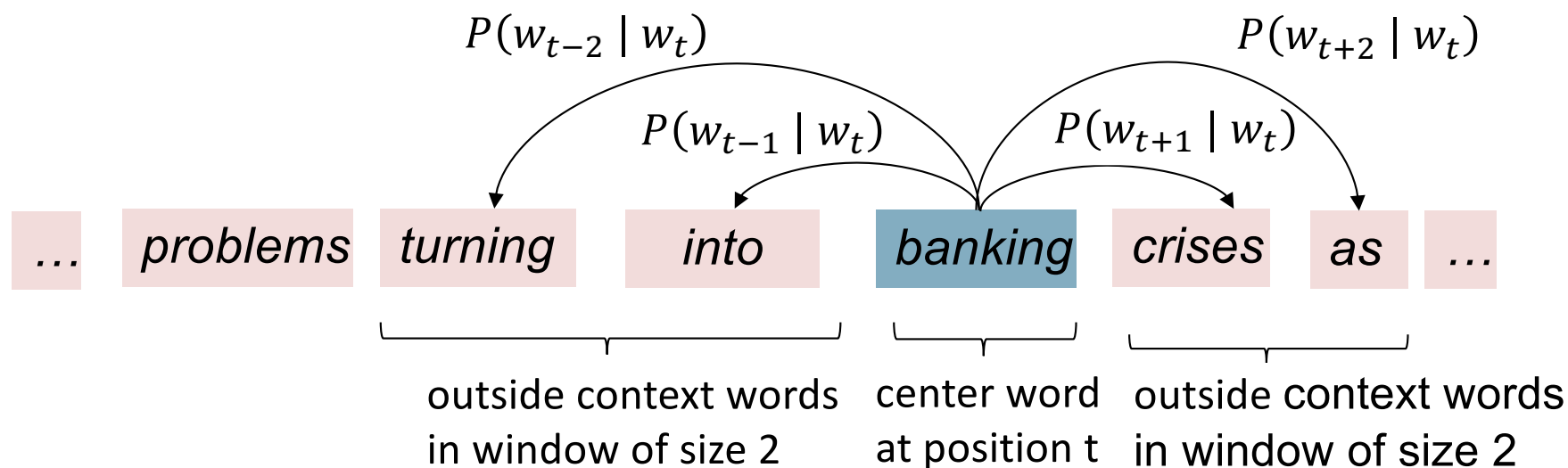
1. Hierarchical softmax

2. Negative sampling

- 3. Naïve softmax**

Word2Vec Skip-gram Overview

- Example windows and process for computing $P(w_{t+j} | w_t)$



Word2vec: objective function

For each position $t = 1, \dots, T$, predict context words within a window of fixed size m , given center word w_j .

Likelihood =

$$L(\theta) = \prod_{t=1}^T \prod_{\substack{-m \leq j \leq m \\ j \neq 0}} P(w_{t+j} | w_t; \theta)$$

θ is all variables
to be optimized

Sometimes called *cost* or *loss* function

The **objective function** $J(\theta)$ is the (average) negative log likelihood:

$$J(\theta) = -\frac{1}{T} \log L(\theta) = -\frac{1}{T} \sum_{t=1}^T \sum_{\substack{-m \leq j \leq m \\ j \neq 0}} \log P(w_{t+j} | w_t; \theta)$$

Minimizing objective function \Leftrightarrow Maximizing predictive accuracy

Word2vec: objective function

- We want to minimize the objective function:

$$J(\theta) = -\frac{1}{T} \sum_{t=1}^T \sum_{\substack{-m \leq j \leq m \\ j \neq 0}} \log P(w_{t+j} | w_t; \theta)$$

- Question: How to calculate $P(w_{t+j} | w_t; \theta)$?
- Answer: We will use two vectors per word w :
 - v_w when w is a center word
 - u_w when w is a context word
- Then for a center word c and a context word o :

$$P(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w \in V} \exp(u_w^T v_c)}$$

Word2vec: prediction function

Exponentiation makes anything positive

Dot product compares similarity of o and c .

$$u^T v = u \cdot v = \sum_{i=1}^n u_i v_i$$

Larger dot product = larger probability

$$P(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w \in V} \exp(u_w^T v_c)}$$

Normalize over entire vocabulary to give probability distribution

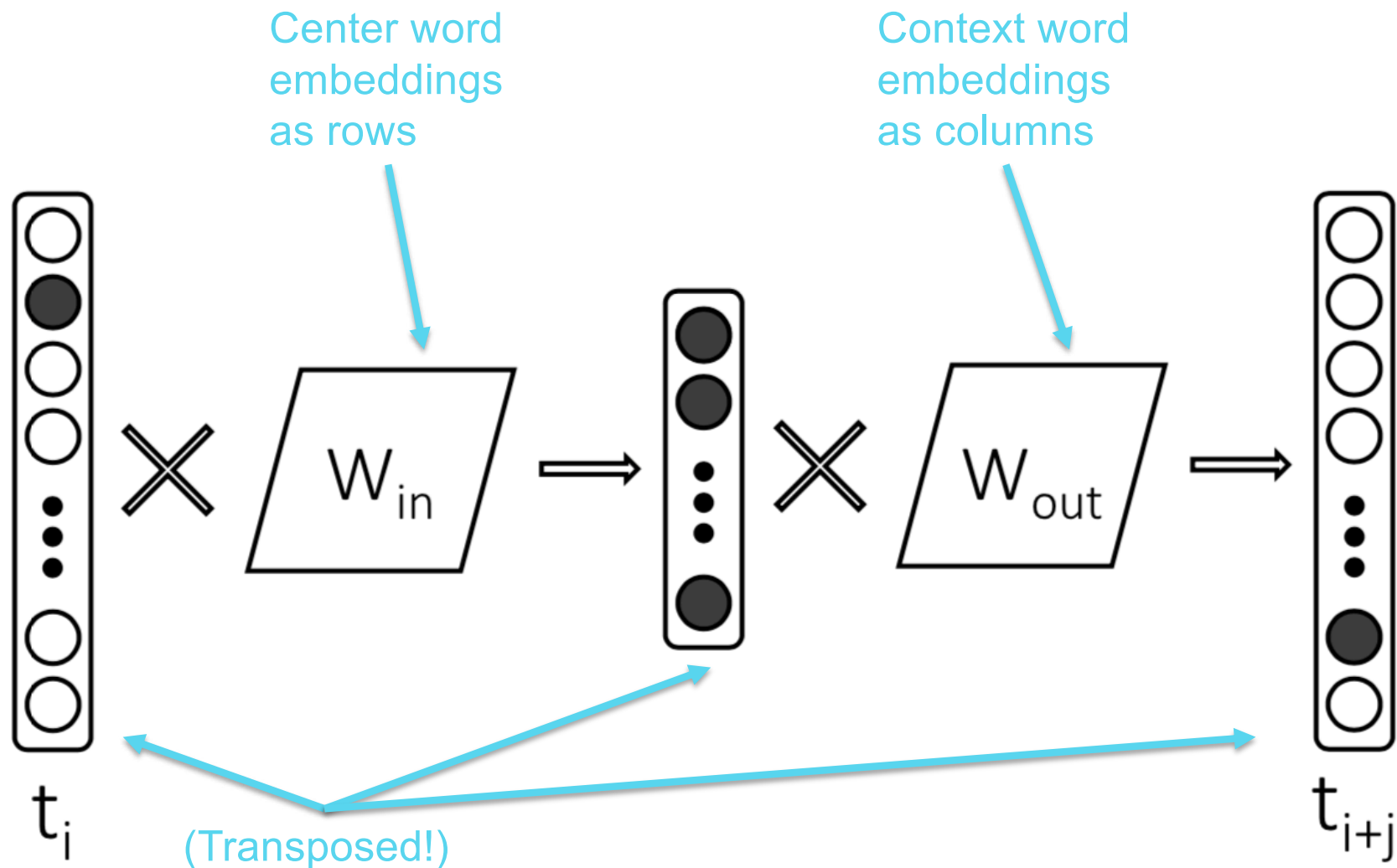
- This is an example of the **softmax function** $\mathbb{R}^n \rightarrow (0,1)^n$

$$\text{softmax}(x_i) = \frac{\exp(x_i)}{\sum_{j=1}^n \exp(x_j)} = p_i$$

Open region

- The softmax function maps arbitrary values x_i to a probability distribution p_i
 - “max” because amplifies probability of largest x_i
 - “soft” because still assigns some probability to smaller x_i
 - Frequently used in neural networks/Deep Learning

Word2vec: 2 matrices of parameters



To learn good word vectors: Compute **all** vector gradients!

- We often define the set of **all** parameters in a model in terms of one long vector θ

- In our case with d -dimensional vectors and V many words:

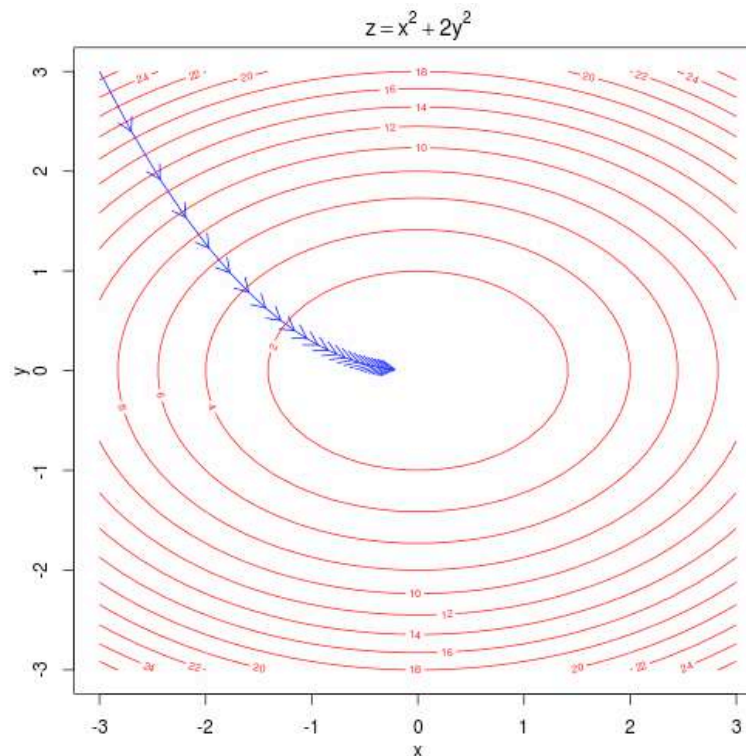
$$\theta = \begin{bmatrix} v_{aardvark} \\ v_a \\ \vdots \\ v_{zebra} \\ u_{aardvark} \\ u_a \\ \vdots \\ u_{zebra} \end{bmatrix} \in \mathbb{R}^{2dV}$$

- We then optimize these parameters

Note: Every word has two vectors! Makes it simpler!

Intuition of how to minimize loss for a simple function over two parameters

We start at a random point and walk in the steepest direction, which is given by the derivative of the function



Contour lines show points of equal value of objective function

Descending by using derivatives

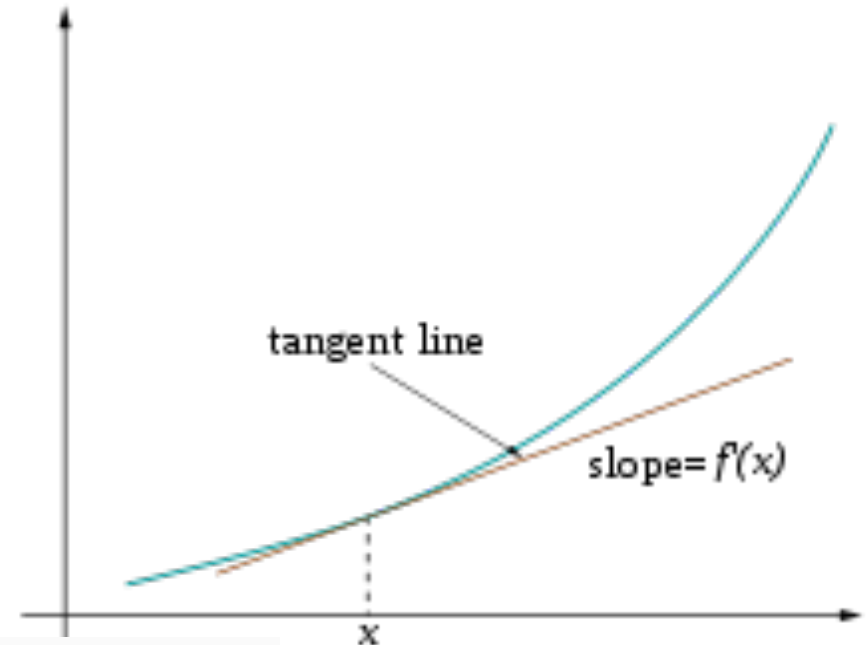
We will minimize a cost function by gradient descent

Trivial example: (from Wikipedia)

Find a local minimum of the function

$$f(x) = x^4 - 3x^3 + 2,$$

with derivative $f'(x) = 4x^3 - 9x^2$



```
x_old = 0
x_new = 6 # The algorithm starts at x=6
eps = 0.01 # step size
precision = 0.00001

def f_derivative(x):
    return 4 * x**3 - 9 * x**2

while abs(x_new - x_old) > precision:
    x_old = x_new
    x_new = x_old - eps * f_derivative(x_old)

print("Local minimum occurs at", x_new)
```

Subtracting a fraction of the gradient moves you towards the minimum!

Vanilla Gradient Descent Code

$$\theta^{new} = \theta^{old} - \alpha \nabla_{\theta} J(\theta)$$

```
while True:  
    theta_grad = evaluate_gradient(J, corpus, theta)  
    theta = theta - alpha * theta_grad
```

Stochastic Gradient Descent

- But Corpus may have 40B tokens and windows
- You would wait a very long time before making a single update!
- **Very** bad idea for pretty much all neural nets!
- Instead: We update parameters after each window t
→ Stochastic gradient descent (SGD)

$$\theta^{new} = \theta^{old} - \alpha \nabla_{\theta} J_t(\theta)$$

```
while True:
    window = sample_window(corpus)
    theta_grad = evaluate_gradient(J, window, theta)
    theta = theta - alpha * theta_grad
```

Working out how to optimize a neural network is really all the chain rule!

Chain rule! If $y = f(u)$ and $u = g(x)$, i.e. $y = f(g(x))$, then:

$$\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx} = \frac{df(u)}{du} \frac{dg(x)}{dx}$$

Simple example: $\frac{dy}{dx} = \frac{d}{dx} 5(x^3 + 7)^4$

$$y = f(u) = 5u^4$$

$$u = g(x) = x^3 + 7$$

$$\frac{dy}{du} = 20u^3$$

$$\frac{du}{dx} = 3x^2$$

$$\frac{dy}{dx} = 20(x^3 + 7)^3 \cdot 3x^2$$

Objective Function

$$\text{Maximize } J'(\theta) = \prod_{t=1}^T \prod_{\substack{-m \leq j \leq m \\ j \neq 0}} p(w'_{t+j} | w_t; \theta)$$

Or minimize
neg. log
likelihood

$$J(\theta) = -\frac{1}{T} \sum_{t=1}^T \sum_{\substack{-m \leq j \leq m \\ j \neq 0}} \log p(w'_{t+j} | w_t)$$

[negate to minimize;
log is monotone]

↑
text
length

↑
window
size

where

$$p(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w=1}^V \exp(u_w^T v_c)}$$

word IDs ↗ ↘

We now take derivatives to work out minimum

Each word type
(vocab entry)
has two word
representations:
as center word
and context word

$$\frac{\partial}{\partial v_c} \log \frac{\exp(u_0^T v_c)}{\sum_{w=1}^V \exp(u_w^T v_c)}$$

$$= \underbrace{\frac{\partial}{\partial v_c} \log \exp(u_0^T v_c)}_{(1)} - \underbrace{\frac{\partial}{\partial v_c} \log \sum_{w=1}^V \exp(u_w^T v_c)}_{(2)}$$

$$(1) \quad \frac{\partial}{\partial v_c} \underbrace{\log \exp(u_0^T v_c)}_{\text{inverses}} = \frac{\partial}{\partial v_c} u_0^T v_c = u_0$$

Vector!
Not high school single variable calculus

You can do things one variable at a time, and this may be helpful when things get gnarly.

$$\forall j \quad \frac{\partial}{\partial (v_c)_j} u_0^T v_c = \frac{\partial}{\partial (v_c)_j} \sum_{i=1}^d (u_0)_i (v_c)_i = (u_0)_j$$

Each term is zero except when $i=j$

$$\textcircled{2} \frac{\partial}{\partial v_c} \log \underbrace{\sum_{w=1}^v \exp(u_w^T v_c)}_f \quad \underbrace{z = g(v_c)}$$

$$= \frac{1}{\sum_{w=1}^v \exp(u_w^T v_c)}$$

$$\frac{\partial}{\partial v_c} f(g(v_c)) = \frac{\partial f}{\partial z} \cdot$$

$$= \frac{1}{\sum_{w=1}^v \exp(u_w^T v_c)}$$

$$\frac{\partial}{\partial v_c} \sum_{x=1}^v \exp(u_x^T v_c)$$

Important to change index

$$\frac{\partial z}{\partial v_c}$$

Use chain rule

$$\left(\sum_{x=1}^v \frac{\partial}{\partial v_c} \underbrace{\exp(u_x^T v_c)}_f \right) \quad \underbrace{z = g(v_c)}$$

Move deriv inside sum

$$\left(\sum_{x=1}^v \exp(u_x^T v_c) \frac{\partial}{\partial v_c} u_x^T v_c \right)$$

Chain rule

$$\left(\sum_{x=1}^v \exp(u_x^T v_c) u_x \right)$$

$$\frac{\partial}{\partial v_c} \log(p(o|c)) = u_o - \frac{1}{\sum_{w=1}^V \exp(u_w^T v_c)} \cdot \left(\sum_{x=1}^V \exp(u_x^T v_c) u_x \right)$$

$$= u_o - \sum_{x=1}^V \frac{\exp(u_x^T v_c)}{\sum_{w=1}^V \exp(u_w^T v_c)} u_x$$

Distribute
term
across sum

$$= u_o - \underbrace{\sum_{x=1}^V p(x|c)}_{\text{this is an expectation: average over all context vectors weighted by their probability}} u_x$$

= observed - expected

This is an expectation:
average over all
context vectors weighted
by their probability

This is just the derivatives for the center vector parameters
Also need derivatives for output vector parameters
(they're similar)
Then we have derivative w.r.t. all parameters and can minimize

Linear Relationships in word2vec

These representations are *very good* at encoding **similarity** and **dimensions of similarity**!

- Analogies testing dimensions of similarity can be solved quite well just by doing vector subtraction in the embedding space

Syntactically

- $x_{apple} - x_{apples} \approx x_{car} - x_{cars} \approx x_{family} - x_{families}$
- Similarly for verb and adjective morphological forms

Semantically (Semeval 2012 task 2)

- $x_{shirt} - x_{clothing} \approx x_{chair} - x_{furniture}$
- $x_{king} - x_{man} \approx x_{queen} - x_{woman}$

Word Analogies

Test for linear relationships, examined by Mikolov et al.

a:b :: c:?



$$d = \arg \max_x \frac{(w_b - w_a + w_c)^T w_x}{\|w_b - w_a + w_c\|}$$

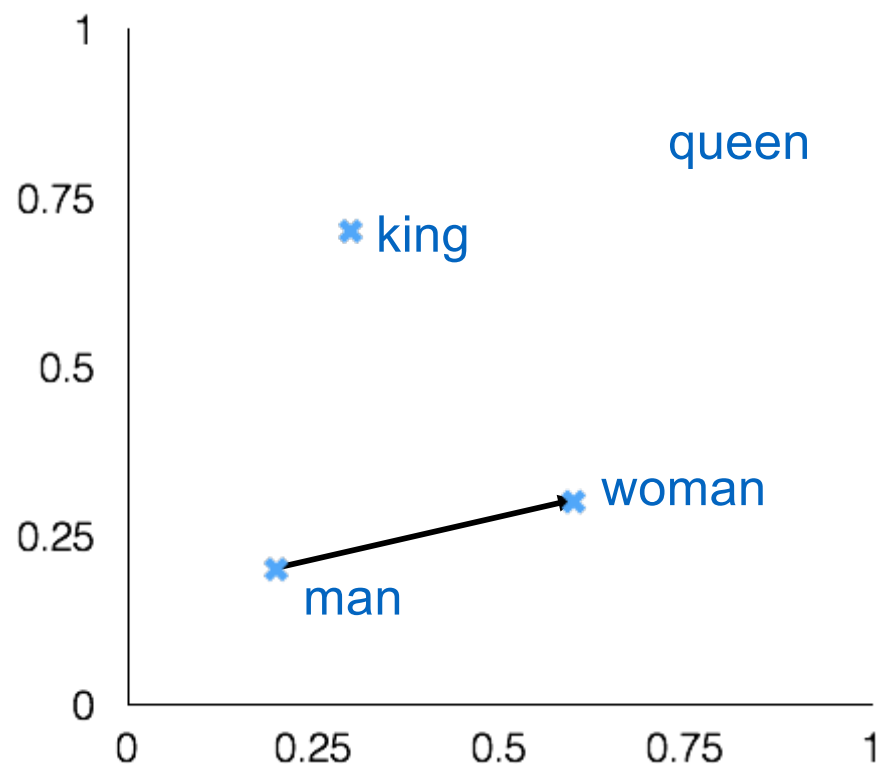
man:woman :: king:?

+ king [0.30 0.70]

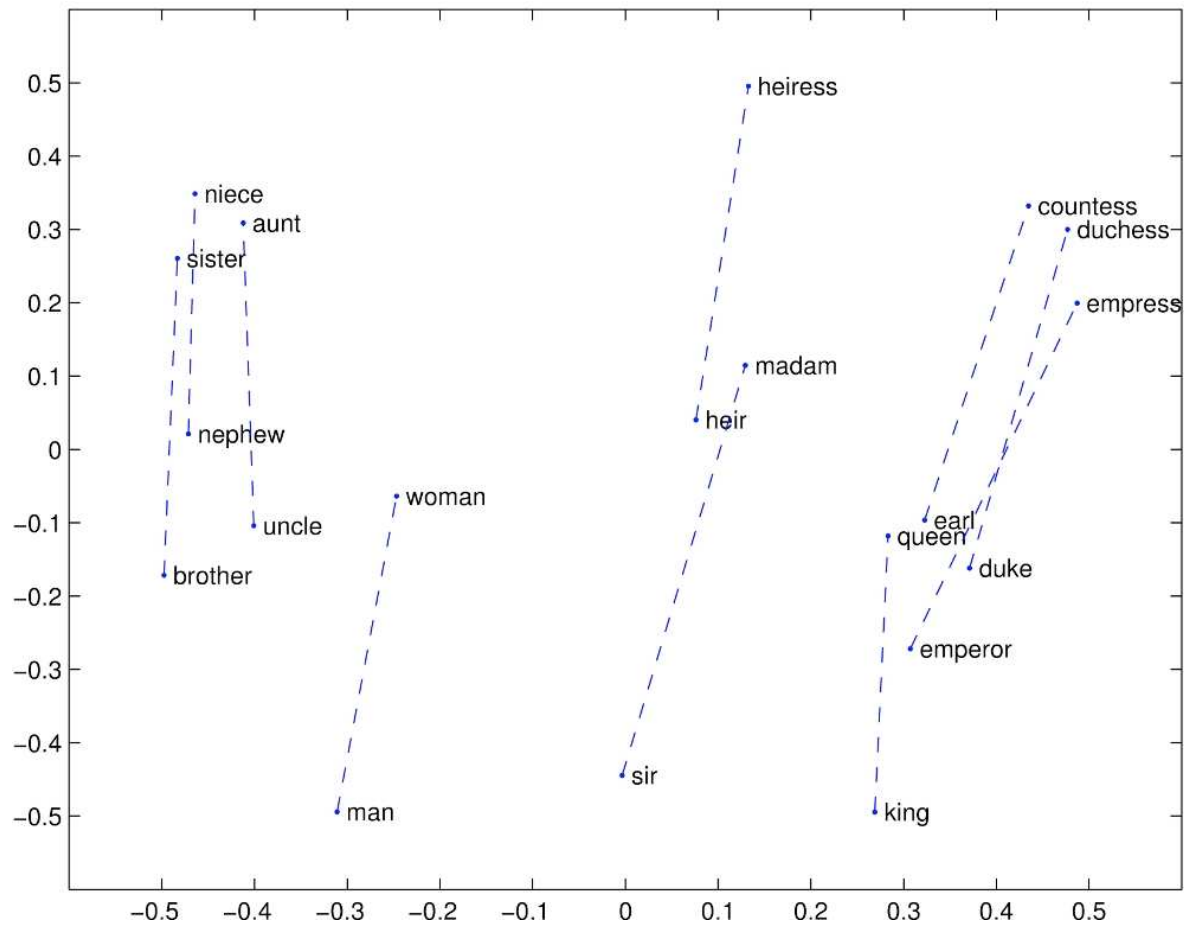
- man [0.20 0.20]

+ woman [0.60 0.30]

queen [0.70 0.80]

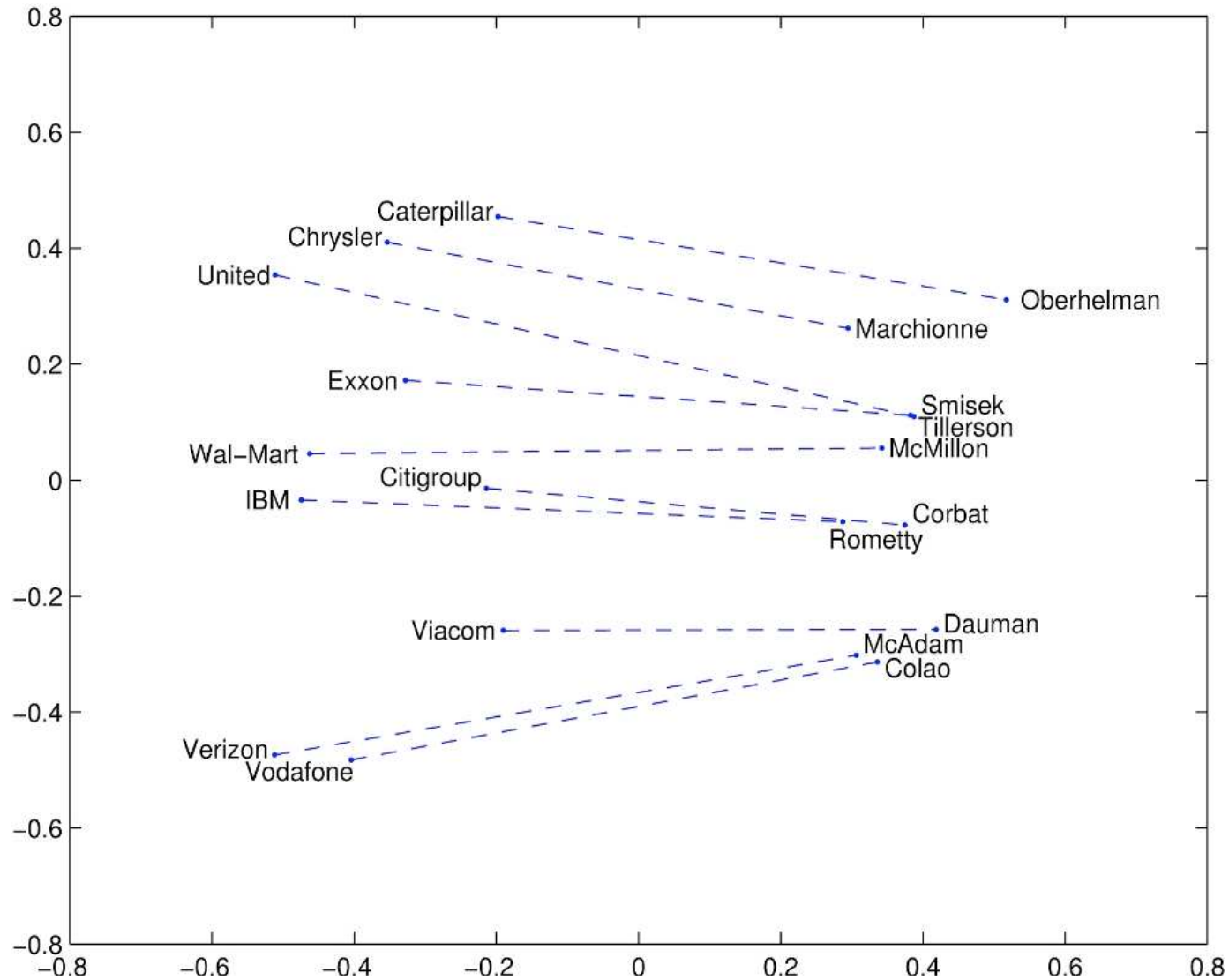


GloVe Visualizations

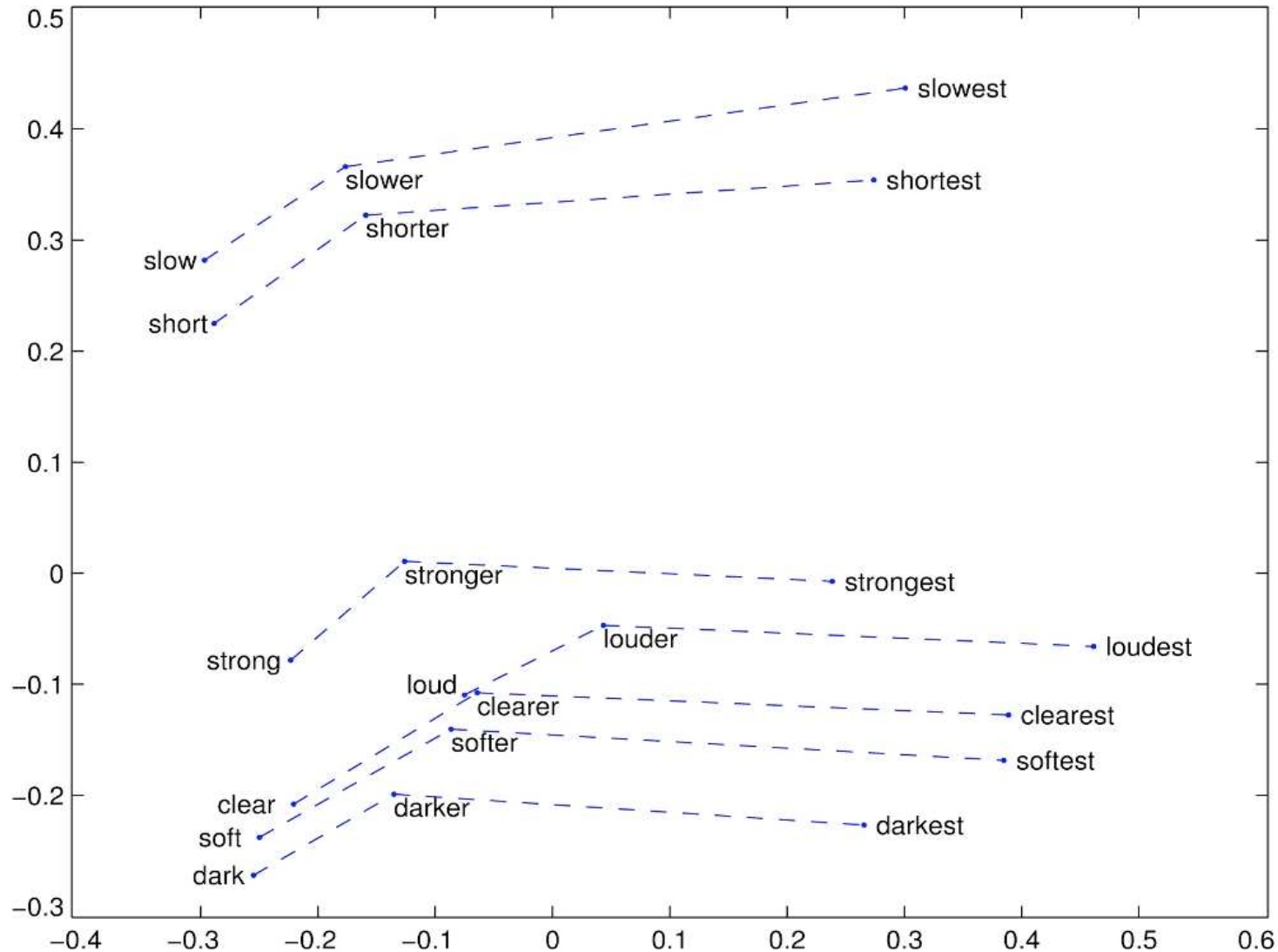


<http://nlp.stanford.edu/projects/glove/>

Glove Visualizations: Company - CEO



Glove Visualizations: Superlatives



Application to Information Retrieval

Application is just beginning – we’re “at the end of the early years”

- Google’s RankBrain – little is publicly known
 - Bloomberg article by Jack Clark (Oct 26, 2015):
<http://www.bloomberg.com/news/articles/2015-10-26/google-turning-its-lucrative-web-search-over-to-ai-machines>
 - A result reranking system. “3rd most valuable ranking signal”
 - But note: more of the potential value is in the tail?
- New SIGIR Neu-IR workshop series (2016 on)



Neu-IR (2016)
The Neural Information Retrieval Workshop @ SIGIR
Pisa, Tuscany, Italy on 21st July, 2016
research.microsoft.com/neuir2016

An application to information retrieval

Nalisnick, Mitra, Craswell & Caruana. 2016. Improving Document Ranking with Dual Word Embeddings. *WWW 2016 Companion*. <http://research.microsoft.com/pubs/260867/pp1291-Nalisnick.pdf>

Mitra, Nalisnick, Craswell & Caruana. 2016. A Dual Embedding Space Model for Document Ranking. [arXiv:1602.01137](https://arxiv.org/abs/1602.01137) [cs.IR]

Builds on BM25 model idea of “aboutness”

- Not just term repetition indicating aboutness
- Relationship between query terms and *all* terms in the document indicates aboutness (BM25 uses only query terms)

Makes clever argument for different use of word and context vectors in word2vec’s CBOW/SGNS or GloVe

Modeling document aboutness: Results from a search for Albuquerque

d_1

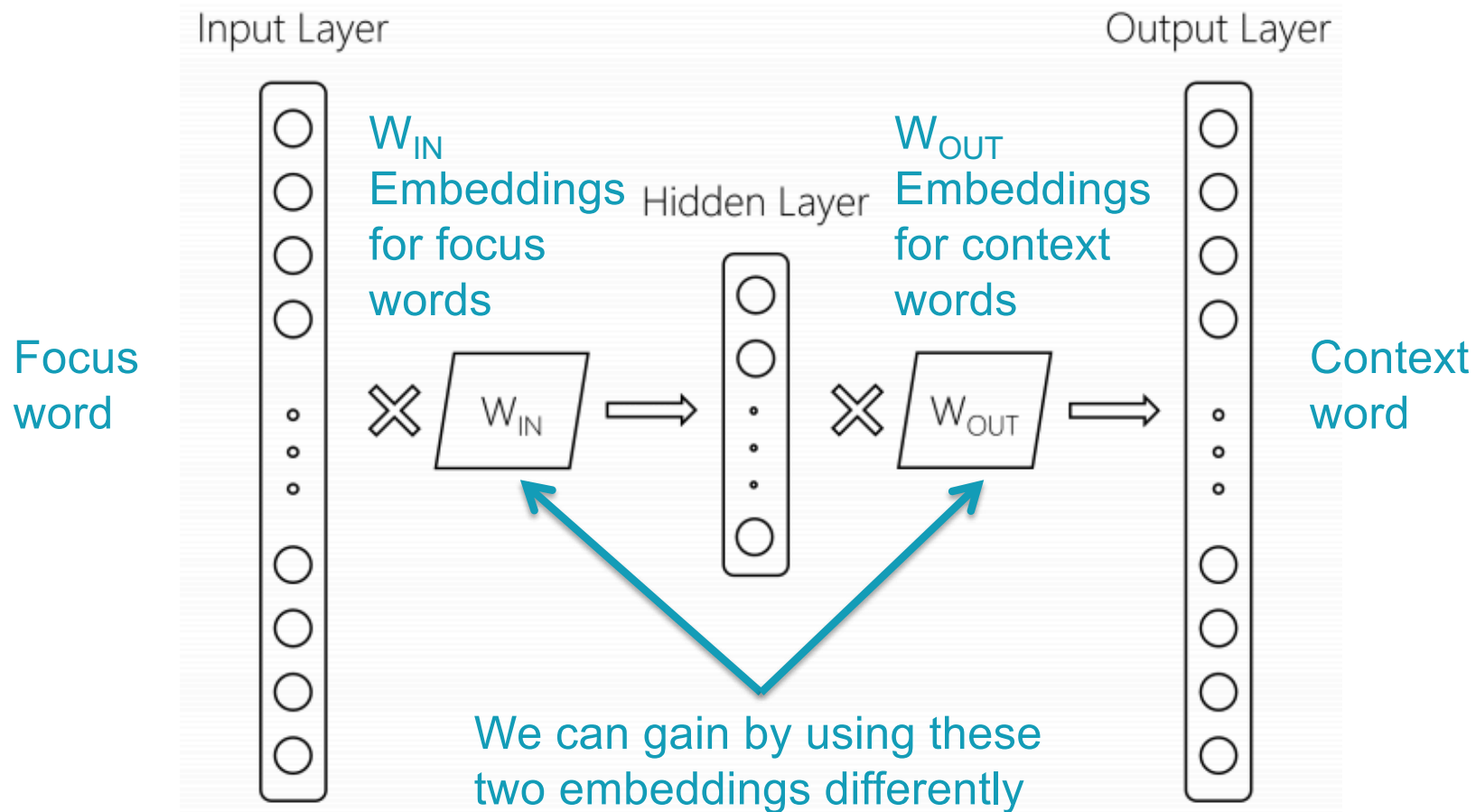
Allen suggested that they could program a BASIC interpreter for the device; after a call from Gates claiming to have a working interpreter, MITS requested a demonstration. Since they didn't actually have one, Allen worked on a simulator for the Altair while Gates developed the interpreter. Although they developed the interpreter on a simulator and not the actual device, the interpreter worked flawlessly when they demonstrated the interpreter to MITS in Albuquerque, New Mexico in March 1975; MITS agreed to distribute it, marketing it as Altair BASIC.

d_2

Albuquerque is the most populous city in the U.S. state of New Mexico. The high-altitude city serves as the county seat of Bernalillo County, and it is situated in the central part of the state, straddling the Rio Grande. The city population is 557,169 as of the July 1, 2014, population estimate from the United States Census Bureau, and ranks as the 32nd-largest city in the U.S. The Metropolitan Statistical Area (or MSA) has a population of 902,797 according to the United States Census Bureau's most recently available estimate for July 1, 2013.

Using 2 word embeddings

word2vec model with 1 word of context



Using 2 word embeddings

| yale | | seahawks | |
|-------------|-------------|-----------------|------------|
| IN-IN | IN-OUT | IN-IN | IN-OUT |
| yale | yale | seahawks | seahawks |
| harvard | faculty | 49ers | highlights |
| nyu | alumni | broncos | jerseys |
| cornell | orientation | packers | tshirts |
| tulane | haven | nfl | seattle |
| tufts | graduate | steelers | hats |

Dual Embedding Space Model (DESM)

- Simple model
- A document is represented by the centroid of its word vectors

$$\bar{\mathbf{D}} = \frac{1}{|D|} \sum_{\mathbf{d}_j \in D} \frac{\mathbf{d}_j}{\|\mathbf{d}_j\|}$$

- Query-document similarity is average over query words of cosine similarity

$$DESM(Q, D) = \frac{1}{|Q|} \sum_{\mathbf{q}_i \in Q} \frac{\mathbf{q}_i^T \bar{\mathbf{D}}}{\|\mathbf{q}_i\| \|\bar{\mathbf{D}}\|}$$

Dual Embedding Space Model (DESM)

- What works best is to use the OUT vectors for the document and the IN vectors for the query

$$DESM_{IN-OUT}(Q, D) = \frac{1}{|Q|} \sum_{q_i \in Q} \frac{q_{IN,i}^T \overline{D_{OUT}}}{\|q_{IN,i}\| \|\overline{D_{OUT}}\|}$$

- This way similarity measures *aboutness* – words that appear with this word – which is more useful in this context than *(distributional) semantic similarity*

Experiments

- Train word2vec from either
 - 600 million Bing queries
 - 342 million web document sentences
- Test on 7,741 randomly sampled Bing queries
 - 5 level eval (Perfect, Excellent, Good, Fair, Bad)
- Two approaches
 1. Use DESM model to rerank top results from BM25
 2. Use DESM alone or a mixture model of it and BM25

$$MM(Q, D) = \alpha DESM(Q, D) + (1 - \alpha) BM25(Q, D)$$
$$\alpha \in \mathbb{R}, 0 \leq \alpha \leq 1$$

Results – reranking k -best list

| | Explicitly Judged Test Set | | |
|-------------------------------------|----------------------------|---------------|---------------|
| | NDCG@1 | NDCG@3 | NDCG@10 |
| BM25 | 23.69 | 29.14 | 44.77 |
| LSA | 22.41* | 28.25* | 44.24* |
| DESM (IN-IN, trained on body text) | 23.59 | 29.59 | 45.51* |
| DESM (IN-IN, trained on queries) | 23.75 | 29.72 | 46.36* |
| DESM (IN-OUT, trained on body text) | 24.06 | 30.32* | 46.57* |
| DESM (IN-OUT, trained on queries) | 25.02* | 31.14* | 47.89* |

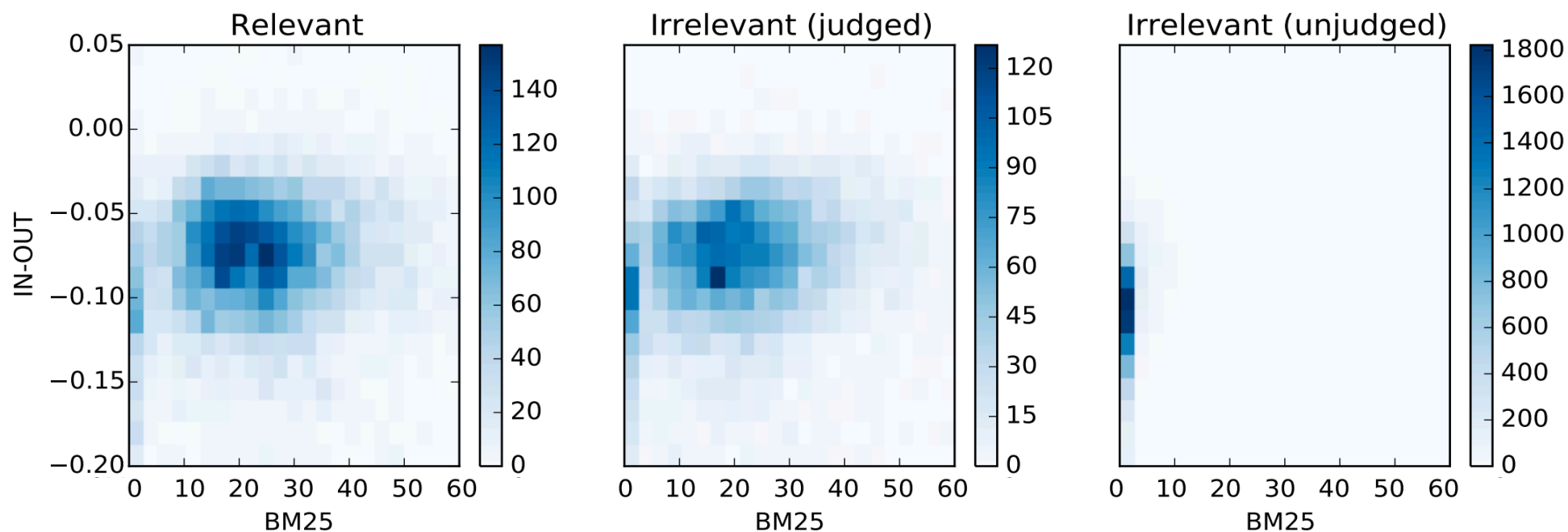
Pretty decent gains – e.g., 2% for NDCG@3

Gains are bigger for model trained on queries than docs

Results – whole ranking system

| | Explicitly Judged Test Set | | |
|--|----------------------------|---------------|---------------|
| | NDCG@1 | NDCG@3 | NDCG@10 |
| BM25 | 21.44 | 26.09 | 37.53 |
| LSA | 04.61* | 04.63* | 04.83* |
| DESM (IN-IN, trained on body text) | 06.69* | 06.80* | 07.39* |
| DESM (IN-IN, trained on queries) | 05.56* | 05.59* | 06.03* |
| DESM (IN-OUT, trained on body text) | 01.01* | 01.16* | 01.58* |
| DESM (IN-OUT, trained on queries) | 00.62* | 00.58* | 00.81* |
| BM25 + DESM (IN-IN, trained on body text) | 21.53 | 26.16 | 37.48 |
| BM25 + DESM (IN-IN, trained on queries) | 21.58 | 26.20 | 37.62 |
| BM25 + DESM (IN-OUT, trained on body text) | 21.47 | 26.18 | 37.55 |
| BM25 + DESM (IN-OUT, trained on queries) | 21.54 | 26.42* | 37.86* |

A possible explanation



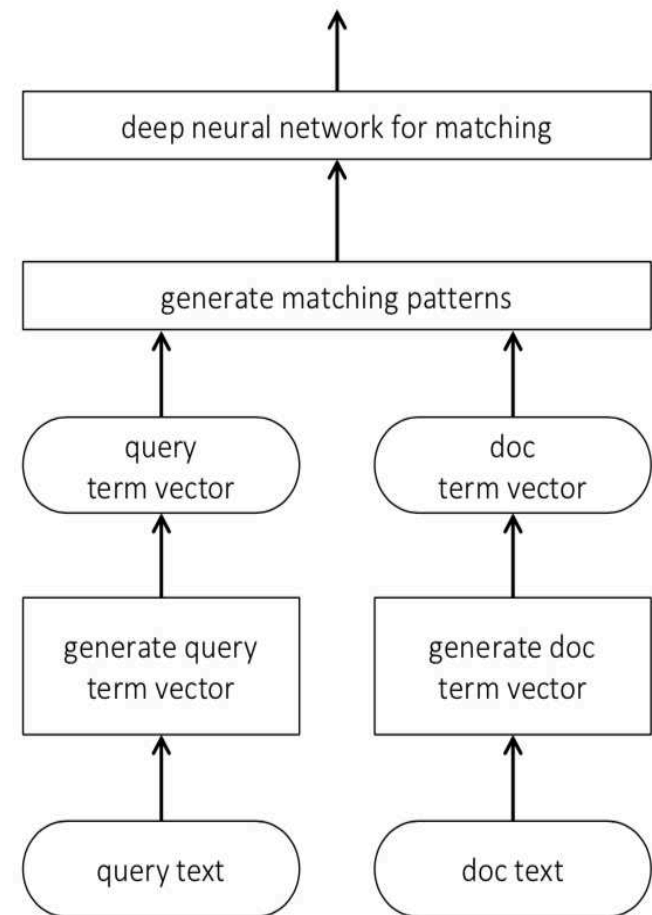
IN-OUT has some ability to prefer Relevant to close-by (judged) non-relevant, but it's scores induce too much noise vs. BM25 to be usable alone

DESM conclusions

- DESM is a weak ranker but effective at finding subtler similarities/aboutness
- It is effective at, but only at, reranking at least somewhat relevant documents
 - For example, DESM can confuse Oxford and Cambridge
 - Bing rarely makes an Oxford/Cambridge mistake!

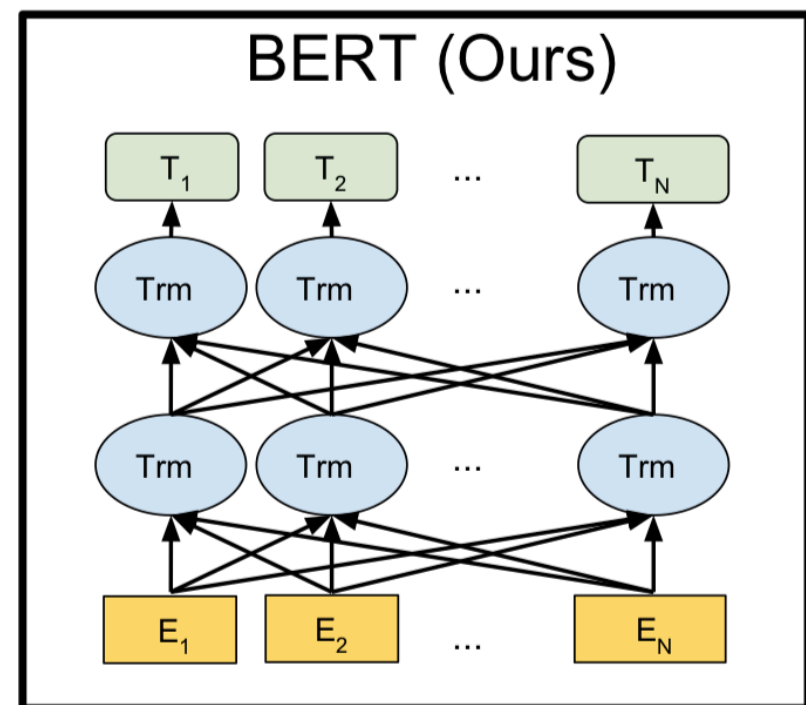
What else can neural nets do in IR?

- Use a neural network as a supervised reranker
- Assume a query and document embedding network (as we have discussed)
- Assume you have (q,d,rel) relevance data
- Learn a neural network (with supervised learning) to predict relevance of (q,d) pair
- An example of “machine-learned relevance”, which we’ll talk about more next lecture

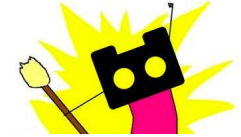


What else can neural nets do in IR?

- BERT: Devlin, Chang, Lee, Toutanova (2018)
- A deep transformer-based neural network
- Builds per-token (in context) representations
- Produces a query/document representation as well
- Or jointly embed query and document and ask for a retrieval score
- Incredibly effective!
- <https://arxiv.org/abs/1810.04805>



Summary: Embed all the things!



Word embeddings are the hot new technology (again!)

Lots of applications wherever knowing word context or similarity helps prediction:

- Synonym handling in search
- Document aboutness
- Ad serving
- Language models: from spelling correction to email response
- Machine translation
- Sentiment analysis
- ...

ONCE UPON A TIME IN THE...



ONCE UPON A TIME IN THE
Cozy Afternoon at Masaryk University



ONCE UPON A TIME IN THE
Cozy Afternoon at Masaryk University

QUESTION ANSWERING AND BEYOND



PROLOGUE:

CHAPTER 1:
INTRODUCTION

Information Need



Information Need

? Information Need



Information Need

? Information Need



When has X his birthday?
I suffer from Y every winter. How to prevent it?
Where to buy skiing equipment?

Information Need

? Information Need



Interact with world
To Know



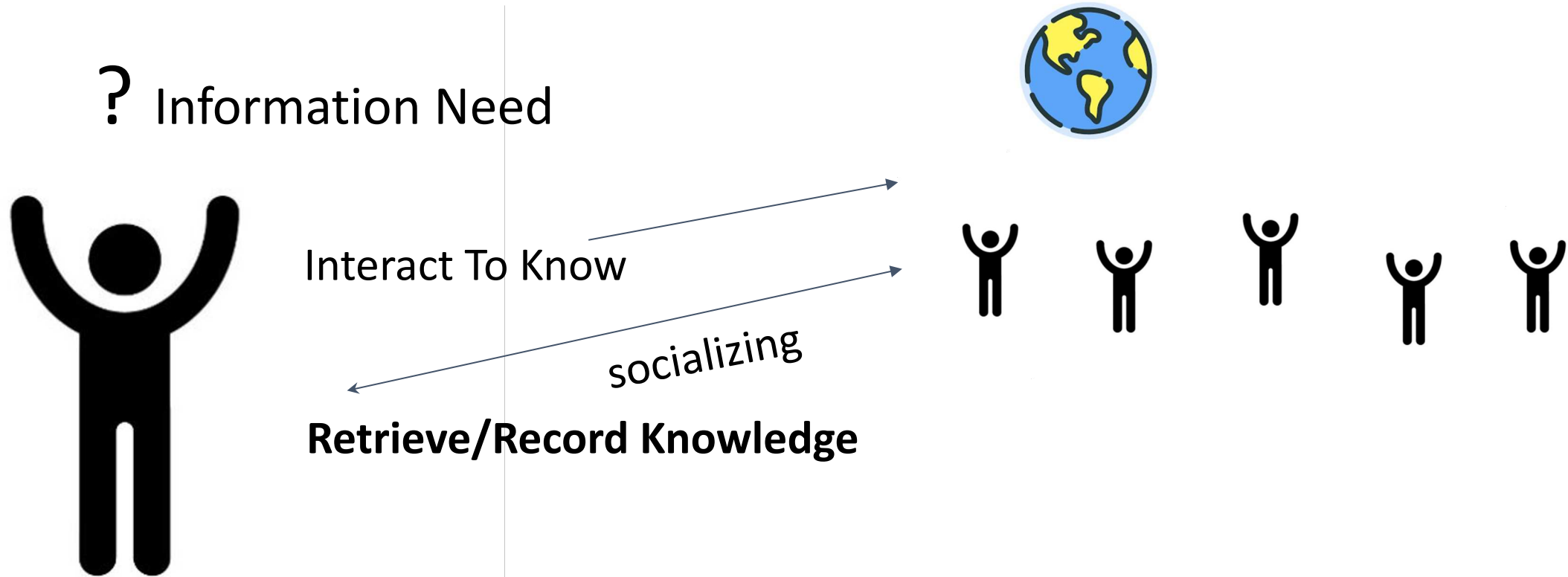
When has X his birthday?

I suffer from Y every winter. How to prevent it?

Where to buy skiing equipment?

What is the information need?

Information Need

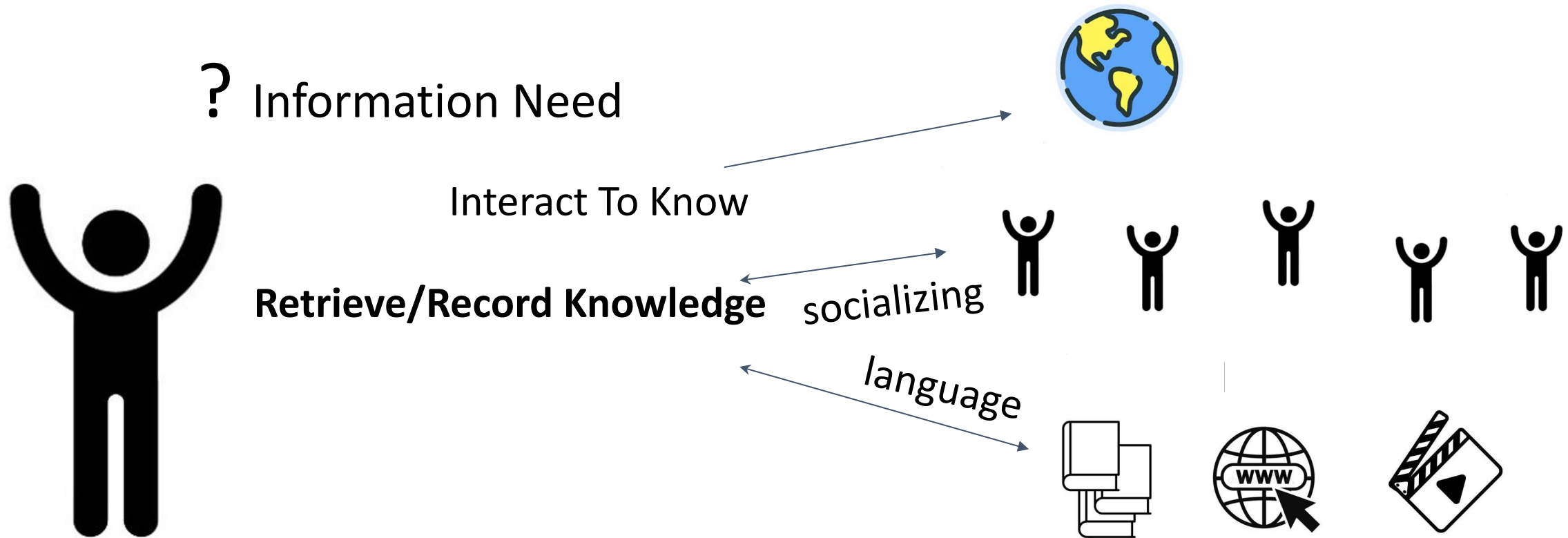


When has X his birthday?

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Where to buy skiing equipment?

Information Need



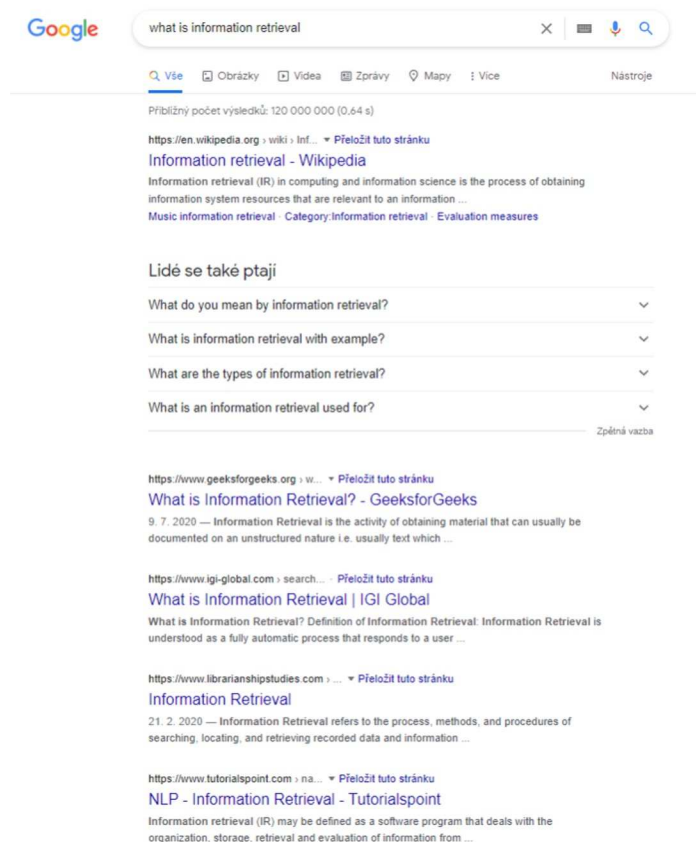
When has X his birthday?

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Where to buy skiing equipment?

Information Need

Traditional Information Retrieval Today



Research Desiderata

- Provide **answer**, if question requires factoid answer
- Provide **summary**, if question requires summary
- Provide **search result** if question requires listing
- Solve logic, if question requires **problem solving**
- Questions are often ambiguous, **disambiguate** via interaction
- Make models understand natural **language**, not humans learn model language

CHAPTER 2:
INFORMATION RETRIEVAL

Information Retrieval (IR)

Term “**Information Retrieval**” in literature. Example from MSMarco (Nguyen et al. 2016)

Q Will I qualify for OSAP if I'm new in Canada?

Selected Passages from Bing

“Visit the OSAP website for application deadlines. To get OSAP, you have to be eligible. You can apply using an online form, or you can print off the application forms. If you submit a paper application, you must pay an application fee. The online application is free.”
Source: <http://settlement.org/ontario/education/colleges-universities-and-institutes/financial-assistance-for-post-secondary-education/how-do-i-apply-for-the-ontario-student-assistance-program-osap/>

“To be eligible to apply for financial assistance from the Ontario Student Assistance Program (OSAP), you must be a: 1 Canadian citizen; 2 Permanent resident; or 3 Protected person/convention refugee with a Protected Persons Status Document (PPSD).”
Source: <http://settlement.org/ontario/education/colleges-universities-and-institutes/financial-assistance-for-post-secondary-education/who-is-eligible-for-the-ontario-student-assistance-program-osap/>

“You will not be eligible for a Canada-Ontario Integrated Student Loan, but can apply for a part-time loan through the Canada Student Loans program. There are also grants, bursaries and scholarships available for both full-time and part-time students.”
Source: <http://www.campusaccess.com/financial-aid/osap.html>

Query (often a list of keywords)



Task: distinguish between relevant/irrelevant documents

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Source: <http://www.campusaccess.com/financial-aid/osap.html>

Query (often a list of keywords)



Task: distinguish between relevant/irrelevant documents



The labels can be non-binary (relevance scores)



Is Information Retrieval Document Retrieval?

- Lets brainstorm, how else can we retrieve information?

Question Answering (QA)

- A set of problems related to drawing conclusions from data (example from MSMarco)

Q Will I qualify for OSAP if I'm new in Canada?

Selected Passages from Bing

"Visit the OSAP website for application deadlines. To get OSAP, you have to be eligible. You can apply using an online form, or you can print off the application forms. If you submit a paper application, you must pay an application fee. The online application is free."
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"To be eligible to apply for financial assistance from the Ontario Student Assistance Program (OSAP), you must be a: 1 Canadian citizen; 2 Permanent resident; or 3 Protected person/convention refugee with a Protected Persons Status Document (PPSD)."
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Source: <http://www.campusaccess.com/financial-aid/osap.html>

Answer
No. You won't qualify.

← Question (in natural language)

← Provided document(s)

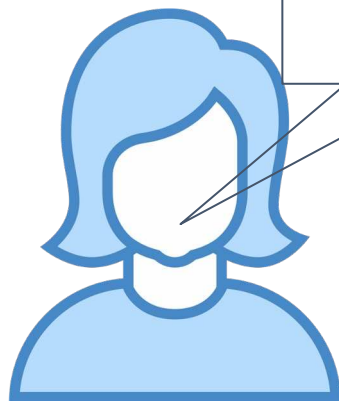
← Task: provide Answer



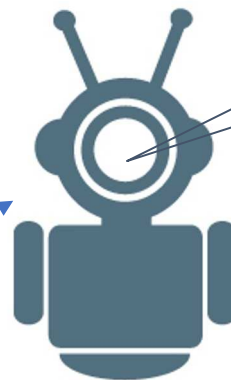
Question Answering (QA)

What is question asking about?

- facts?
- open-ended?
- chit-chat?
- math?
- multi-answer/multihop question?



Who is Jožko Mrkvička?



A fictional character in colloquial Slovak, whose name is used to denote an ordinary average citizen

What answer is expected?

- factoid?
- open-ended?
- chit-chat?
- CODE?
- **no-answer?**
- **respond with clarifying question to ambiguous question?**

Extractive QA

The first recorded travels by Europeans to China and back date from this time. The most famous traveler of the period was the Venetian Marco Polo, whose account of his trip to "Cambaluc," the capital of the Great Khan, and of life there astounded the people of Europe. The account of his travels, *Il milione* (or, *The Million*, known in English as the *Travels of Marco Polo*), appeared about the year 1299. Some argue over the accuracy of Marco Polo's accounts due to the lack of mentioning the Great Wall of China, tea houses, which would have been a prominent sight since Europeans had yet to adopt a tea culture, as well the practice of foot binding by the women in capital of the Great Khan. Some suggest that Marco Polo acquired much of his knowledge **through contact with Persian traders** since many of the places he named were in Persian.

How did some suspect that Polo learned about China instead of by actually visiting it?

Answer: through contact with Persian traders

Exact Match measures the percentage of predictions that match at least one of the ground truth answers exactly

of correctly answered questions

of all questions

Extractive QA

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(macro)**F1** measures the average overlap between the prediction and ground truth answer.

Prediction and ground truth are treated as bags of tokens and their F1 is computed.

Usually a maximum F1 over all of the ground truth answers for a given question is taken, and the result is an average over all of the questions.

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- Ground truth answer = {cat named kitty}

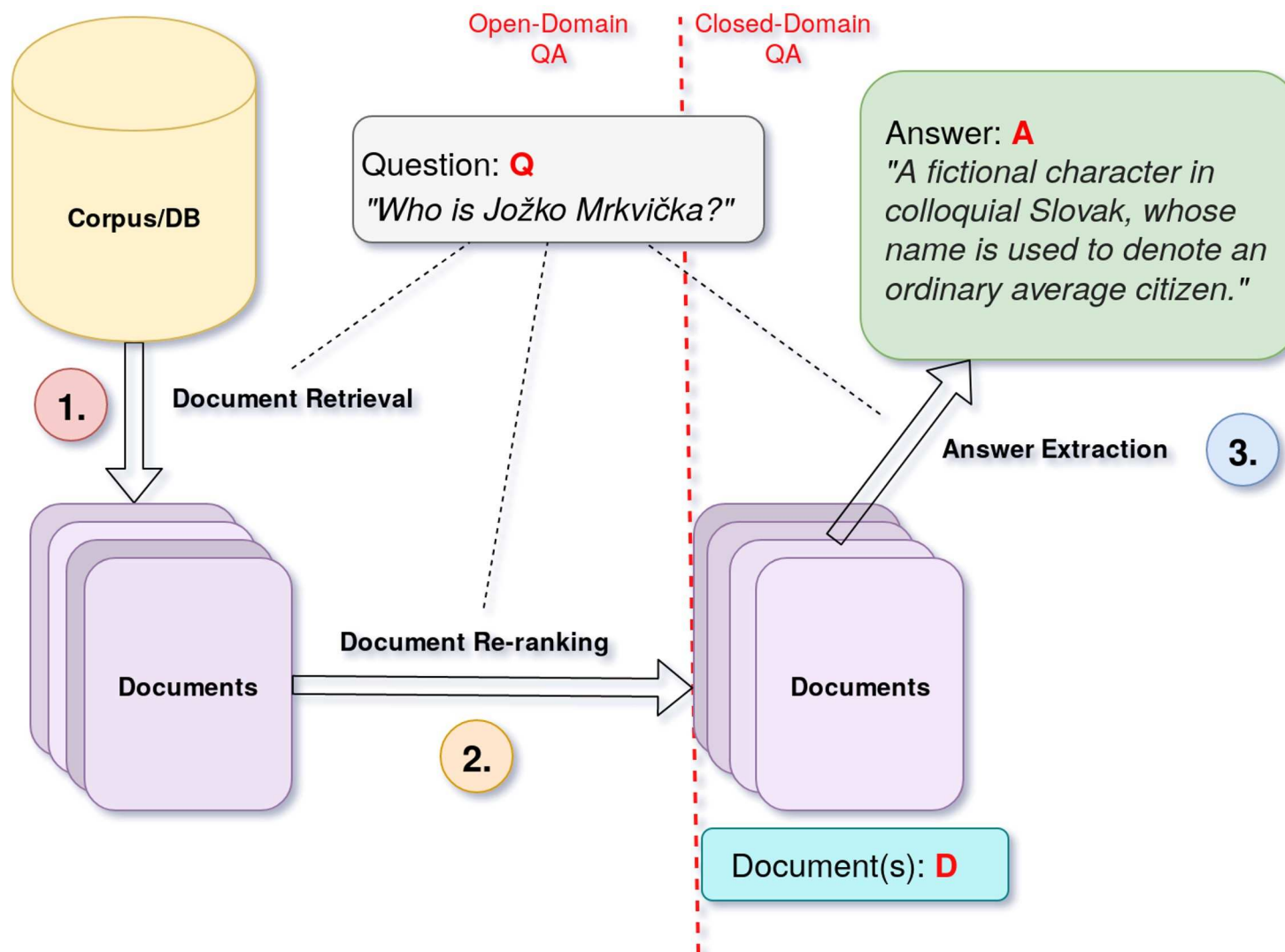
- Predicted answer = {cat named }

- $precision = \frac{\# \text{ of same tokens}}{\text{length of prediction}} = \frac{2}{2}$

- $recall = \frac{\# \text{ of same tokens}}{\text{length of ground truth}} = \frac{2}{3}$

- $F1 = 2 * \frac{precision * recall}{precision + recall} = 2 * \frac{\frac{2}{2} * \frac{2}{3}}{\frac{2}{2} + \frac{2}{3}}$

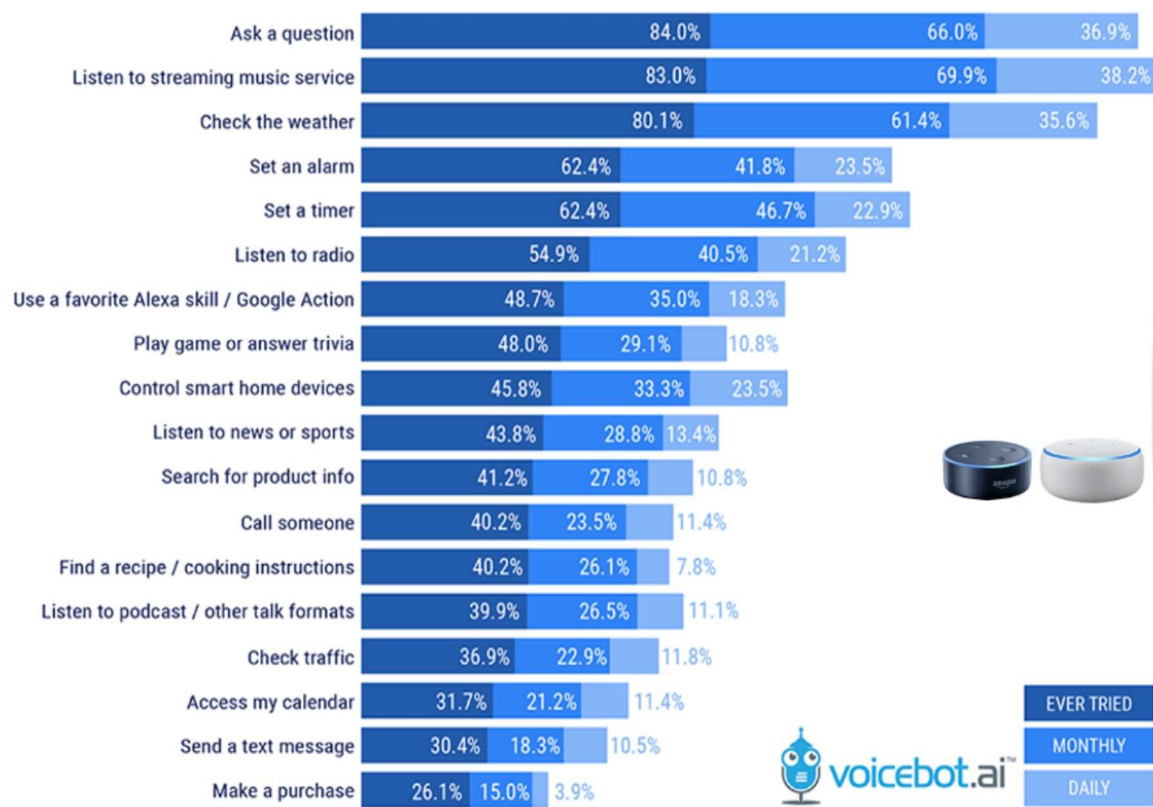
When Document Retrieval meets QA



Open-domain QA

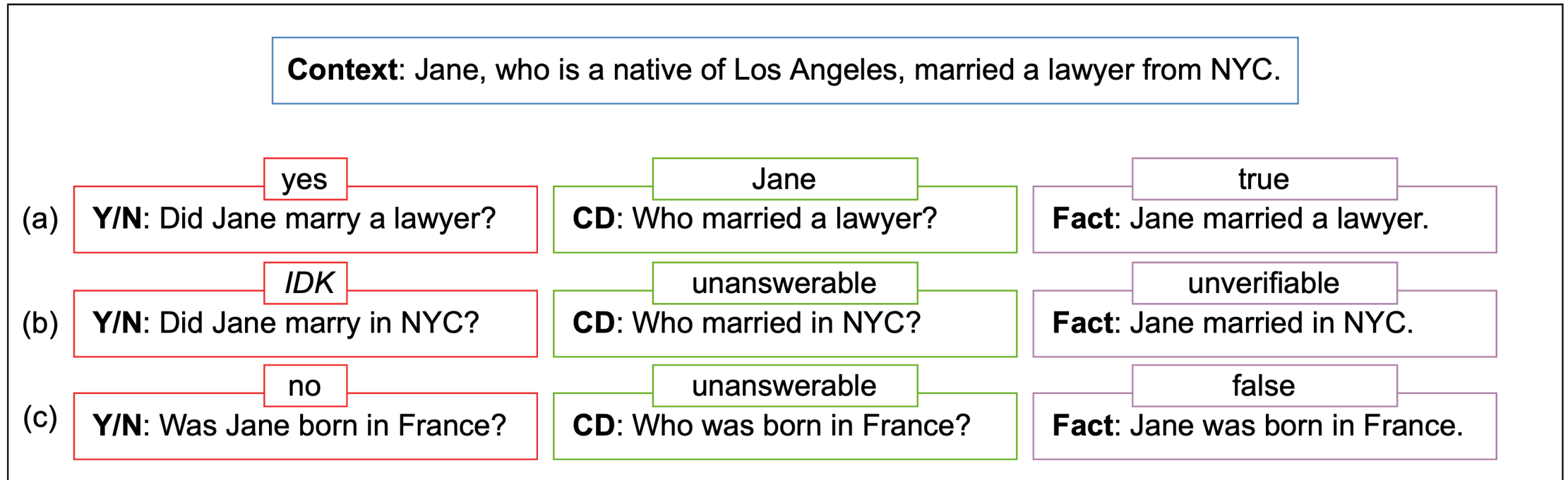
Brief Business Motivation

Smart Speaker Use Case Frequency - January 2019



voicebot.ai
 Source: Voicebot Smart Speaker Consumer Adoption Report Jan 2019

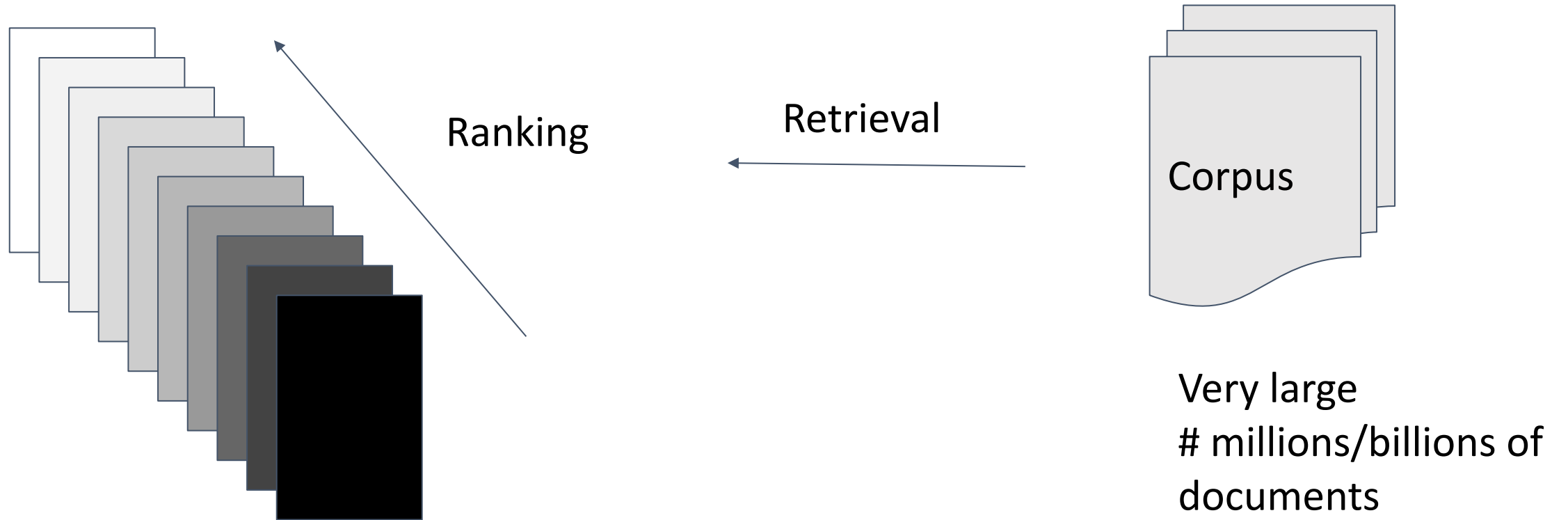
QA vs Fact-Checking



Yes/No Question (Y/N), Closed-domain Extractive QA (CD), A fact to be verified (FACT)

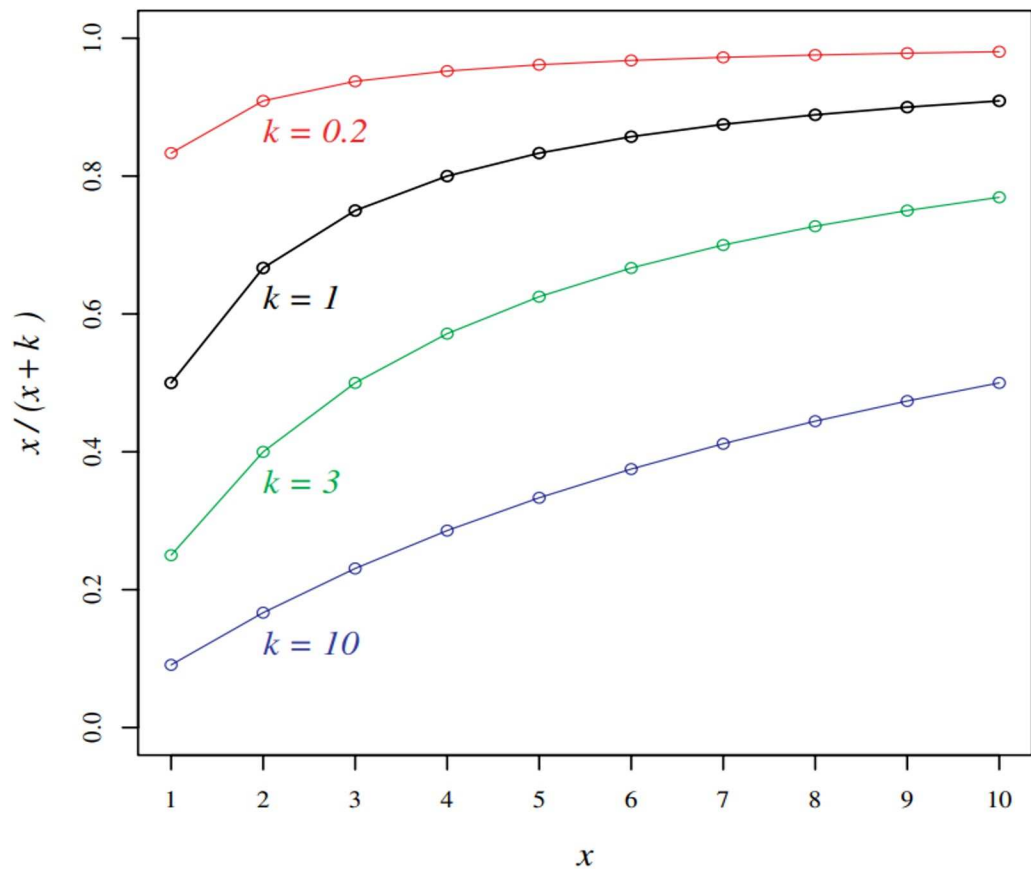
CHAPTER 3:
INTRODUCTION INTO BMI25

Retrieval



Building BM25 Retrieval

1. **[Query term importance in the document]** Pick a function, which increases monotonically with tf , is rising slowly, but this time is asymptotically approaching (saturates at) some value.



$$\frac{tf}{k + tf} \quad \text{for some } k > 0$$

this is term frequency in document D

$$Score(D, Q) = \sum_{w \in Q, w \in D} \frac{tf_w}{tf_w + k}$$

saturation
parameter

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2. **[Overall Term importance]** For every term pick a weight W_w expressing overall term's w importance (e.g. it can be old school $W_w = IDF_w$)

$$Score(D, Q) = \sum_{w \in Q, w \in D} \frac{tf_w}{tf_w + k} W_w$$

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3. **[Fix Long Document Bias]** Alleviate **long document bias** problem present in certain collections by penalizing too long documents.

Hypothesis
A



- Some authors are simply **more verbose** than others, using more words to say the same thing.
- These create **bias** in our model; long documents which say the same thing are preferred before short documents, as they achieve more tfs on average.
- An obvious solution to this is to **divide tfs by the document length**.

Hypothesis
B



- Some authors have **more to say**: they may write a single document containing or covering more ground. An extreme version would have the author writing two or more documents and concatenating them.

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3. **[Fix Long Document Bias]** Alleviate **long document bias** problem present in certain collections by penalizing too long documents.

$$B := \left((1 - b) + b \frac{dl}{avdl} \right), \quad 0 \leq b \leq 1$$

current document's length

average document length in corpus

soft constraint to cover both hypotheses

Building BM25 Retrieval

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BM-25 Formula

$$Score(D, Q) = \sum_{w \in Q, w \in D} \frac{\frac{tf_w}{B}}{\frac{tf_w}{B} + k} W_w = \sum_{w \in Q, w \in D} \frac{tf_w}{tf_w + kB} W_w$$

Building BM25 Retrieval

1. **[Query term importance in the document]** Pick a function, which increases monotonically with tf , is rising slowly, but this time is asymptotically approaching (saturates at) some value.
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3. **[Fix Long Document Bias]** Alleviate **long document bias** problem present in certain collections by penalizing too long documents.
4. **Robertson & Zaragoza, 2009** recommends hyperparam settings $0.5 < b < 0.8$; $1.2 < k < 2$

$$Score(D, Q) = \sum_{w \in Q, w \in D} \frac{\frac{tf_w}{B}}{\frac{tf_w}{B} + k} W_w = \sum_{w \in Q, w \in D} \frac{tf_w^{(k+1)}}{tf_w + kB} W_w$$

CHAPTER 4:
QUESTION ANSWERING

Selective QA

Evaluation: Standard multiclass classification metrics (Accuracy, F1, MCC)

Which of these do scientists offer as the most recent explanation as to why many plants and animals died out at the end of the Mesozoic era?

- (A) worldwide disease
- (B) global mountain building
- (C) rise of mammals that preyed upon plants and animals
- (D) impact of an asteroid created dust that blocked the sunlight

Extractive QA

The first recorded travels by Europeans to China and back date from this time. The most famous traveler of the period was the Venetian Marco Polo, whose account of his trip to "Cambaluc," the capital of the Great Khan, and of life there astounded the people of Europe. The account of his travels, *Il milione* (or, *The Million*, known in English as the *Travels of Marco Polo*), appeared about the year 1299. Some argue over the accuracy of Marco Polo's accounts due to the lack of mentioning the Great Wall of China, tea houses, which would have been a prominent sight since Europeans had yet to adopt a tea culture, as well the practice of foot binding by the women in capital of the Great Khan. Some suggest that Marco Polo acquired much of his knowledge **through contact with Persian traders** since many of the places he named were in Persian.

How did some suspect that Polo learned about China instead of by actually visiting it?

Answer: through contact with Persian traders

(macro)**F1** measures the average overlap between the prediction and ground truth answer.

Prediction and ground truth are treated as bags of tokens and their F1 is computed.

Usually a maximum F1 over all of the ground truth answers for a given question is taken, and the result is an average over all of the questions.

- Ground truth answer = {cat named kitty}

- Predicted answer = {cat named }

- $precision = \frac{\# \text{ of same tokens}}{\text{length of prediction}} = \frac{2}{2}$

- $recall = \frac{\# \text{ of same tokens}}{\text{length of ground truth}} = \frac{2}{3}$

- $F1 = 2 * \frac{precision * recall}{precision + recall} = 2 * \frac{\frac{2}{2} * \frac{2}{3}}{\frac{2}{2} + \frac{2}{3}}$

Abstractive QA

Title: Ghostbusters II

Question: How is Oscar related to Dana?

Answer: her son

Summary snippet: ...Peter's former girlfriend Dana Barrett has had a son, Oscar...

Story snippet:

DANA (setting the wheel brakes on the buggy)
Thank you, Frank. I'll get the hang of this eventually.

She continues digging in her purse while Frank leans over the buggy and makes funny faces at the baby, OSCAR, a very cute nine-month old boy.

FRANK (to the baby)
Hiya, Oscar. What do you say, slugger?

FRANK (to Dana)
That's a good-looking kid you got there, Ms. Barrett.

Task: Answer question from the story

Evaluation via Traditional NLG metrics

BLEU-4, ROUGE-L

Via neural metrics

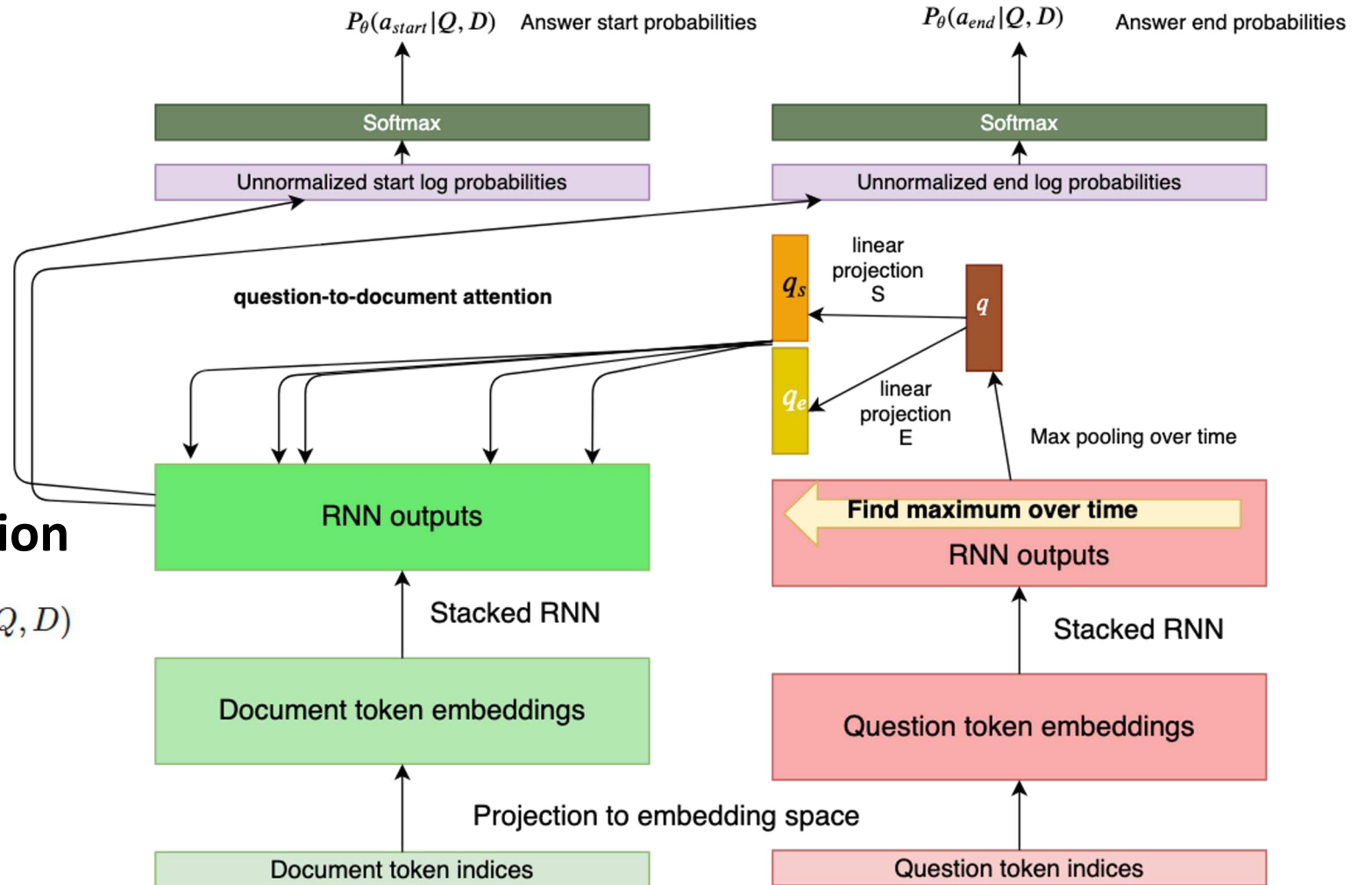
BERTScore, BELURT, GPT-4 eval

A simple extractive QA system A

Given question **Q** and document **D**
find answer span $\langle \mathbf{a}_{start}, \mathbf{a}_{end} \rangle$

Estimate parameters via
maximum likelihood estimation

$$\theta^* = \operatorname{argmax}_{\theta} \sum_{(Q, D, a_{start}, a_{end}) \in Data} \log P_{\theta}(a_{start}, a_{end} | Q, D)$$



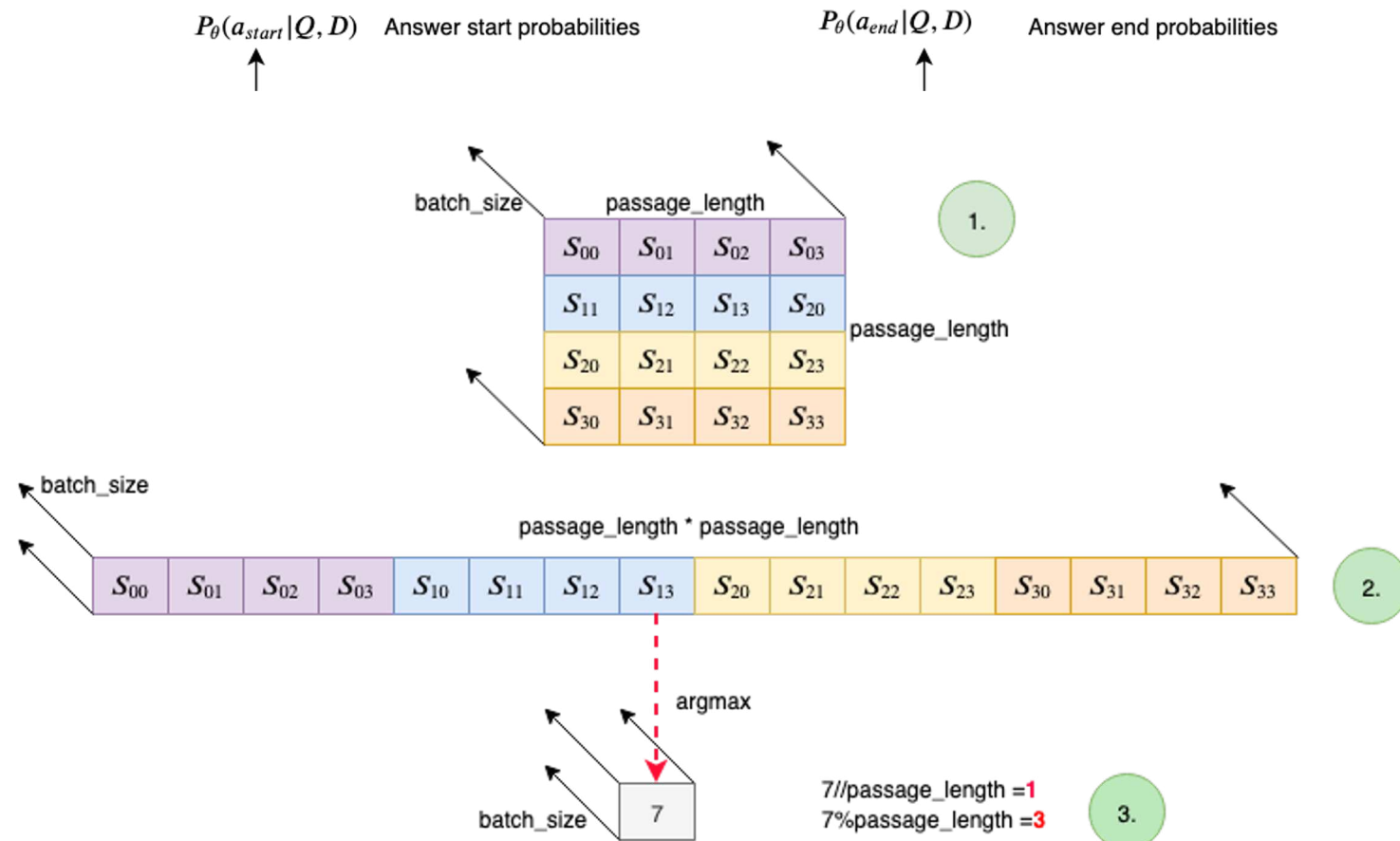
A simple extractive QA system: Decoding

Given question **Q** and document **D**
find answer span $\langle \mathbf{a}_{start}, \mathbf{a}_{end} \rangle$

Estimate parameters via **maximum likelihood estimation**

$$\theta^* = \operatorname{argmax}_{\theta} \sum_{(Q, D, a_{start}, a_{end}) \in \text{Data}} \log P_{\theta}(a_{start}, a_{end} | Q, D)$$

$P_{\theta}(a_{start} | Q, D)$ Answer start probabilities $P_{\theta}(a_{end} | Q, D)$ Answer end probabilities

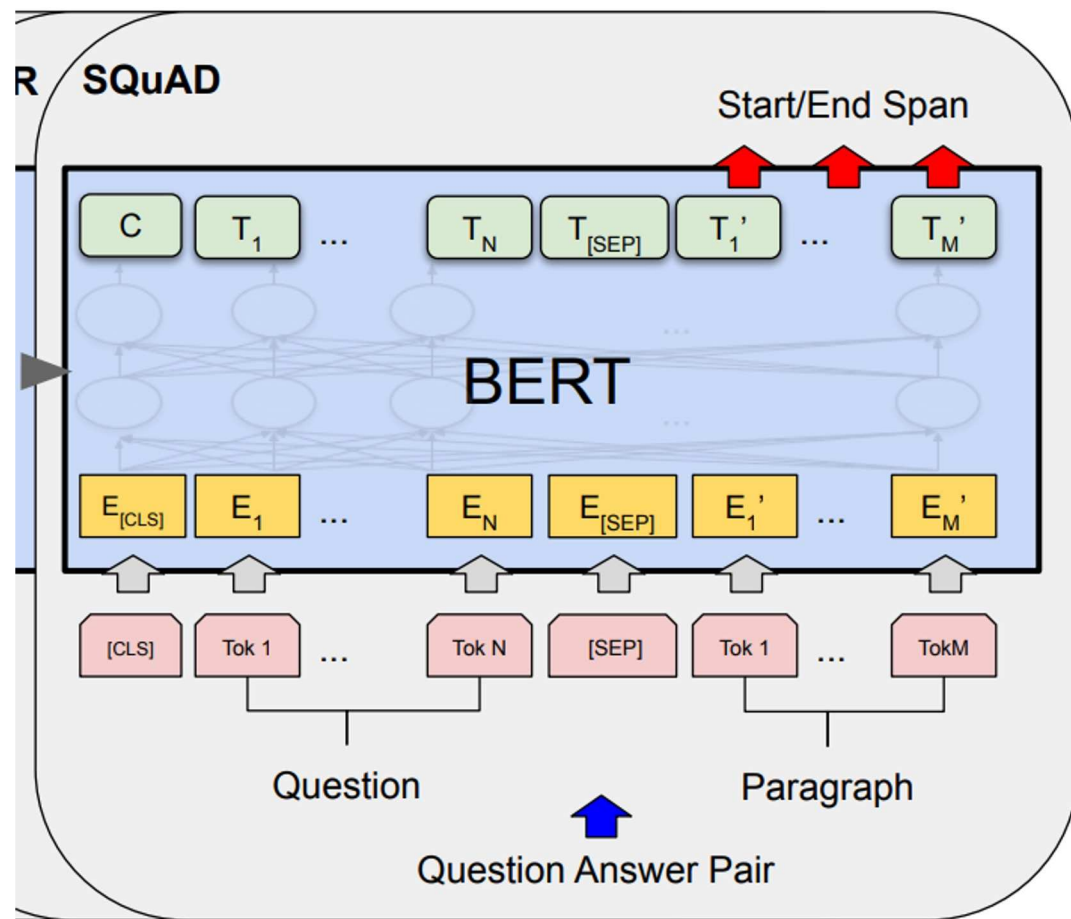


A simple extractive QA system B

Given question **Q** and document **D**
find answer span $\langle \mathbf{a}_{start}, \mathbf{a}_{end} \rangle$

Estimate parameters via **maximum likelihood estimation**

$$\theta^* = \operatorname{argmax}_{\theta} \sum_{(Q, D, \mathbf{a}_{start}, \mathbf{a}_{end}) \in \text{Data}} \log P_{\theta}(\mathbf{a}_{start}, \mathbf{a}_{end} | Q, D)$$



img source: Devlin, Jacob, et al. "BERT: Pre-training of Deep Bidirectional Transformers for Language Understanding." *NAACL-HLT*. 2019.

The Objective

$$- \sum_{(q,D,a) \in \mathcal{D}} \log P_{\theta}(a_s, a_e | q, D)$$

Assumption on Independence (Xiong et al., 2017; Seo et al., 2017; Chen et al., 2017; Yu et al., 2018; Devlin et al., 2019; Cheng et al., 2020; inter alia)

$$P(a_s, a_e | q, D) = P_{\theta}(a_s) P_{\theta}(a_e) \quad \text{Do we need to assume the independence?}$$

- Cross-entropy objective for extractive question answering

- given question q
- passage (or a set of passages) D
- answer represented by start/end positions $\mathbf{a}_s/\mathbf{a}_e$

No, we can compute joint objective with similar complexity directly, and it “works better”

(Fajcik et al., 2021)

Open-domain QA

MOTIVATION #1: Research-wise

1. **Dense** Neural Passage retrieval “just” started to work (Lee et al., 2019; Guu et al., 2020; Karupkhin et al., 2020; Khatatab et al. 2020; Izacard et al., 2020)
2. Open-domain QA is easy to annotate, all you need is **questions** and **answers**.
3. Closed-domain QA in some cases already works “very well”. Human Performance surpassed - SQuADv1.1, SQuADv2.0 (Rajpurkar et al. 2016,2018), CoQA (Reddy et al., 2018)

Almost any NLP task can be framed as question answering!

The first recorded travels by Europeans to China and back date from this time. The most famous traveler of the period was the Venetian Marco Polo, whose account of his trip to "Cambaluc," the capital of the Great Khan, and of life there astounded the people of Europe. The account of his travels, Il milione (or, The Million, known in English as the Travels of Marco Polo), appeared about the year 1299. Some argue over the accuracy of Marco Polo's accounts due to the lack of mentioning the Great Wall of China, tea houses, which would have been a prominent sight since Europeans had yet to adopt a tea culture, as well the practice of foot binding by the women in capital of the Great Khan. Some suggest that Marco Polo acquired much of his knowledge through contact with Persian traders since many of the places he named were in Persian.

How did some suspect that Polo learned about China instead of by actually visiting it?

Answer: through contact with Persian traders

Open-domain QA

MOTIVATION #2: Information retrieval in everyday life

- **Search needs a shake-up** (Etzioni, 2011)

“Academics and industry researchers need to achieve the intellectual ‘escape velocity’ necessary to **revolutionize search**. They must invest much more in bold strategies that can achieve **natural-language searching and answering**, rather than providing the electronic equivalent.”

← Keyword searching

“Moving up the information food chain requires a search engine that can **interpret** a user's **question**, extract facts from all the information on the **web**, and select an appropriate **answer**.”

Etzioni, Oren. "Search needs a shake-up." *Nature* 476.7358 (2011): 25-26.

why is the sky blue

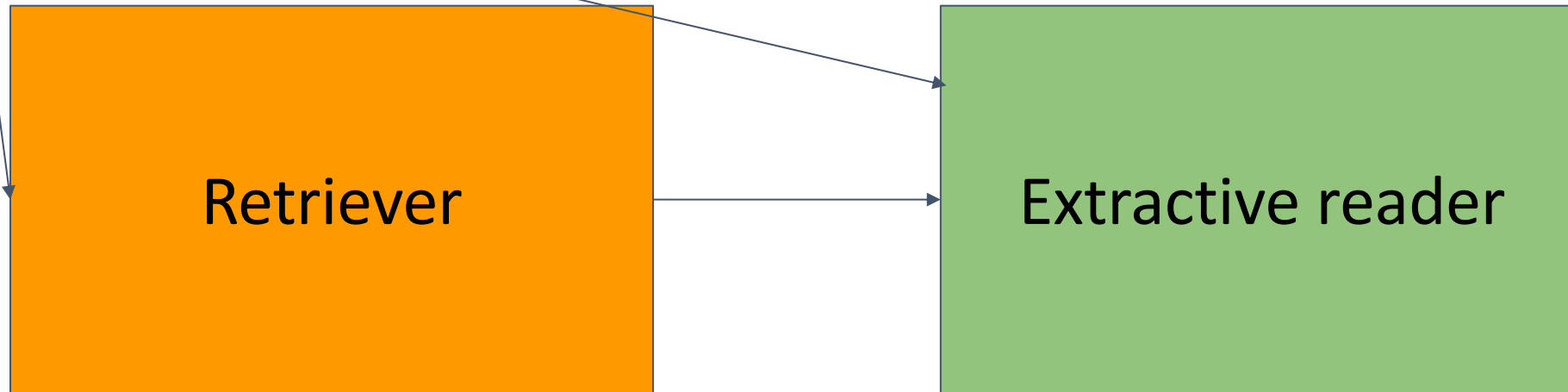


The blue component of the spectrum of visible light has shorter wavelengths and higher frequencies than the red component. **Thus, as sunlight of all colors passes through air, the blue part causes charged particles to oscillate faster than does the red part.** The faster the oscillation, the more scattered light is produced, so blue is scattered more strongly than red. For particles such as air molecules that are much smaller than the wavelengths of visible light the difference is dramatic. The acceleration of the charged particles is proportional to the square of the frequency, and the intensity of scattered light is proportional to the square of this acceleration. Scattered light intensity is therefore proportional to the fourth power of frequency. The result is that blue light is scattered into other directions almost 10 times as efficiently as red light.

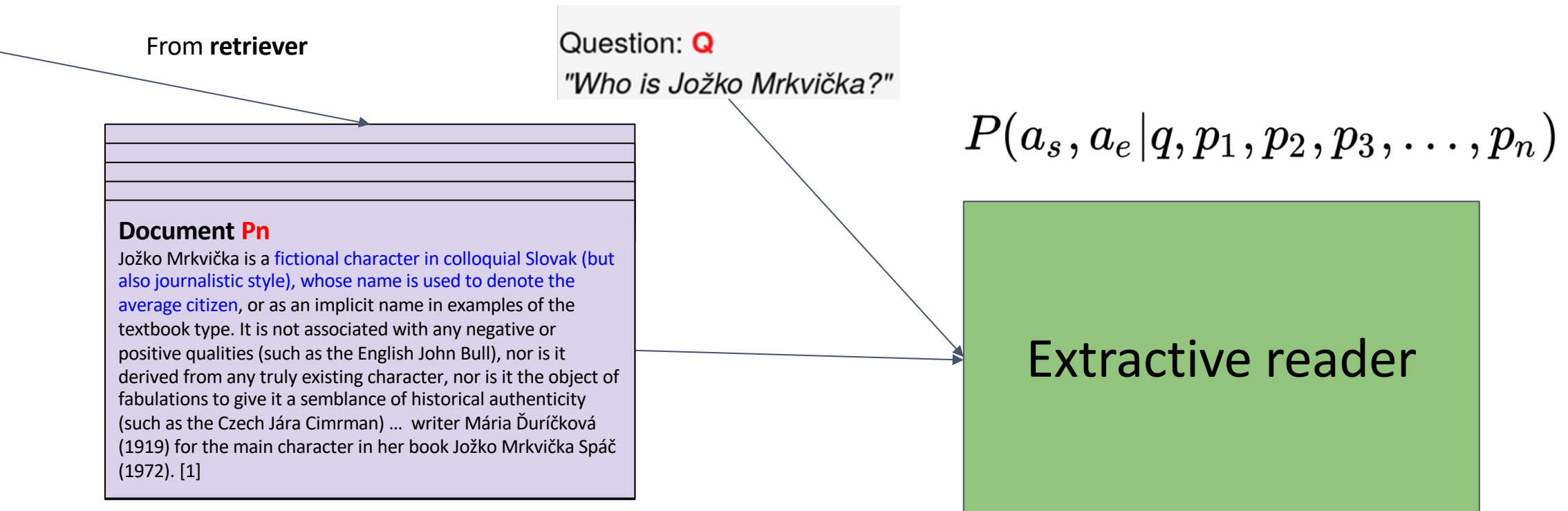
When we look at an arbitrary point in the sky, away from the sun, we see only the light that was redirected by the atmosphere into our line of sight. Because that occurs much more often for blue light than for red, the sky appears blue. Violet light is actually scattered even a bit more strongly than blue. **More of the sunlight entering the atmosphere is blue than violet, however, and our eyes are somewhat more sensitive to blue light than to violet light, so the sky appears blue.**

Example of traditional approach

Question: 
"Who is Jožko Mrkvička?"



Example of traditional approach: Reader



- In current literature, each document is usually processed via language representation model (e.g. BERT) separately.

Maximum Marginal Likelihood

- In Open-QA, we often do not know, which answer span is correct and which is not

Question: Which British general was killed at Khartoum in 1885?

Answer: Gordon

Context: In February 1885 **Gordon** returned to the Sudan to evacuate Egyptian forces. Khartoum came under siege the next month and rebels broke into the city, killing **Gordon** and the other defenders. The British public reacted to his death by acclaiming '**Gordon** of Khartoum', a saint. However, historians have suggested that **Gordon**...

Figure 1: Noisy supervision can cause many spans of text that contain the answer, but are not situated in a context that relates to the question (red), to distract the model from learning from more relevant spans (green).

Maximum Marginal Likelihood

- In Open-QA, we often do not know, which answer span is correct and which is not
- Solution? Marginalize over all spans with correct surface form, let the model decide
- Formally:
- in **fully supervised** setting, we are given input x , and answer span \bar{z} , our NLL objective for 1 sample is

$$J_{\text{Sup}}(\theta|x, \bar{z}) = -\log \mathbb{P}(\bar{z}|x; \theta)$$

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in **weakly supervised** setting, we are given input x , and many answer spans for each string match $Z=\{z_1, z_2, \dots, z_n\}$, some of which are correct, some of which are not.

- Note that Z is subset of Z_{tot} , the set of \bar{z} all spans in the document(s), y is answer string match

$$\begin{aligned} \mathbb{P}(y|x; \theta) &= \sum_{z_i \in Z_{\text{tot}}} \mathbb{P}(y|z_i) \mathbb{P}(z_i|x; \theta) \\ &= \sum_{z_i \in Z} \mathbb{P}(z_i|x; \theta) \end{aligned}$$

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0 if z_i is not from Z , 1 otherwise

$$J_{\text{MML}}(\theta|x, Z) = -\log \sum_{z_i \in Z} \mathbb{P}(z_i|x; \theta)$$

Maximum Marginal Likelihood

- In Open-QA, we often do not know, which answer span is correct and which is not
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in **weakly supervised** setting, we are given input x , and many answer spans for each string match $Z=\{z_1, z_2, \dots, z_n\}$, some of which are correct, some of which are not.

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$$J_{\text{MML}}(\theta|x, Z) = -\log \sum_{z_i \in Z} \mathbb{P}(z_i|x; \theta)$$

This is a so called „latent variable model“ with latent variable v_i . Remember GMM!

MML in Open-domain QA

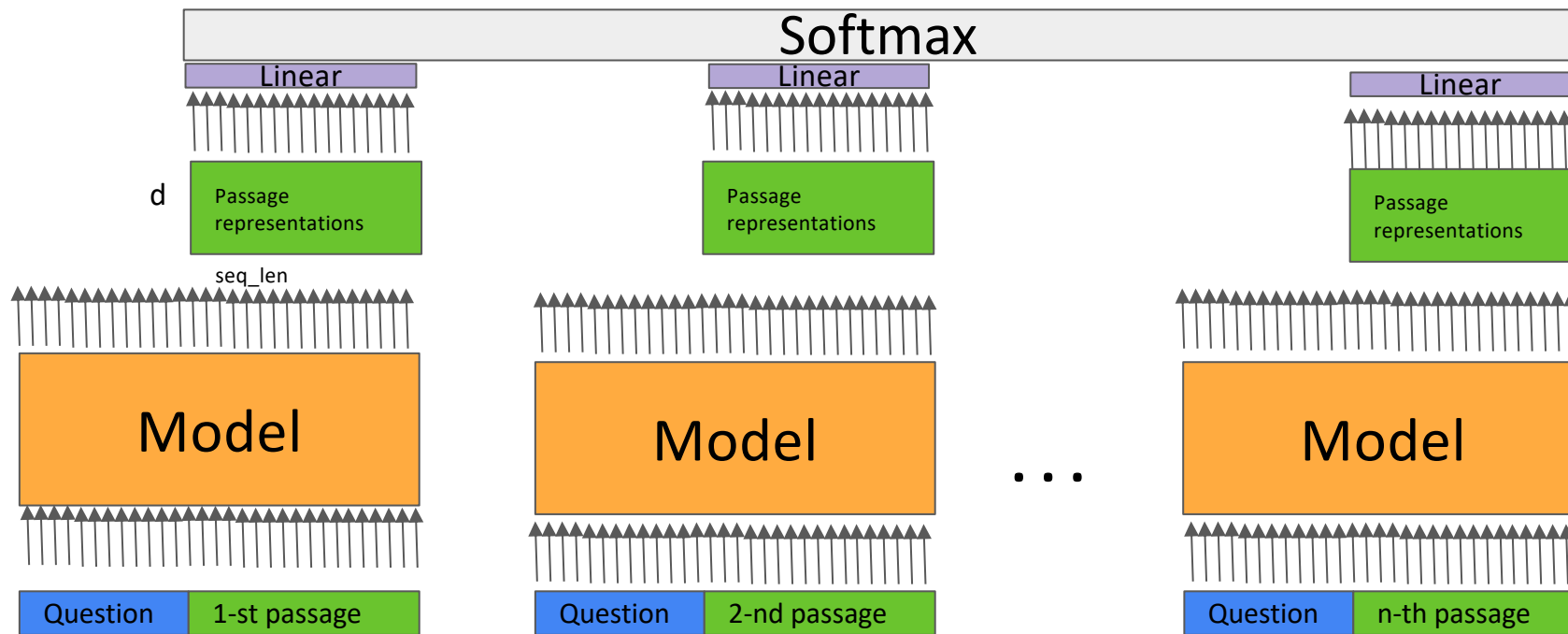
Loss for 1 sample $\mathcal{L}_i =$

$$-\log \sum_{p \in P} \sum_{a \in GT(p)} P(a_s | q, P)$$

$$-\log \sum_{p \in P} \sum_{a \in GT(p)} P(a_e | q, P)$$

$$P(a_{start} | q, p_1, p_2, \dots, p_n)$$

$$P(a_{end} | q, p_1, p_2, \dots, p_n)$$



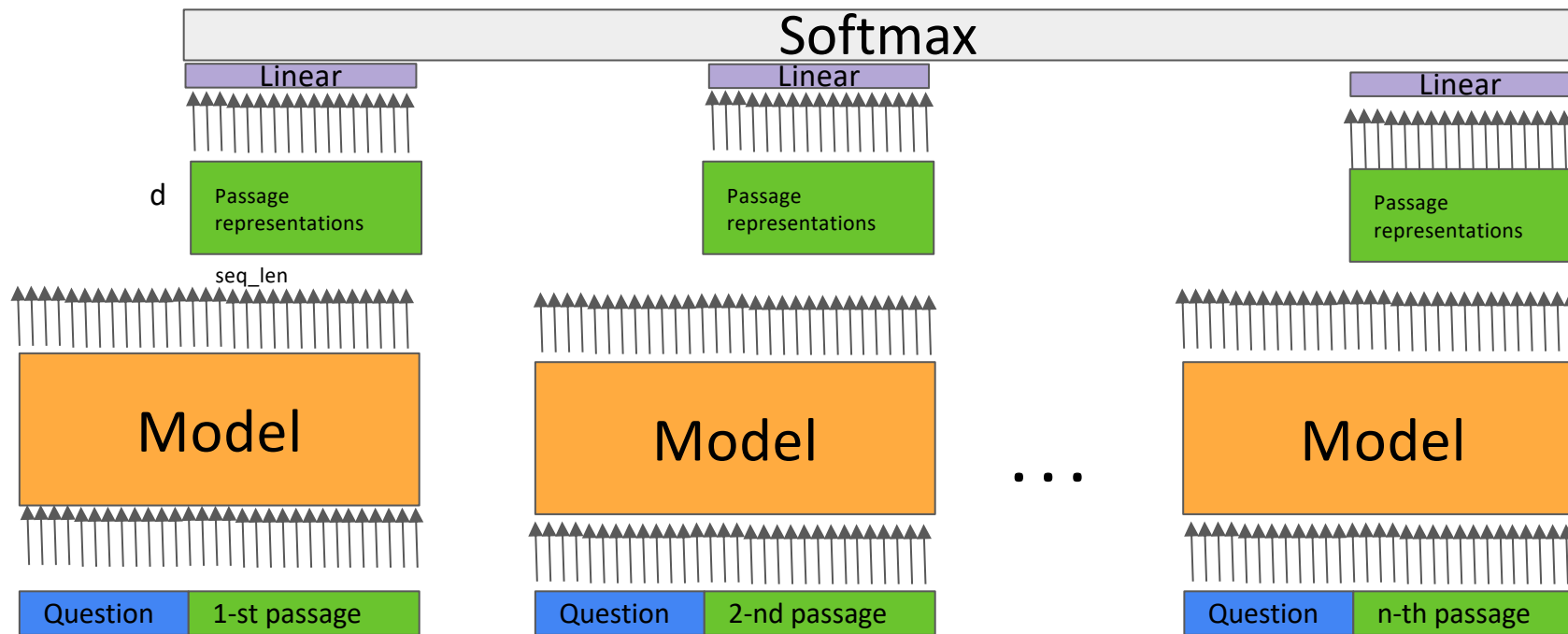
MML in Open-domain QA

Loss for 1 sample $\mathcal{L}_i =$

$$-\log \sum_{p \in P} \sum_{a \in GT(p)} P(a_s | q, P)$$
$$-\log \sum_{p \in P} \sum_{a \in GT(p)} P(a_e | q, P)$$

$$P(a_{start} | q, p_1, p_2, \dots, p_n)$$

$$P(a_{end} | q, p_1, p_2, \dots, p_n)$$



Important for cross-passage answer score calibration!

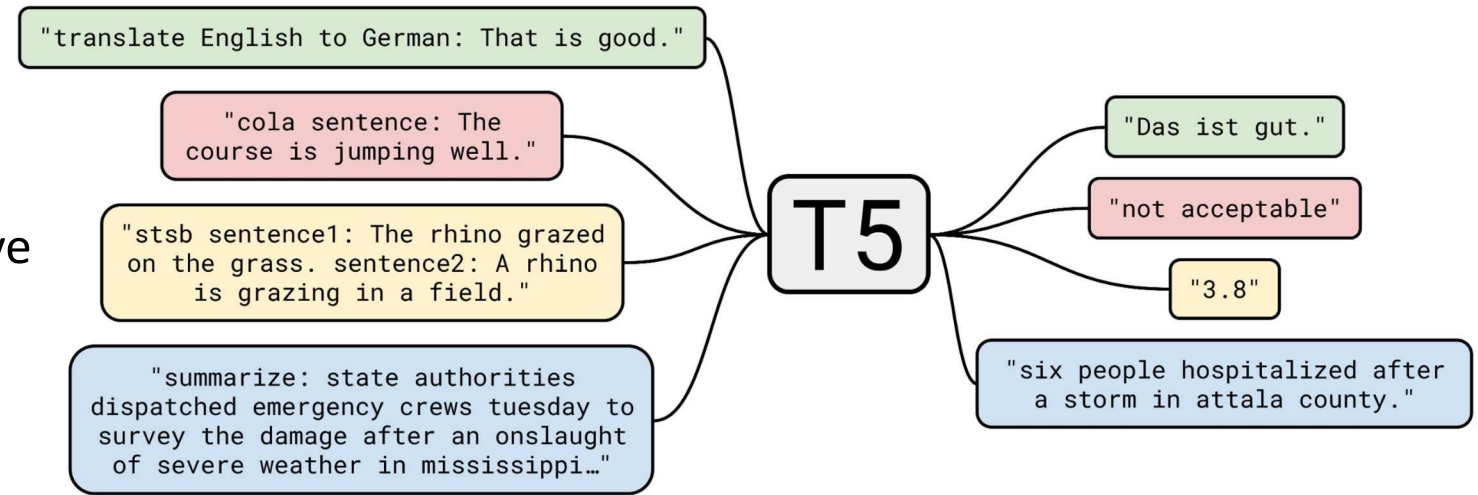
Clark, Christopher, and Matt Gardner. "Simple and Effective Multi-Paragraph Reading Comprehension." *Proceedings of the 56th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*. 2018.

Do we need to use extractive models?

- IDEA: generate answer through the language model

T5

- Seq-2-seq, Enc-Decoder unlike BERT
- subword language units
- trained on denoising objective and ~25 supervised tasks
- 750GB CommonCrawl data



Original text

Thank you ~~for inviting~~ me to your party ~~last~~ week.

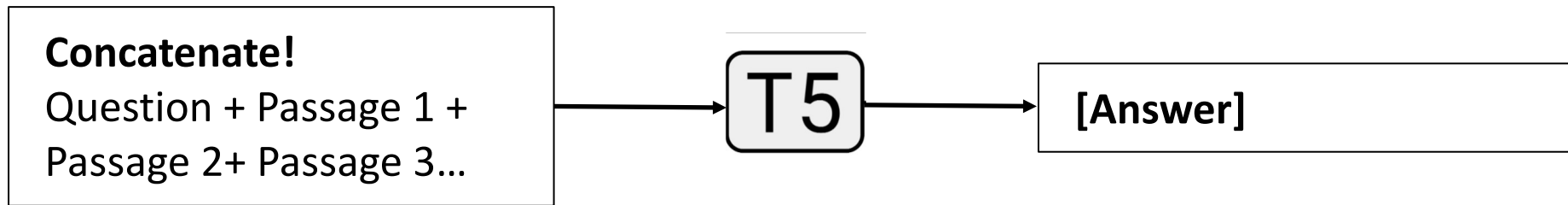
Inputs

Thank you <X> me to your party <Y> week.

Targets

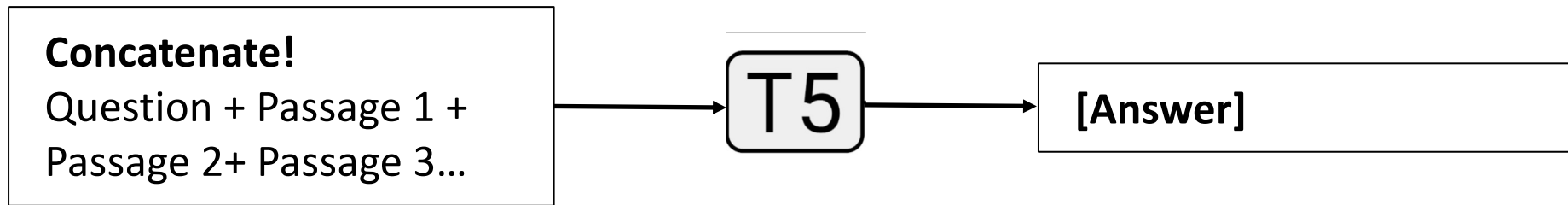
<X> for inviting <Y> last <Z>

Idea #1: „Concatenate, pass, profit“



Drawbacks?

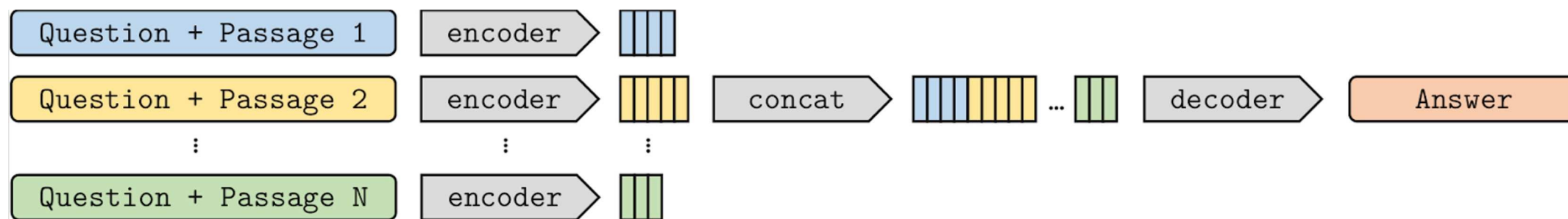
Idea #1: „Concatenate, pass, profit“



- 1. Memory complexity**
2024' (tricks can be involved: flash-attention, windowed attention)
- 2. Decoding: If we do decoding without restrictions,**
the model might generate something not present in the text
= HALLUCINATION

Idea #2: Processing passages jointly: Fusion-in-Decoder

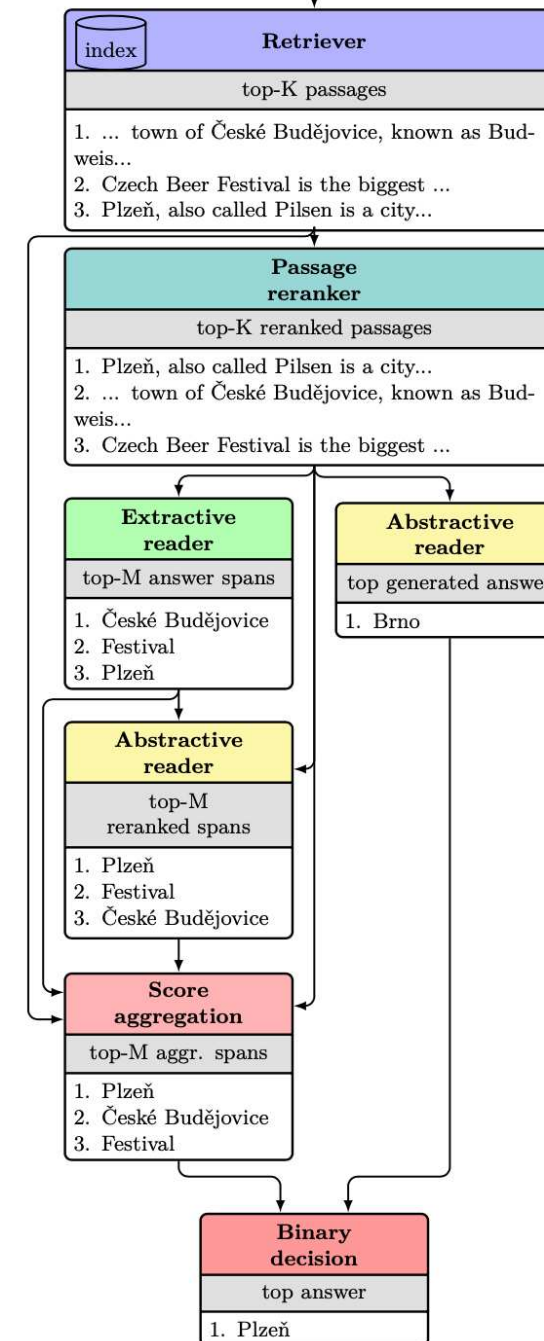
- Do we need to read every passage independently?
- No, we can actually allow inter-passage interaction learning!
- Example: Fusion-in-Decoder (FiD), encode every passage separately, decode jointly
- Trick works well with pre-trained models (T5)!
- Can process very long inputs (sequences of $200(\text{passage length}) * 100(\text{context size})$ tokens long)
- Optimize target answer via standard language modeling loss (Cross-Entropy)



Fusing the extractive and generative approaches

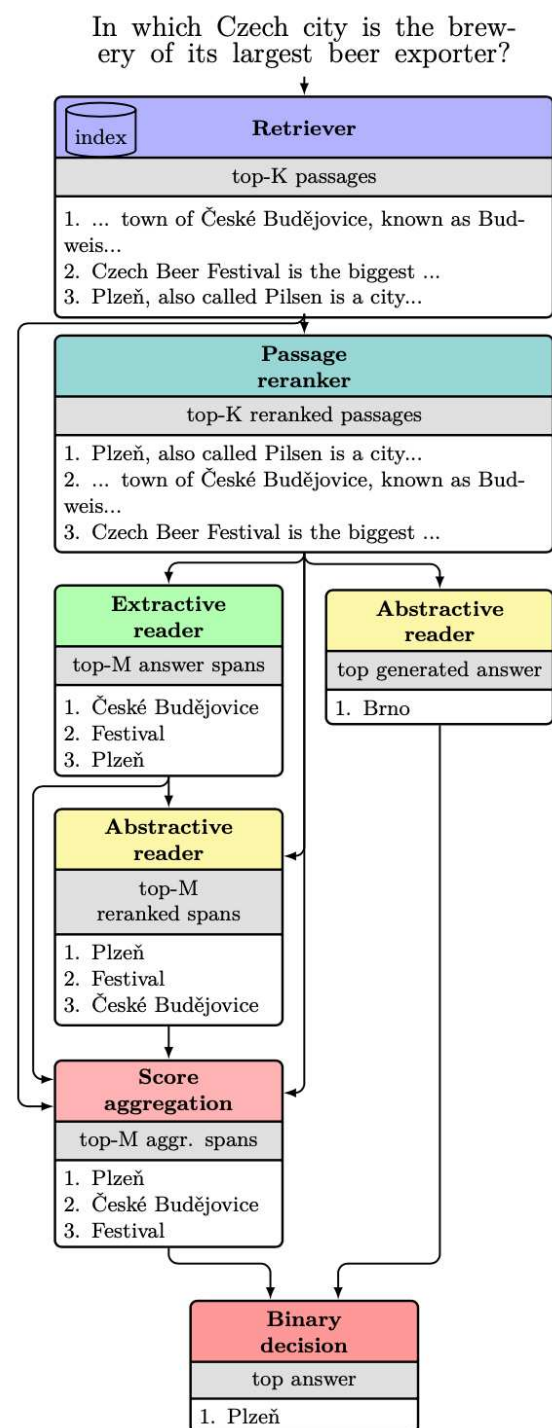
- Our past work:
Rank twice, read twice R2-D2
- <https://r2d2.fit.vutbr.cz/>
- Some demo details:
 - The search is done in “popular” 8% of Wikipedia
 - Only factoid answers, up to 6 words
 - Wikipedia from dec 2018 is used

In which Czech city is the brewery of its largest beer exporter?



Fusing the extractive and generative approaches

- Why is the search done in “popular” 8% of Wikipedia?
 - We’ve shown we can remove 92% of index from two most popular datasets for open-domain QA, NaturalQuestions and TriviaQA, while losing only up to 3% absolute performance on test set.
 - How? We trained a classifier which given a passage, tries to say apriori (without seeing any question), whether the passage is relevant or not.
 - Could same “pruning” mechanism be implicitly present in modern supervised neural retrieval approaches?
 - Wait for the release of my PhD thesis 😊



CHAPTER 5:
'24 TRENDS

Is QA “solved” by LLM such as Grok/ChatGPT/GPT4?

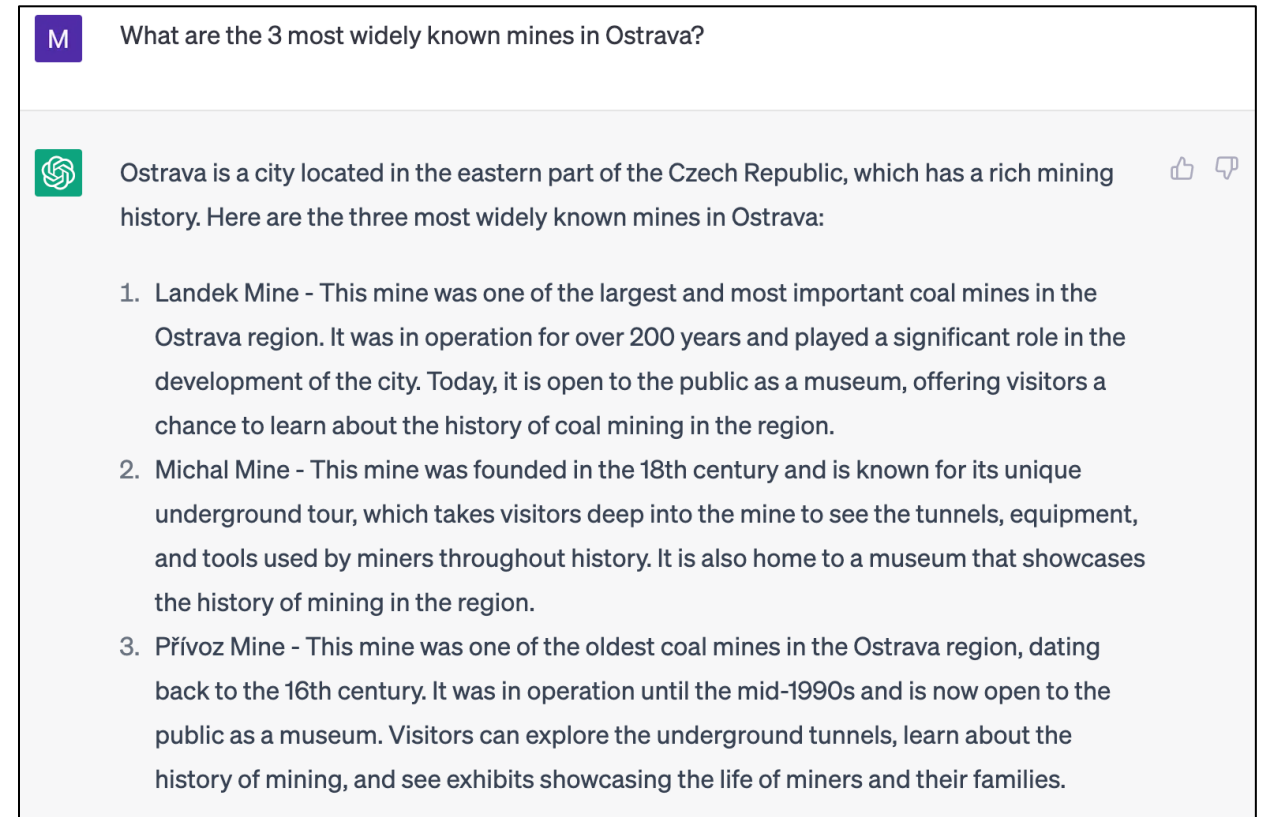
Not really, for example in Czech

<https://huggingface.co/spaces/hynky/CZ-EVAL>


Is QA “solved” by LLM such as ChatGPT/GPT4?

1. Yes because...

1. Large LLM have extensive factual knowledge.
2. LLMs can present answers excellently!



M What are the 3 most widely known mines in Ostrava?

 Ostrava is a city located in the eastern part of the Czech Republic, which has a rich mining history. Here are the three most widely known mines in Ostrava: 👍 🗨

1. Landek Mine - This mine was one of the largest and most important coal mines in the Ostrava region. It was in operation for over 200 years and played a significant role in the development of the city. Today, it is open to the public as a museum, offering visitors a chance to learn about the history of coal mining in the region.
2. Michal Mine - This mine was founded in the 18th century and is known for its unique underground tour, which takes visitors deep into the mine to see the tunnels, equipment, and tools used by miners throughout history. It is also home to a museum that showcases the history of mining in the region.
3. Přívoz Mine - This mine was one of the oldest coal mines in the Ostrava region, dating back to the 16th century. It was in operation until the mid-1990s and is now open to the public as a museum. Visitors can explore the underground tunnels, learn about the history of mining, and see exhibits showcasing the life of miners and their families.

Is QA “solved” by LLM such as ChatGPT/GPT4?

1. Maybe because...
 1. Large LLMs can **lie** excellently. This kind of problem is called “Hallucination”.

M

Name a few mining tunnels (adits) from Kremnica mountains



The Kremnica Mountains in central Slovakia have a rich mining history with numerous adits (horizontal tunnels) that were used for mining various metals including gold, silver, copper, and other minerals. Here are a few examples of mining tunnels from the Kremnica Mountains:

1. Andrej Adit - This is one of the oldest and most famous mining tunnels in the Kremnica Mountains, used for silver and other metal mining. The adit is open to visitors for guided tours.
2. Rozalia Adit - A historic adit used for silver, copper, and other metal mining in the Kremnica Mountains, now open to visitors for guided tours.
3. Zobor Adit - An adit located near the town of Štiavnické Bane in the Kremnica Mountains, used for silver and copper mining. It is open to visitors for guided tours.
4. Svatopluk Adit - An adit used for gold and silver mining in the Kremnica Mountains, now open to visitors for guided tours.
5. Barbora Adit - A historic adit located in the town of Kremnica, used for silver and other metal mining. It is open to visitors for guided tours.
6. Nová Baňa Adit - An adit used for copper and gold mining in the Kremnica Mountains, now open to visitors for guided tours.
7. Sklené Teplice Adit - A historic adit used for silver and copper mining in the Kremnica Mountains, now open to visitors for guided tours.

Is QA “solved” by LLM such as ChatGPT/GPT4?

1. No because

1. Large LLMs cannot explain themselves.

M

Name a few mining tunnels (adits) from Kremnica mountains



The Kremnica Mountains in central Slovakia have a rich mining history with numerous adits (horizontal tunnels) that were used for mining various metals including gold, silver, copper, and other minerals. Here are a few examples of mining tunnels from the Kremnica Mountains:

1. Andrej Adit - This is one of the oldest and most famous mining tunnels in the Kremnica Mountains, used for silver and other metal mining. The adit is open to visitors for guided tours.
2. Rozalia Adit - A historic adit used for silver, copper, and other metal mining in the Kremnica Mountains, now open to visitors for guided tours.
3. Zobor Adit - An adit located near the town of Štiavnické Bane in the Kremnica Mountains, used for silver and copper mining. It is open to visitors for guided tours.
4. Svatopluk Adit - An adit used for gold and silver mining in the Kremnica Mountains, now open to visitors for guided tours.
5. Barbora Adit - A historic adit located in the town of Kremnica, used for silver and other metal mining. It is open to visitors for guided tours.
6. Nová Baňa Adit - An adit used for copper and gold mining in the Kremnica Mountains, now open to visitors for guided tours.
7. Sklené Teplice Adit - A historic adit used for silver and copper mining in the Kremnica Mountains, now open to visitors for guided tours.

Is QA “solved” by LLM such as ChatGPT/GPT4?

1. No because

1. LLMs are competitive, but not outperforming the task specific models.

| Tasks | Dataset | Metric | Reference | Fine-Tuned SOTA | Zero-Shot SOTA | ChatGPT |
|---------------------------------|------------------|-------------|---------------------------------|-----------------|--------------------|---------|
| Summarization | CNN/DM | ROUGE-1 | Lewis et al. (2020a) | 44.47 | 35.27 ⁷ | 35.29 |
| | SAMSum | ROUGE-1 | Lewis et al. (2020a) | 47.28 | - | 35.29 |
| MT (XXX→Eng) | FLoRes-200 (HRL) | ChrF++ | Team et al. (2022) | 63.5 | - | 58.64 |
| | FLoRes-200 (LRL) | ChrF++ | Team et al. (2022) | 54.9 | - | 27.75 |
| MT (Eng→XXX) | FLoRes-200 (HRL) | ChrF++ | Team et al. (2022) | 54.4 | - | 51.12 |
| | FLoRes-200 (LRL) | ChrF++ | Team et al. (2022) | 41.9 | - | 21.57 |
| Sentiment Analysis | NusaX - Eng | Macro F1 | Winata et al. (2022) | 92.6 | 61.5 | 83.24 |
| | NusaX - Ind | Macro F1 | Winata et al. (2022) | 91.6 | 59.3 | 82.13 |
| | NusaX - Jav | Macro F1 | Winata et al. (2022) | 84.2 | 55.7 | 79.64 |
| | NusaX - Bug | Macro F1 | Winata et al. (2022) | 70.0 | 55.9 | 55.84 |
| Question Answering | bAbI task 15 | Accuracy | Weston et al. (2016a) | 100 | - | 93.3 |
| | bAbI task 16 | Accuracy | Weston et al. (2016a) | 100 | - | 66.7 |
| | EntailmentBank | Accuracy | Clark et al. (2018) | 86.5 | 78.58 | 93.3 |
| | CLUTRR | Accuracy | Minervini et al. (2020) | 95.0 | 28.6 | 43.3 |
| | StepGame (k=9) | Accuracy | Mirzaee and Kordjamshidi (2022) | 48.4 | - | 23.3 |
| | StepGame (k=1) | Accuracy | Mirzaee and Kordjamshidi (2022) | 98.7 | - | 63.3 |
| | Pep-3k | AUC | Porada et al. (2021) | 67.0 | - | 93.3 |
| Misinformation Detection | COVID-Social | Accuracy | Lee et al. (2021) | 77.7 | 50.0 | 73.3 |
| | COVID-Scientific | Accuracy | Lee et al. (2021) | 74.7 | 71.1 | 92.0 |
| Task-Oriented Dialogue | MultiWOZ2.2 | JGA | Zhao et al. (2022) | 60.6 | 46.7 | 24.4 |
| | MultiWOZ2.2 | BLEU | Nekvinda and Dušek (2021) | 19.1 | - | 5.65 |
| | MultiWOZ2.2 | Inform Rate | Yang et al. (2021) | 95.7 | - | 71.1 |
| Open-Domain KGD | OpenDialKG | BLEU | Ji et al. (2022c) | 20.8 | 3.1 | 4.1 |
| | OpenDialKG | ROUGE-L | Ji et al. (2022c) | 40.0 | 29.5 | 18.6 |
| | OpenDialKG | FeQA | Ji et al. (2022c) | 48.0 | 23.0 | 15.0 |

Table 1: Performance of ChatGPT compared to state-of-the-art fully-fine-tuned models (Fine-Tuned SOTA) and LLM in zero-shot settings (Zero-Shot SOTA). The referenced performances are evaluation results on full test sets, while the ChatGPT performances are computed on subsets of the corresponding dataset **using 30 to 200 data samples** for each task. For Machine Translation (MT) tasks, we use the definitions of high-resource language (HRL) and low-resource language (LRL) from NLLB (Team et al., 2022) and take subsets of languages to represent each group. JGA denotes joint goal accuracy.

Is QA “solved” by Retrieval-Augmented LLMs?

1. Yes because
 1. all responses with factoid answers are grounded.

The screenshot displays a chat interface with two queries and their corresponding answers, demonstrating grounded responses. The interface includes a search bar, a chat input field, and a list of suggested questions.

Query 1: Who won the 2022 World Cup?

Answer 1: Argentina won the 2022 World Cup by beating France on penalties in the final at the Lusail Iconic Stadium in Qatar^{1 2}. The score was 3-3 after extra time, and Argentina won 4-2 on penalties^{3 1}. It was Argentina's third World Cup title, and their first since 1986^{1 2}.

Query 2: Who is the President of the USA today?

Answer 2: The President of the USA today is Joe Biden^{1 2 3}. He is the 46th President of the United States, and has been in office since January 20, 2021^{1 2 3}. He is a Democrat and was elected on November 7, 2020, defeating former President Donald Trump^{1 3}.

Additional Suggested Questions: Who is the Vice President of the USA?, What are some of Joe Biden's policies?, How old is Joe Biden?

Is QA “solved” by Evidence-grounded LLMs?

1. Maybe because

1. Evidence-grounded models still suffer from hallucination.

Query: What are the pros and cons of the top 3 selling pet vacuums?

The screenshot shows a search engine results page for the query "What are the pros and cons of the top 3 selling pet vacuums?". The page displays several search results, including articles from hgtv.com, consumerreports.org, goodhousekeeping.com, appliancesradar.com, bobvila.com, bestforpets.org, and msn.com. The results are organized into sections: "EXPLORE FURTHER", "The Best Cordless Vacuums for Pet Hair of 2023 - Bob Vila", "The 15 Best Pet Vacuum of 2023 - bestforpets.org", and "16 Best Vacuums for Dog and Cat Hair, According to ...". At the bottom, there is a section titled "See what are the pros and cons of the top 3 selling pet vacuums" with a link to bing.com/shop. Below this, there are buttons for Bissell, Shark, Hoover, Dyson, and Bagles. On the right side, there is a detailed list of pros and cons for the top 3 selling pet vacuums: Dyson V8 Animal Cordless Stick Vacuum, Bissell Pet Hair Eraser Handheld Vacuum, and Shark Navigator Lift-Away Professional. The pros and cons are listed in a structured format with bullet points.

odor when you vacuum. Some al... owners. If your current vacuum cleaner is do... vacuum cleaners available that are...

EXPLORE FURTHER

- The Best Vacuums for Pet Hair in 2023, Tested by HGTV Edit... hgtv.com
- Best Vacuums of 2023 - Consumer Reports consumerreports.org
- 8 Best Vacuums for Pet Hair of 2023 - Good Housekeeping goodhousekeeping.com
- Best Vacuums for Pet Hair - Consumer Reports consumerreports.org
- Best Vacuum Cleaners For Carpet And Pet Hair - Top 10 for 2... appliancesradar.com

Recommended to you based on what's popular - Feedback

The Best Cordless Vacuums for Pet Hair of 2023 - Bob Vila
<https://www.bobvila.com/articles/best-cordless...>
Pros: Tangle-free brush roll; Dustbin is easy to empty; Easy to store; Cons: Pricey; Get the Bissell ICON pet vacuum on Amazon or at ...
Estimated Reading Time: 10 mins

The 15 Best Pet Vacuum of 2023 - bestforpets.org - A powerful ...
<https://bestforpets.org/best-pet-vacuum>
Jan 21, 2023 · PROS: A powerful vacuum may swiftly cover a great deal of ground; Swivel ...
5/5 ★★★★★ (2)

16 Best Vacuums for Dog and Cat Hair, According to ...
<https://www.msn.com/en-us/lifestyle/shopping/16...>
May 20, 2022 · Pros: Lift-off technology allows you to clean where other vacuums do not; ...

See what are the pros and cons of the top 3 selling pet vacuums
<bing.com/shop>

Bissell Shark Hoover Dyson Bagles >

Ads

Learn more: 1. hgtv.com 2. rtngs.com +8 more

• **Dyson V8 Animal Cordless Stick Vacuum** 4 5 6 7 8 :
Pros:

- It has a powerful suction and a long battery life of up to 40 minutes.
- It has a HEPA filter that captures 99.97% of allergens and dust particles as small as 0.3 microns.
- It can be converted into a handheld vacuum for cleaning furniture, stairs, cars, etc.

Cons:

- It is expensive compared to other cordless vacuums.
- It has a small dust bin capacity of 0.54 liters and a long charging time of 5 hours.
- It doesn't have a soft roller cleaner head for cleaning hard floors, which is only available in the Absolute model.

• **Bissell Pet Hair Eraser Handheld Vacuum** 1 :
Pros:

- It is lightweight, compact, and easy to use for quick cleanups.
- It has a rubber nozzle that attracts and removes pet hair from upholstery, stairs, bedding, etc.
- It has a washable filter and a bagless design for low maintenance.

Cons:

- It has a limited suction power and a short cord length of 16 feet.
- It is noisy and may scare some pets.
- It is not suitable for cleaning large areas or carpets.

Is QA “solved” by Evidence-grounded LLMs?

Query: What are the pros and cons of the top 3 selling pet vacuums?

The screenshot shows a Bing search results page for the query "What are the pros and cons of the top 3 selling pet vacuums?". The page features several search results and a detailed snippet for the "Dyson V8 Animal Cordless Stick Vacuum".

Search Results:

- The Best Cordless Vacuums for Pet Hair of 2023 - Bob Vila**
https://www.bobvila.com/articles/best-cordless...
Pros: Tangle-free brush roll; Dustbin is easy to empty; Easy to store; Cons: Pricey; Get the Bissell ICON pet vacuum on Amazon or at ...
Estimated Reading Time: 10 mins
- The 15 Best Pet Vacuum of 2023 - bestforpets.org - A powerful ...**
https://bestforpets.org/best-pet-vacuum...
Jan 21, 2023 · PROS. A powerful vacuum may swiftly cover a great deal of ground; Swivel ...
5/5 ★★★★★ (2)
- 16 Best Vacuums for Dog and Cat Hair, According to ...**
https://www.msn.com/en-us/lifestyle/shopping/16...
May 20, 2022 · Pros: Lift-off technology allows you to clean where other vacuums do not; ...
- See what are the pros and cons of the top 3 selling pet vacuums**
bing.com/shop

Navigation: Bissell, Shark, Hoover, Dyson, Bagles

Dyson V8 Animal Cordless Stick Vacuum 4 5 6 7 8 :

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Learn more: 1. hgtv.com 2. rtings.com +8 more

“This is all completely made up information.

Bing AI was kind enough to give us its sources, so we can go to the [hgtv article](#) and check for ourselves.

The cited article says nothing about limited suction power or noise. In fact, the top amazon review for this product talks about how quiet it is.

The article also says nothing about the “short cord length of 16 feet” because it doesn’t have a cord. It’s a portable handheld vacuum.”

Is QA “solved” by Evidence-grounded LLMs?

Evidence-grounded models still **suffer from hallucination and bad evidence grounding**.

| <i>Citation F_1</i> (↑) | |
|--------------------------------------|-------|
| Average Over All Queries | |
| Bing Chat | 70.9% |
| NeevaAI | 69.8% |
| perplexity.ai | 70.6% |
| YouChat | 18.9% |
| Average | 57.6% |

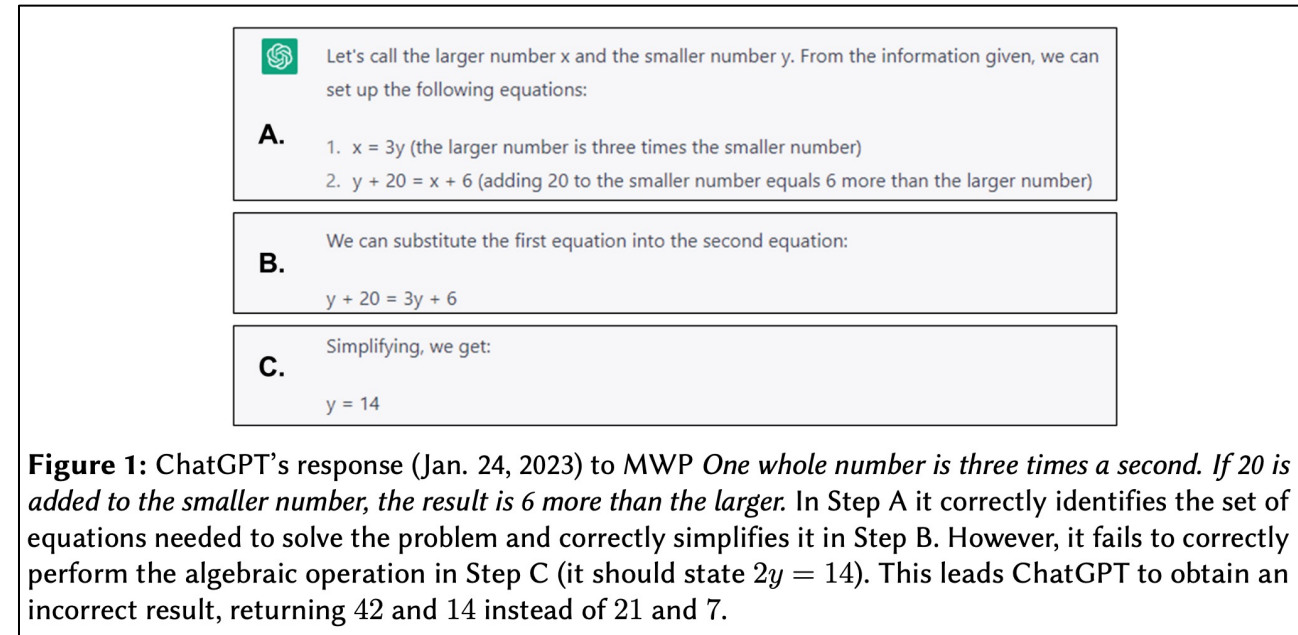
Citation recall is the proportion of verification worthy statements that are fully supported by their associated citations.

Citation precision is the proportion of generated citations that support their associated statements.

“We find that responses from existing generative search engines are fluent and appear informative, but frequently contain unsupported statements and inaccurate citations: **on average, a mere 51.5% of generated sentences are fully supported by citations (*citation recall*) and only 74.5% of citations support their associated sentence (*citation precision*)**. We believe that these results are concerningly low for systems that may serve as a primary tool for information seeking users, especially given their facade of trustworthiness.”

Is QA “solved” by Evidence-grounded LLMs?

1. Maybe because
 1. Evidence-grounded models still suffer from hallucination.
 2. LLMs still cannot solve logic well.



Let's call the larger number x and the smaller number y . From the information given, we can set up the following equations:

A.

1. $x = 3y$ (the larger number is three times the smaller number)
2. $y + 20 = x + 6$ (adding 20 to the smaller number equals 6 more than the larger number)

B.

We can substitute the first equation into the second equation:

$$y + 20 = 3y + 6$$

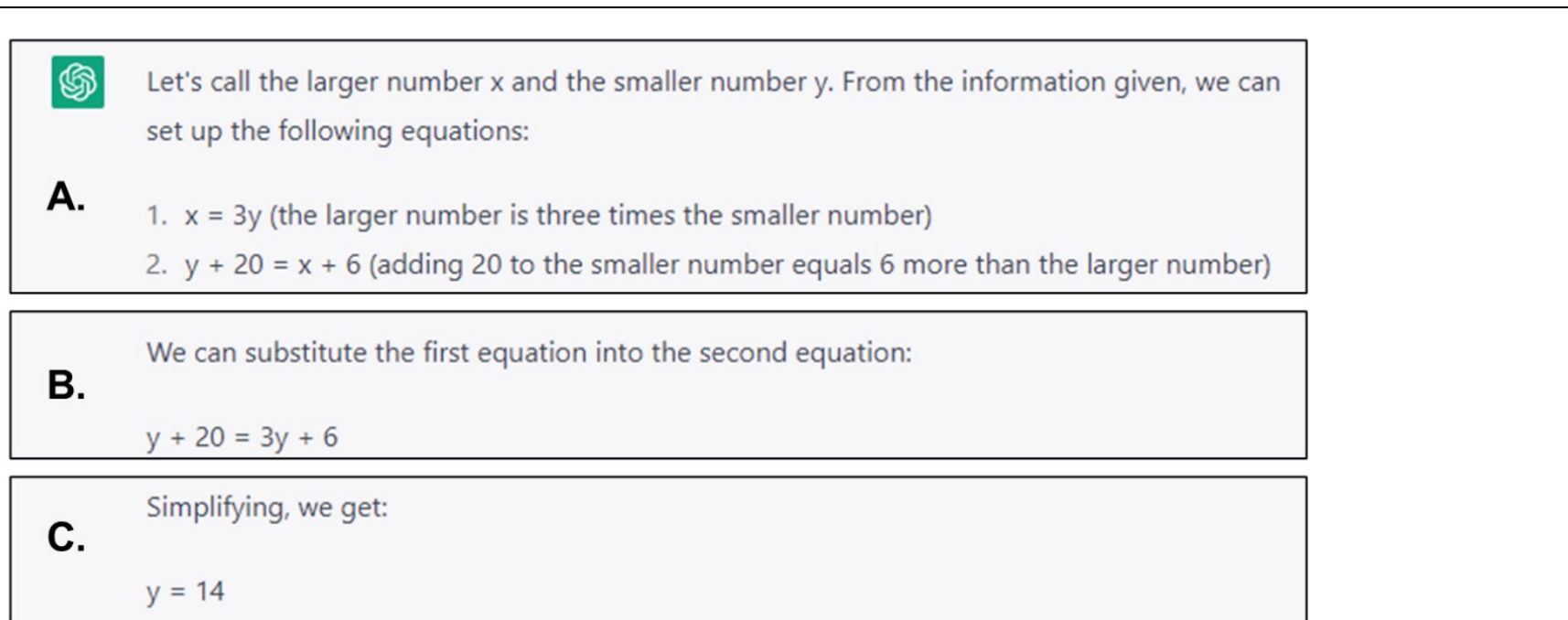
C.


Simplifying, we get:

$$y = 14$$

Figure 1: ChatGPT's response (Jan. 24, 2023) to MWP *One whole number is three times a second. If 20 is added to the smaller number, the result is 6 more than the larger.* In Step A it correctly identifies the set of equations needed to solve the problem and correctly simplifies it in Step B. However, it fails to correctly perform the algebraic operation in Step C (it should state $2y = 14$). This leads ChatGPT to obtain an incorrect result, returning 42 and 14 instead of 21 and 7.

Is QA “solved” by Evidence-grounded LLMs?



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Invited Talk: Marek Kadlčík

- **Today's MLMU TALK:**

[LLMs for math problems: overcoming the challenges](#)

WED, APR 10 · 5:30 PM CEST

Kadlčík, Marek, et al. "Calc-X and Calcformers: Empowering Arithmetical Chain-of-Thought through Interaction with Symbolic Systems." *The 2023 Conference on Empirical Methods in Natural Language Processing*. 2023.

**EPILOGUE:
TAKEAWAYS**

Takeaways: QA

- Question Answering, Document Retrieval, Fact-Checking, Entity Disambiguation, Multimodal Retrieval, all of this is **information retrieval**.

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- Extractive QA can be tackled **with answer start/end probability estimation**
- Open-domain QA needs to deal with multi-passage processing, with methods such as **MML** and **cross-passage normalization**.
- **Be sure to check out Czech QA dataset from MU! SQAD (Medved' and Horák, 2014).**

Takeaways: Document Retrieval

- **BM25** is a “fairly popular” baseline from “classic IR” in production-ready systems today. With standard BM25, one has two hyperparameters to control:
 - (a) term saturation
 - (b) long-document bias

Recent Directions, Literature, etc.

Neural Document Retrieval

Contriever/mContriever — Unsupervisedly pretrained dense retrieval (also multilingual, but no Czech), sometimes matching closely supervised approaches, well generalizing.

LaBSE — Symmetric embeddings for textual similarity (not query-document) over 109 languages, trained in a supervised way (parallel sentences) and unsupervised way.

ColBERTv2 — SOTA multi-vector learned dense retrieval model, with interesting quantization of residual vectors.

SPLADEv2 — SOTA learned sparse retrieval model.

JPR — Diverse retrieval for multi-answer questions.

Baleen — Multi-hop retrieval for multihop questions.

Open-Domain Question Answering

ATLAS — Unsupervisedly pre-trained evidence-grounded LLM (11B).

REATT — A joint retrieval-reader model for both, retrieval and LM.

DENSEPHRASES — All potential short answers on Wikipedia are encoded into gigantic index, answer is retrieved directly (no reader part!).

Open-Domain Fact-Checking

Claim-Dissector — Our new work on interpretable evidence-grounded fact-checking.

General Model Pretraining

MetalCL — A model pre-trained for learning to learn from context (so-called in-context learning).

No links included, IR it out! 😊

NEURAL DOCUMENT RETRIEVAL

Martin Fajčík
MUNI PV211 2024

Last edited: 15.04.2024

Outline

Dense retrieval vs Sparse retrieval

Dense Retrieval - Dense Passage Encoder

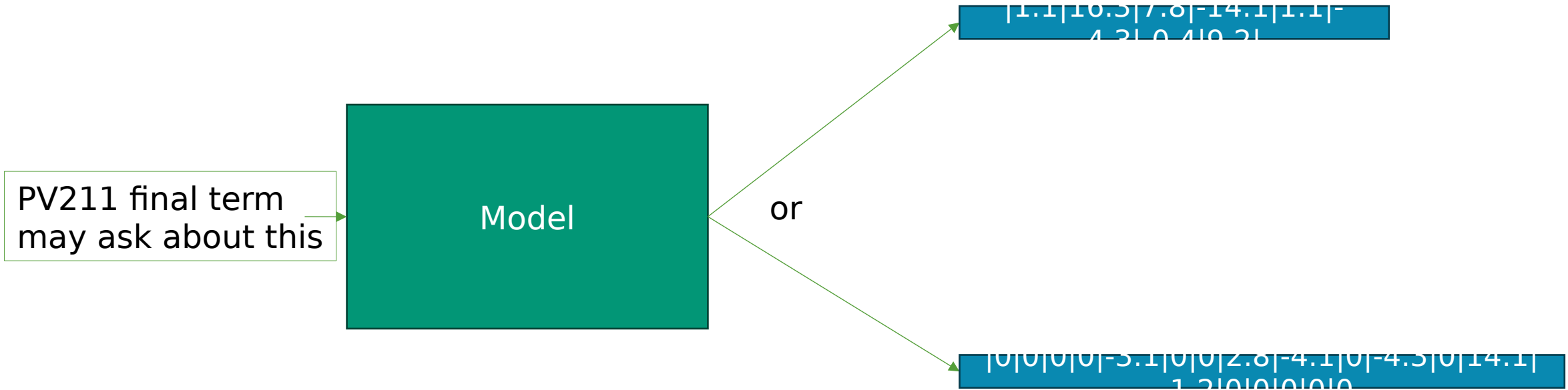
Neural Reranking - Cross-Encoder

Dense Retrieval - Contriever

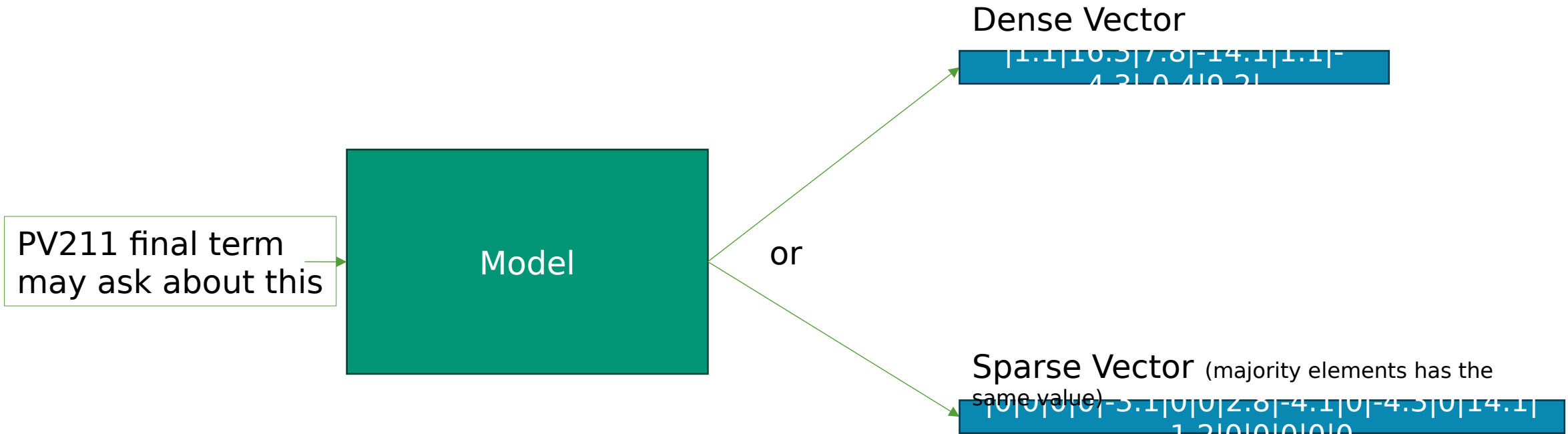
Sparse Retrieval - SPLADE

Dense Retrieval - ColBERT

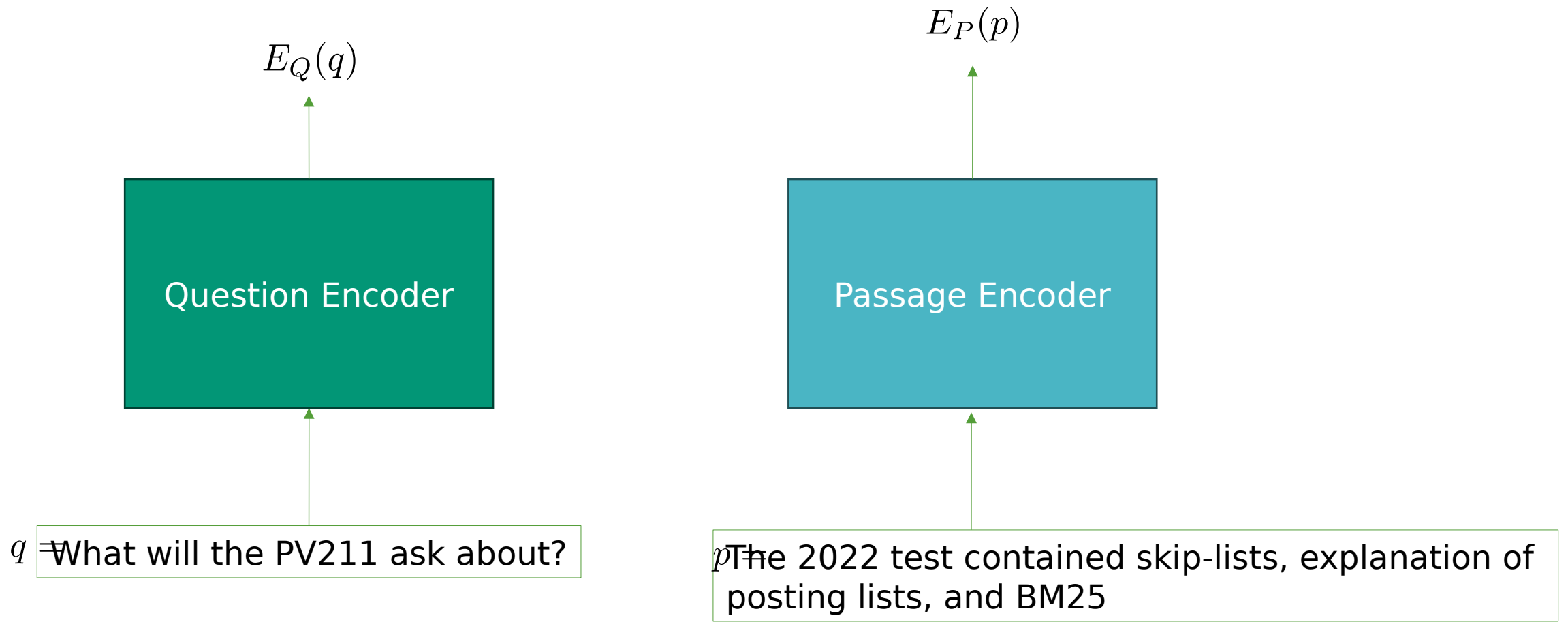
Dense Retrieval vs Sparse Retrieval



Dense Retrieval vs Sparse Retrieval



Dense Passage Retrieval



Dense Passage Retrieval

- The similarity function between two representations

$$\text{sim}(q, p) = E_Q(q)^\top E_P(p)$$

- Assume dataset with m training instances

$$\mathcal{D} = \{(q_i, p_i^+, p_{i,1}^-, p_{i,2}^-, \dots, p_{i,n}^-)\}_{i=1}^m$$

- Each instance contains one question and one relevant (positive) passage along with n irrelevant (negative) passages

Dense Passage Retrieval Training

- Cross-Entropy Contrastive Loss

$$L(q_i, p_i^+, p_{i,1}^-, p_{i,2}^-, \dots, p_{i,n}^-) = -\log \frac{\exp(\text{sim}(q_i, p_i^+))}{\exp(\text{sim}(q_i, p_i^+)) + \sum_{j=1}^n \exp(\text{sim}(q_i, p_{i,j}^-))}$$

- Hyperparameters and Model choices
 - Encoder and Decoder are both based on **BERT** pre-trained models
 - 21M of **100 words** passages of Wikipedia were indexed
 - Each passage is also prepended with the **title** of the Wikipedia article where the passage is from, separated with a [SEP] token
 - batch size **128**
 - Learning rate 1e-5, using Adam optimizer, linear

scheduling with warmup rate 0.1, and dropout 0.1

Dense Passage Retrieval Inference

- Index Construction
 - Create embeddings for all (21M) passages, using **passage encoder**.
 - This takes a lot of memory (fp16 of 21M 768 dimensional embeddings ~ 32 GB)
- Query Time
 - Use **query encoder** to encode question.
 - Find **nearest neighbor** doing full dot-product ($O(n)$) with 21M embeddings.
 - Then compute **arg top-K**, to find K nearest values.
 - (Optional) use **approximate nearest neighbor methods**, with logarithmic expected computational complexity, such as [HNSW](#).

Dense Passage Retrieval Negative Sample Mining

- Top BM25 passage that does not contain answer string (original DPR was made on open-domain QA)
- In-batch negatives
- Pros and Cons of both? (discussion)



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Dense Passage Retrieval Mining

Negative Sample

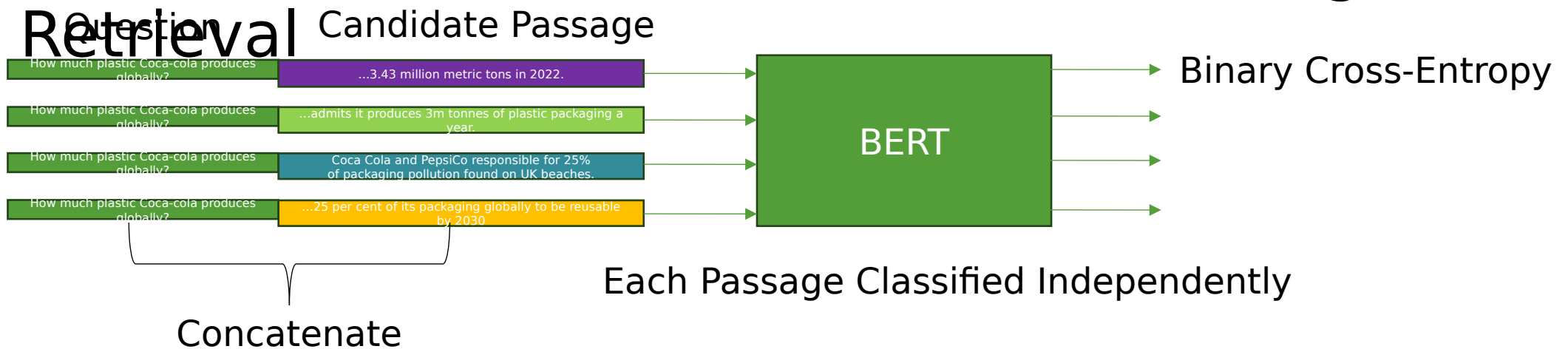
- Top BM25 passage that does not contain answer string (original DPR was made on open-domain QA)
 - C: Answer list is non-exhaustive, possibility of **False negatives**
 - C: Unclear how to mine for non-QA applications
 - P: BM25 is unsupervised
 - P: BM25 provides near-to-relevant negatives
- In-batch negatives
 - P: Cheaply obtained, no need for extra encoding
 - C: Requires **large** batch size



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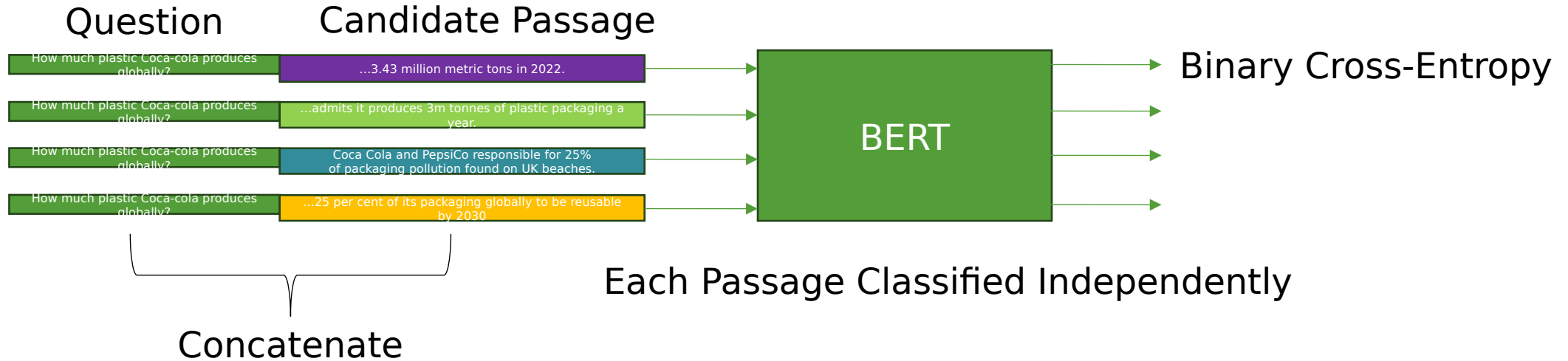
Cross-Encoder Reranking

- Cross-Encoder tends to work better than Bi-Encoder
- Cross-Encoder can't be used for (First stage)



Nogueira, Rodrigo, and Kyunghyun Cho. "Passage Re-ranking with BERT." *arXiv preprint arXiv:1901.04085* (2019).

Cross-Encoder Reranking



- Reranking dataset (from the original paper)
 - Positives: relevant passage from dataset.
 - Negatives: top-1000 non-relevant passages.

Nogueira, Rodrigo, and Kyunghyun Cho. "Passage Re-ranking with BERT." *arXiv preprint arXiv:1901.04085* (2019).

Contriever

Parallels with DPR

- Cross-Entropy Loss similar to DPR
 - τ is a temperature hyperparameter (0.05, in pretraining and finetuning)

$$\mathcal{L}(q, k_+) = - \frac{\exp(s(q, k_+)/\tau)}{\exp(s(q, k_+)/\tau) + \sum_{i=1}^K \exp(s(q, k_i)/\tau)},$$

- Based on **bi-encoder** BERT architecture (same as DPR), but encoder is **shared**
- Inference is the same as with DPR

Contriever

Unsupervised Pretraining

- Pretraining with **Independent cropping**
 - **Positive** samples are random subsequences of the same document in pre-training corpus.
 - “We use the random cropping data augmentation, with documents of **256 tokens** and span sizes sampled between **5% and 50% of the document** length. Documents are simply random piece of text sampled from a mix between Wikipedia and CCNet data, where half the batches are sampled from each source. We also apply **token deletion** with a probability of 10%.”

Contriever

Unsupervised Pretraining

- Pretraining with **Independent cropping**
 - **Negative** samples come from
 - In-batch negatives (with very large batch 2048)
 - MoCo algorithm (He et al., 2020)

Gautier Izacard, Mathilde Caron, Lucas Hosseini, Sebastian Riedel, Piotr Bojanowski, Armand Joulin, and Edouard Grave. 2022. Unsupervised dense information retrieval with contrastive learning. TMLR.

Kaiming He, Haoqi Fan, Yuxin Wu, Saining Xie, and Ross Girshick. **Momentum contrast** for unsupervised visual representation learning. In Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition, pp. 9729–9738, 2020

Contriever Unsupervised Pretraining

- MoCo algorithm
 - Store **representations from last N previous batches** in a queue and use them as (cheap) negative examples in the loss.
 - The gradients for similarity with these representations is only computed w.r.t. parameters of the **“query”** encoder.
 - As the model might sometimes change rapidly, reusing the old representations might **lead to a drop of performance when the network rapidly changes during training.**
 - Hence authors define document encoder is an exponential average of query encoder.
 - At every training update step:
 - Query network θ_q is updated via gradient computed from SGD-like optimizer.
 - Document network θ_d is updated from the new parameters of query network θ_q .

Gautier Izacard, Mathilde Caron, Lucas Hosseini, Sebastian Riedel, Piotr Bojanowski, Armand Joulin, and Edouard Grave. 2022. Unsupervised dense information retrieval with contrastive learning. TMLR.

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• Authors use $m=0.9995$

Contriever

Unsupervised Pretraining Hyperparameters

Optimizer: AdamW

Learning rate: 5e-5

Batch size: 2048

Steps: 500,000

Queue: 131,072 (representations from last 64 batches were considered)

Gautier Izacard, Mathilde Caron, Lucas Hosseini, Sebastian Riedel, Piotr Bojanowski, Armand Joulin, and Edouard Grave. 2022. Unsupervised dense information retrieval with contrastive learning. TMLR.

Kaiming He, Haoqi Fan, Yuxin Wu, Saining Xie, and Ross Girshick. **Momentum contrast** for unsupervised visual representation learning. In Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition, pp. 9729–9738, 2020

Contriever Supervised Finetuning

- Batch size 1024
- Learning rate 1e-5
- Negatives:
 - First phase: 20k steps only with in-batch negatives
 - Second phase: in-batch negatives in 90% of cases, 10% of cases are **hard negatives** mined from the model trained in phase 1 (how many is not documented)

SPLADE (V2)

- Learning **sparse** vectors for retrieval using BERT-based model.

SPLADE (V2)

- Learning **sparse** vectors for retrieval using BERT-based model.

- A sequence of tokens from vocabulary **V** set for question / passage:

$$t = (t_1, t_2, \dots, t_N)$$

- A sequence of contextualized representations extracted as

$$h_1, h_2, \dots, h_N = \text{BERT}(t)$$

SPLADE (V2)

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$$h_1, h_2, \dots, h_N = \text{BERT}(t)$$

- Next, let's reuse BERT-pretraining "head" to compute importance scores of
 - i-th position representation to the
 - j-th vocabulary token
$$w_{ij} = \text{transform}(h_i)^\top E_j + b_j$$

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- **E_j** is a token-embedding matrix of BERT
- **b_j** is a token-embedding bias
- **transform** is a non-linear function $\text{transform}(h_i) = \ln(\text{GeLU}(Wh_i))$
- both learned during BERT pretraining

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- E_j is a token-embedding matrix of BERT
 - b_j is a token-embedding bias
 - **transform** is a non-linear function
 - both learned during BERT pretraining
-
- **w_{ij}** are actually pre-softmax scores of i -th representation h_i during pretraining

SPLADE (V2)

$$w_{ij} = \text{transform}(h_i)^\top E_j + b_j$$

$$w_j = \max_{i=0}^N \log(1 + \text{ReLU}(w_{i,j})) \quad \text{ReLU}(x) = \max(x, 0]$$

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- Sanity check: What is the size of vector w ?

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$$w_{ij} = \text{transform}(h_i)^T E_j + b_j$$

$$w_j = \sum_{i=0}^N \log(1 + \text{ReLU}(w_{i,j})) \quad \text{ReLU}(x) = \max(x, 0]$$

- Sanity check: What is the size of vector w ?
- $|w| = |V|$ (same as size of vocabulary)

SPLADE Training

- Uses the same style contrastive loss as DPR

$$\text{sim}(q, p) = w_q^\top w_p$$

$$L_{\text{rank}}(q_i, p_i^+, p_{i,1}^-, p_{i,2}^-, \dots, p_{i,n}^-) = -\log \frac{\exp(\text{sim}(q_i, p_i^+))}{\exp(\text{sim}(q_i, p_i^+)) + \sum_{j=1}^n \exp(\text{sim}(q_i, p_{i,j}^-))}$$

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- Combined with **sparsity losses** for query and passage representations

$$L = L_{\text{rank}}(q_i, p_i^+, p_{i,1}^-, p_{i,2}^-, \dots, p_{i,n}^-) + \lambda_q L_{\text{sparse}}(w_q) + \lambda_d L_{\text{sparse}}(w_d)$$

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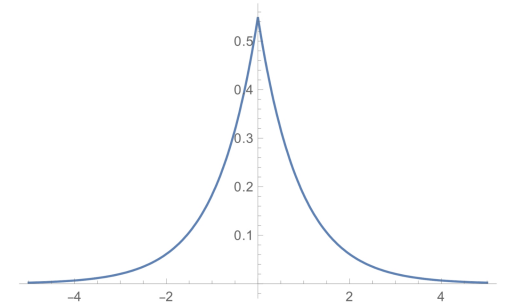
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Tunable hyperparameters that control sparsity strength

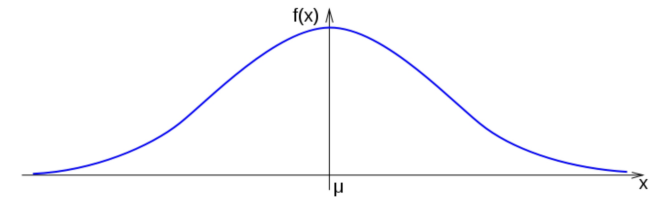
Sparsity Loss (vanilla)

- Common sparsity losses are L1/L2 regularization loss

$$L_1(w) = \sum_i |w_i|$$



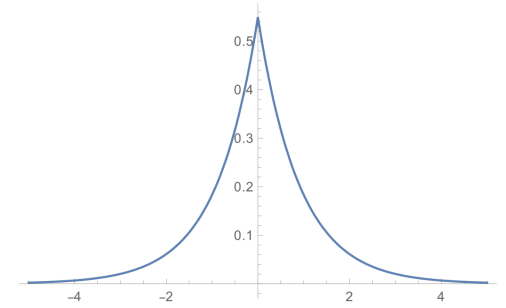
$$L_2(w) = \sum_i w_i^2$$



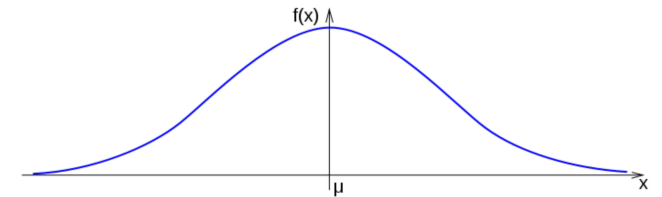
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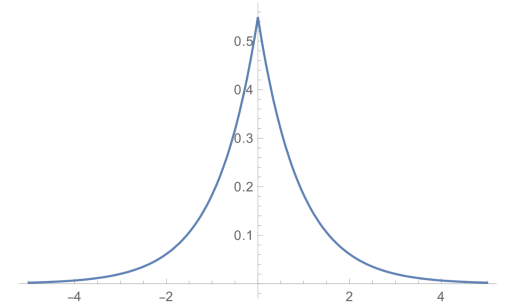


$$\begin{aligned} \lambda L_2(w) &\propto -\log \prod_i \mathcal{N}(w_i : 0, \sigma^2) = -\sum_{i=1}^n \log\left(\frac{1}{\sqrt{2\pi}} \frac{1}{\sigma^2} \exp\left(-\frac{w_i^2}{2\sigma^2}\right)\right) = \\ & n \log(\sqrt{2\pi}) + n \log \sigma^2 + \sum_i \frac{1}{2\sigma^2} w_i^2 \end{aligned}$$

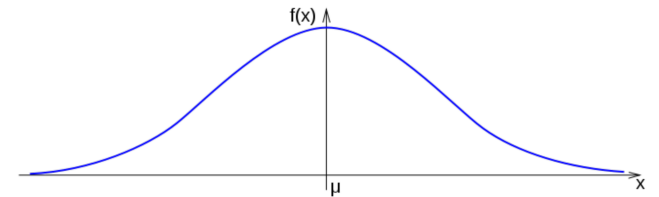
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Offsetting loss won't affect the optimization ($\operatorname{argmax} [f(x)] = \operatorname{argmax} [f(x)+c]$)

Sparsity Loss (complexity analysis)

- However, different representations might have same representations not sparse
 - L^* losses only care about sparsity across vector dimension

p1

| | | | | | |
|---|---|---|---|---|---|
| 0 | 2 | 0 | 0 | 0 | 3 |
|---|---|---|---|---|---|

p2

| | | | | | |
|---|---|---|---|---|---|
| 0 | 4 | 0 | 0 | 0 | 8 |
|---|---|---|---|---|---|

p3

| | | | | | |
|---|---|---|---|---|---|
| 0 | 1 | 0 | 0 | 0 | 2 |
|---|---|---|---|---|---|

- Expected # of FLOPS for $\text{sim}(w_q, w_p)$ is $\mathbf{d/p}$,
where \mathbf{d} is $|w|$ **dimensionality** (V) and
 $\mathbf{1/p}$ is average **proportion** of non-0 elements in w

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p2

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|---|---|---|---|---|---|
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|---|---|---|---|---|---|

p3

| | | | | | |
|---|---|---|---|---|---|
| 0 | 1 | 0 | 0 | 0 | 2 |
|---|---|---|---|---|---|

How to enforce sparsity across vectors?

FLOPS Sparsity Loss

- Estimate expected w_j across minibatch of M elements (p_1, p_2, \dots, p_M)
- Enforce sparsity of such estimate
- Expected # of FLOPS for $\text{sim}(w_q, w_p)$ is $\mathbf{d/p^2}$, where \mathbf{d} is $|w|$ **dimensionality** (V) and $\mathbf{1/p}$ is average **proportion** of non-0 elements in w

$$\bar{a}_j = \frac{1}{M} \sum_{i=0}^M w_j^{(p_i)} \quad L_{FLOPS} = \sum_{j \in V} \bar{a}_j^2$$

- The probability that n -th element is sparse is the same for all n

SPLADE Training

- From the paper

3.4 Distillation and hard negatives

We also incorporate distillation to our training procedure, following the improvements shown in [12]. The distillation training is done in two steps: (1) we first train both a SPLADE first-stage retriever as well as a cross-encoder reranker¹ using the triplets generated by [12]; (2) in the second step, we generate triplets using SPLADE trained with distillation (thus providing harder negatives than BM25), and use the aforementioned reranker to generate the scores needed for the Margin-MSE loss. We then train a SPLADE model from scratch using these triplets and scores. The result of the second step is what we call DistilSPLADE-max.

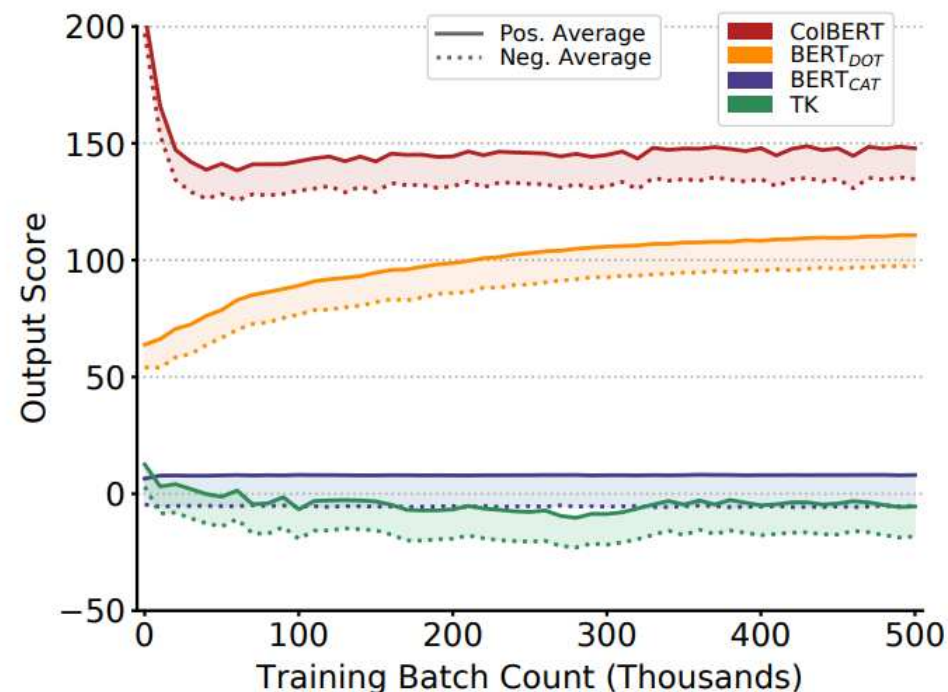
DistilSPLADE-max Training

1. Get triples for MS-MARCO from traditional system, picking negatives at random from top-1000 ranked passages. Construct first dataset of triplets (D#1)
2. Train Cross-Encoder on D#1 (CE#1).
3. Train SPLADE#1 on D#1 using **distillation** from CE#1.
4. Generate new negatives from SPLADE #1 top-K retrieved; construct new dataset of triplets (D#2).
5. Train Cross-Encoder on D#2 (CE#2).
6. Train SPLADE#2 on D#2 using **distillation** from CE#2.

Distillation via Margin-MSE

Margin Mean Squared Error Loss

- Assume **Teacher Model** score function M_T .
 - E.g. BERT output projected to a scalar, as in Cross-Encoder.
- And **Student Model** score function M_S .
 - E.g., DPR/Contriever/SPLADE model's dot-product.
- To avoid enforcing specific scores from M_T to M_S **only margins** can be distilled from Teacher into Student.



Notes:

- Model Distillation = Transferring information between two models, training Student Model from Teacher Model.
- Score function = Similarity function

Distillation via Margin-MSE

Margin Mean Squared Error Loss

- Assume **Teacher Model** score function M_T .
 - E.g. BERT output projected to a scalar, as in Cross-Encoder.
- And **Student Model** score function M_S .
 - E.g., DPR/Contriever/SPLADE model's dot-product.
- Loss function for triples of queries Q , positive passages P^+ , negative passages P^- .

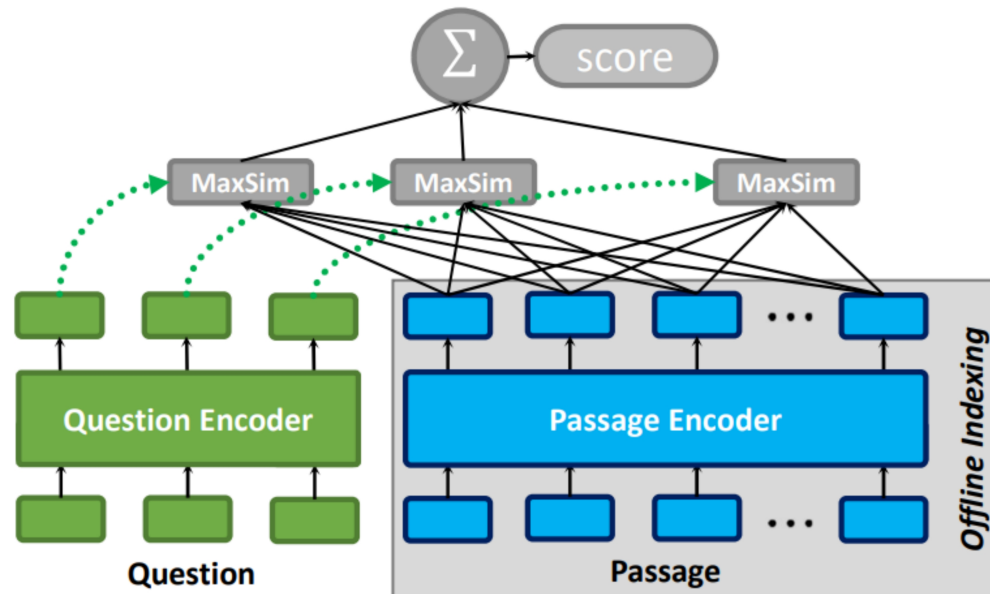
$$L(Q, P^+, P^-) = \text{MSE}(\underbrace{M_S(Q, P^+) - M_S(Q, P^-)}_{\text{Student's error margin}}, \underbrace{M_T(Q, P^+) - M_T(Q, P^-)}_{\text{Teacher's error margin}})$$

$$\text{MSE}(s, t) = \frac{1}{|t|} \sum_{i=0}^{|t|-1} (s_i - t_i)^2$$

SPLADE Inference

- Similar to DPR/Contriever.
- Sparse-vector products, are efficiently implemented in Numba/Numpy.

COLBERT v2



- **Multi-vector** query/document representations.
- Middle ground **between** cross-encoder and bi-encoder.
- Can be used for (first-stage) **retrieval**.
- However, it's large passage index makes it suited for **smaller collections**.

Santhanam, Keshav, et al. "PLAID: an efficient engine for late interaction retrieval." *Proceedings of the 31st ACM International Conference on Information & Knowledge Management*. 2022.

COLBERT_{v2}

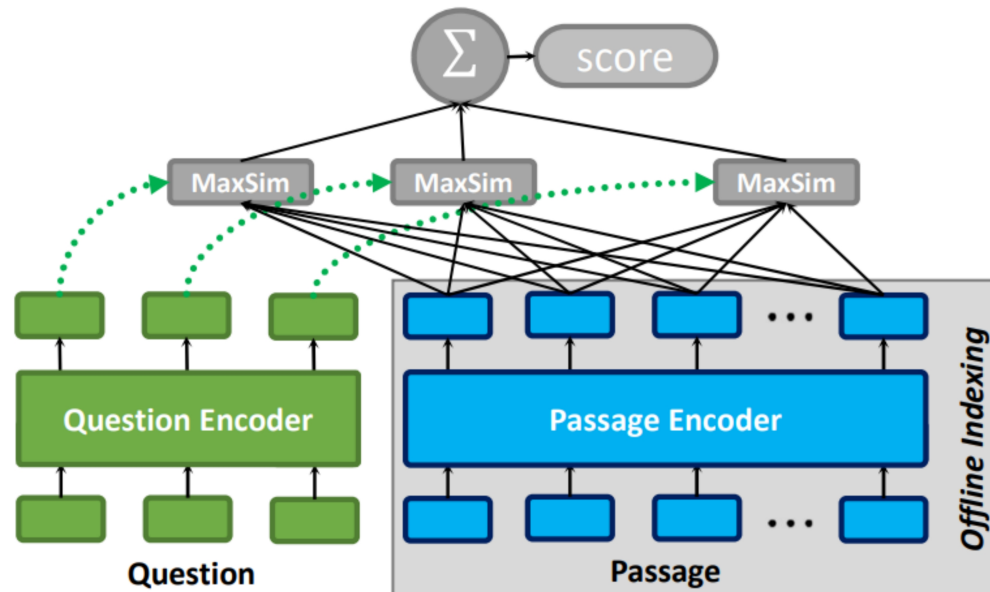
- Punctuation symbol embeddings are removed.
- Query is always represented with $N_q (=32)$ tokens. Shorter queries are padded.
- Documents are split so that they contain $N_d (=300 \text{ on BEIR})$ representations.
- Representations are low-dimensional
 - (Each DPR vector has 768d, each of COLBERT's vectors is 128d).

• Each vector representation is L2 normalized (=

Santhanam, Keshav, et al. "PLAID: an efficient engine for late interaction retrieval." *Proceedings of the 31st ACM International Conference on Information & Knowledge Management*. 2022.

COLBERT

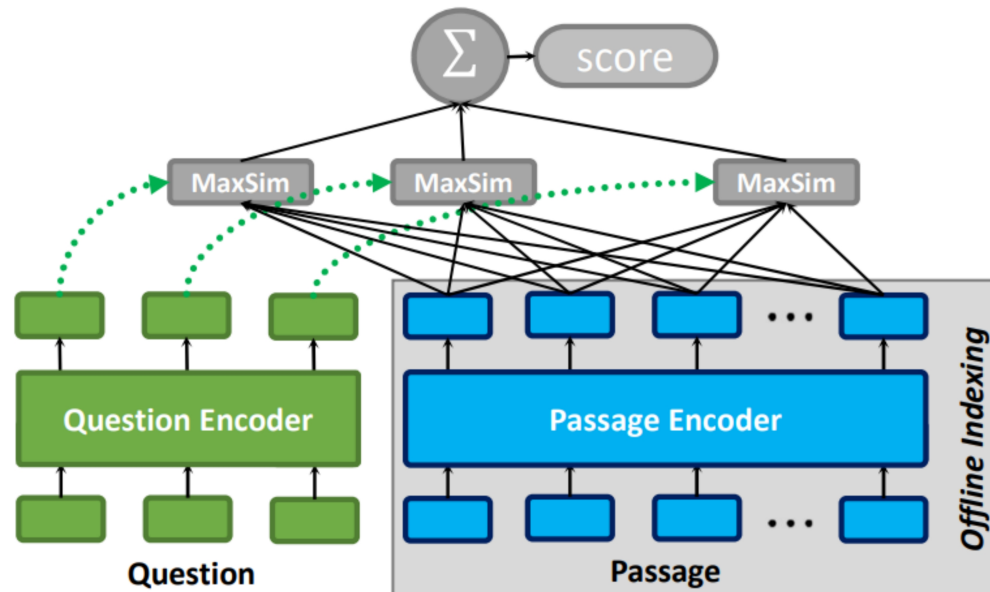
MaxSim



- Each token in Question/Passage is encoded into vector using BERT.
- Similarity between query and passage is computed between two matrices **Q** and **P**.
- Max-pooled **over document** representations.

COLBERT

MaxSim



- Each token in Question/Passage is encoded into vector using BERT.
- Similarity between query and passage is computed between two matrices **Q** and **P**.
- Max-pooled **over document** representations.

$$sim(Q, P) = \sum_{i=0}^{N_q} \max_{j=0}^{N_d} \underbrace{Q_i^\top P_j}_{\text{Cosine Similarity}}$$

COLBERT

- Similar to previous methods.
- V2 uses hard negatives, cross-encoder distillation, in-batch negatives.

COLBERT Inference

- (PLIND) Tomorrow practical

MTEB Massive Text Embedding Benchmark

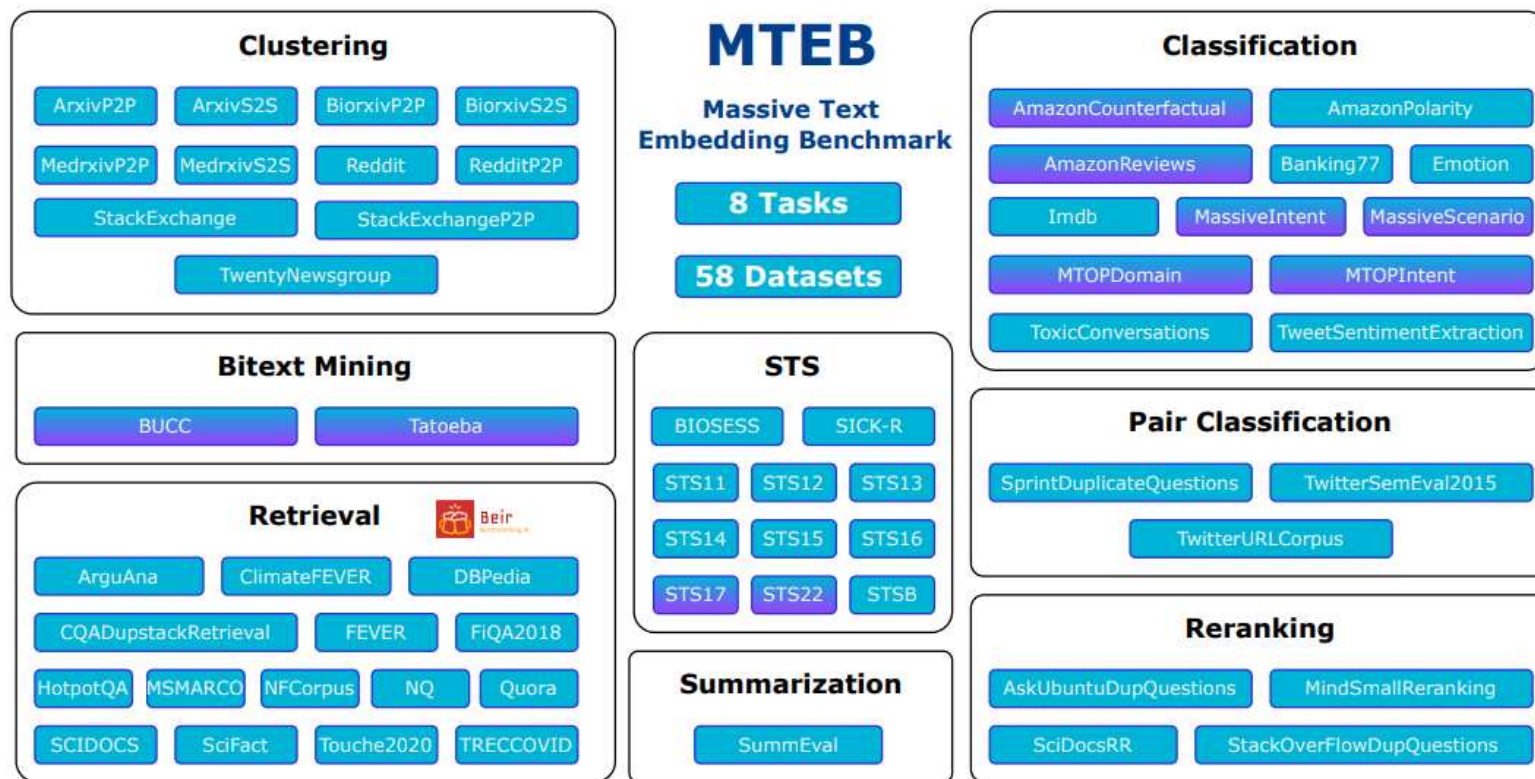


Figure 1: An overview of tasks and datasets in MTEB. Multilingual datasets are marked with a purple shade.

- <https://huggingface.co/spaces/mteb/leaderboard>

Muennighoff, Niklas, et al. "MTEB: Massive Text Embedding Benchmark." *Proceedings of the 17th Conference of the European Chapter of the Association for Computational Linguistics*. 2023.

COLBERT RETRIEVAL (PRACTICAL)

Martin Fajčík
MUNI PV211 2024

Last edited: 16.04.2024

COLBERT Inference

1. Indexing

- Storing all vectors for all documents in fp16 has unrealistic memory requirements.
 - For example, 100k documents, 124 tokens on average, fp16 index only for embeddings would take $100,000 \times 124 \times 2 \times 128 \sim 3,17$ GB.

COLBERT Inference

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 - For example, 100k documents, 124 tokens on average, fp16 index only for embeddings would take $100,000 \times 124 \times 2 \times 128 \sim 3,17$ GB.

2. Approximate Retrieval

- Exact retrieval is too slow
 - 32 products on matrix with $100,000 \times 124 \sim 12,400,000$ embeddings

COLBERT PLAID

Indexing

1. Centroids:

- Find a set of centroids using **K-means** on random subsample of corpus C.
 - Subsample size \sim square root of # of documents.
 - $K \sim$ rounded down to nearest power of 2 for $16 \times$ square root of (# of embeddings).

COLBERT

PLAID Indexing – CASE

STUDY

Assume ColBERTv2 model with each passage having at most 300 tokens.

Next, assume there is

- 100,000 passages in corpus (≤ 300 tokens).
- 124 tokens per passage on average.
- model with 128 dimensional vectors.
- 16-bit float type precision used.

Exercise 1

How much memory will centroid vectors cost.

COLBERT

PLAID Indexing – CASE

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- 124 tokens per passage on average.
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- 16-bit float type precision used.

Exercise 1

How much memory will centroid vectors cost.

Solution

We have 124 tokens per passage, and 100k passages, this leads to 12 400 000 raw embeddings. K is rounded down to nearest power of 2 for $16 \times \text{square root of } (\# \text{ of embeddings})$. That is K is rounded down to the nearest power of 2 of $\sim 56,000$, that is 32 768. Each embedding is save if float 16 type, so the total size in bytes is:

2 bytes x 128 dimensions x 32 768 centroids = 8388608 bytes \sim 8.4 MB.

COLBERT PLAID

Indexing

2. Compressed Representations:

- Each passage is encoded into matrix P .
- Embeddings in P are compressed.

COLBERT

PLAID Indexing - Compression

Mechanism

2. Compressed Representations:

- Each vector p is stored as
 - index of its nearest centroid C_p , and
 - a residual vector $r_p = p - C_p$
- Each dimension of residual vectors are further quantized into 2 bits.
 - **How to quantize?**
- Theoretical space requirements for 1 representation (b=2, n=128)
 $\log[|C|] + bn$

COLBERT

PLAID Indexing - Compression

Mechanism

2. Compressed Representations:

- Each vector p is stored as
 - index of its nearest centroid C_p , and
 - a residual vector $r_p = p - C_p$
- Each dimension of residual vectors are further quantized into 2 bits.
 - Simple quantization = perform **K**-means on each dimension, assign its fp32 intervals into 4 clusters.
- Theoretical space requirements for 1 representation
($b = 2, n = 128$)
 $\log_2 |C| + n \cdot b$

COLBERT

PLAID Indexing - Compression

Mechanism

2. Compressed Representations:

- Theoretical space requirements for 1 representation
($\log_2 C, n = 128$)
- In practice, authors assume there are up to 2^{32} centroids, so
 - **How many bytes will each vector representation consume?**

COLBERT

PLAID Indexing – Compression

Mechanism

2. Compressed Representations:

- Theoretical space requirements for 1 representation ($\log_2 C, n = 128$)
- In practice, authors assume there are up to 2^{32} centroids, so
 - $32 + 2 \times 128 = 288$ bits = 36 bytes
- **How much memory it saves from naïve fp16 implementation?**

COLBERT

PLAID Indexing - Compression

Mechanism

2. Compressed Representations:

- Theoretical space requirements for 1 representation ($\log_2 C, n = 128$)
- In practice, authors assume there are up to 2^{32} centroids, so
 - $32 + 2 \times 128 = 288$ bits = 36 bytes
- How much memory it saves from naïve fp16 implementation?
 - Naïve = 2 bytes x 128 = 256 bytes (7.1x less)

COLBERT

PLAID Indexing – CASE STUDY

Exercise 2:

Assume ColBERT model with each passage having at most 300 tokens.

Next, assume there is

- 100,000 passages in corpus (≤ 300 tokens).
- 124 tokens per passage on average.
- model with 128 dimensional vectors.
- 16-bit float type precision used.

Estimate the size of saved compressed vectors.

COLBERT

PLAID Indexing – CASE STUDY

Exercise 2:

Assume ColBERT model with each passage having at most 300 tokens.

Next, assume there is

- 100,000 passages in corpus (≤ 300 tokens).
- 124 tokens per passage on average.
- model with 128 dimensional vectors.
- 16-bit float type precision used.
- 2 bits per dimension quantization.

Estimate the size of saved compressed vectors.

Solution:

We have 124 tokens per passage, and 100k passages, this leads to 12 400 000 raw embeddings. Each is indexed with centroid index (int32) and residual vector (128x 2 bits) = 32 bytes). To find out, how much embeddings belong to each passage, we further need to save passage lengths (int16 will suffice to passages < 300), So the result is:

$32 \text{ bytes} \times 12\,400\,000 + 4 \text{ bytes} \times 12\,400\,000 + 2 \text{ bytes} \times 100\,000 = 446\,600\,000 \text{ bytes} = 446,6 \text{ MB}.$

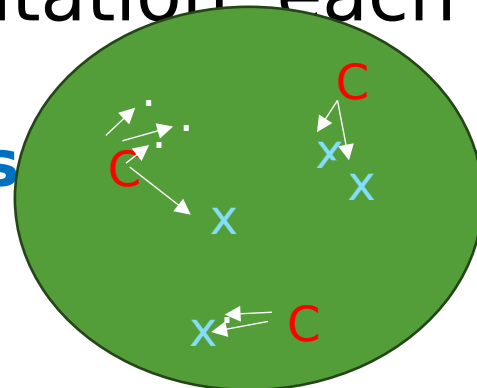
Santhanam, Keshav, et al. "PLAID: an efficient engine for late interaction retrieval." *Proceedings of the 31st ACM International Conference on Information & Knowledge Management*. 2022.

COLBERT PLAID

Indexing

3. Inverted list of passages

- For each embedding, add passage to an inverted list mapping centroids to their nearest unique passage ID.
 - If 1st embedding in P is nearest to centroid C_1 , and 2nd embedding in P is nearest to centroid C_2 , both centroids will be mapped to this passage.
- In default implementation, each passage is indexed using **uint32**.
 - **Q: How much pass** **ows to**



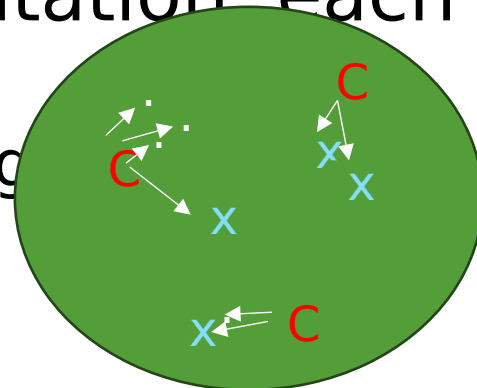
| LEGEND | |
|--------|---------------------|
| . | → passage a |
| x | → passage b |
| C | → centroid location |

COLBERT PLAID

Indexing

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 - Q: How much passage



LEGEND

- . → passage a
- x → passage b
- C → centroid location

COLBERT

PLAID Indexing – CASE

STUDY

Exercise 3:

Assume ColBERT model with each passage having at most 300 tokens.

Next, assume there is

- 100,000 passages in corpus (≤ 300 tokens).
- 124 tokens per passage on average.
- Assume each index of each passage is encoded in uint32.
- Assume each cluster is mapped to 198 passages on average.

How much memory will such an inverted index take?

COLBERT

PLAID Indexing – CASE

STUDY

Exercise 3:

Assume ColBERT model with each passage having at most 300 tokens.

Next, assume there is

- 100,000 passages in corpus (≤ 300 tokens).
- 124 tokens per passage on average.
- Assume each index of each passage is encoded in uint32.
- Assume each cluster is mapped to 198 passages on average.

How much memory will such an inverted index take?

Solution:

There is 32 768 total clusters (from Exercise 1), so $32\,768 \times 198 = 6\,488\,064$ mapped passages in total. These can be saved in a list, if we also separately save a length offset for each cluster. In this case 32 bits will suffice (using standard dtypes) to encode # of passages mapped to each cluster (remember, there can be the case when almost all passages are mapped to single cluster!).

So in total we have $6\,488\,064 \times 4 \text{ bytes} + 32\,768 \times 4 \text{ bytes} = 26\,083\,328 \text{ bytes} \sim 26 \text{ MB}$ in total.

COLBERT

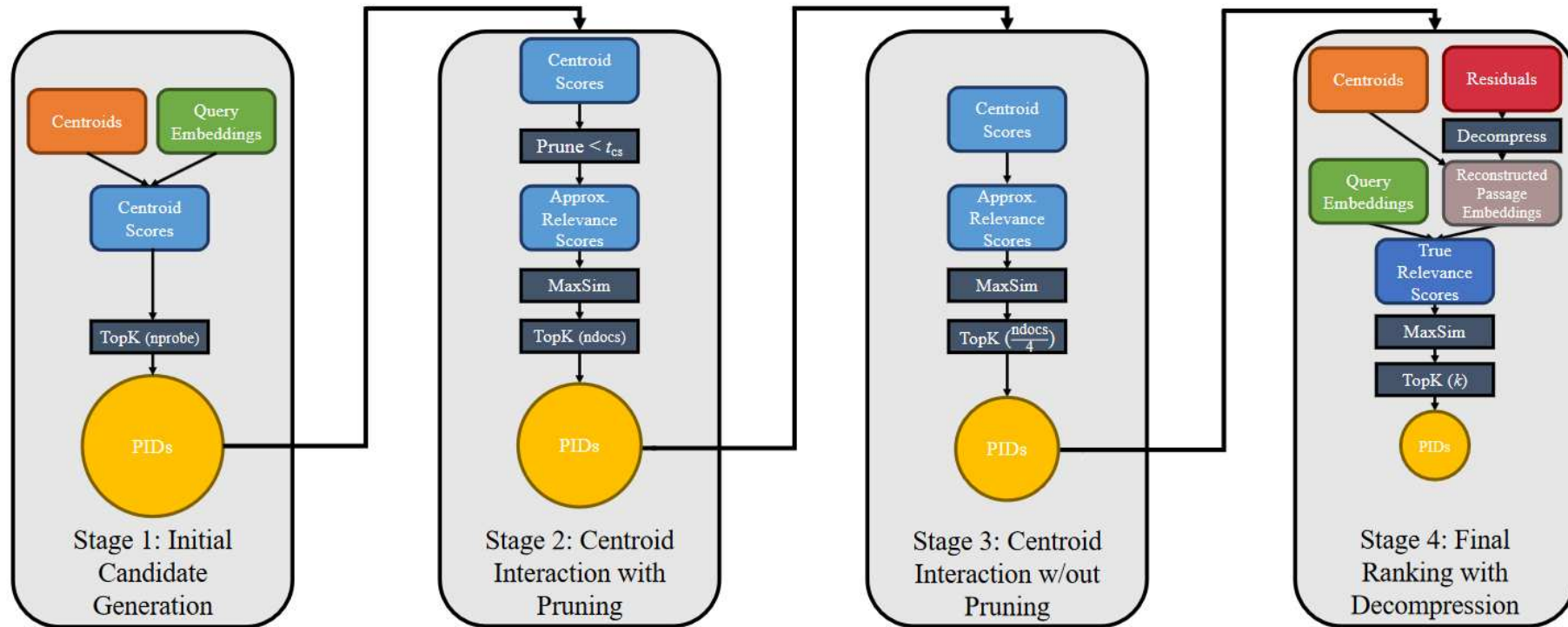
PLAID Indexing - CASE

STUDY Index Summary

- Centroids **8.4 MB**
- Embeddings **446,6 MB**
- Inverted Index **26 MB**
- **In total 481 MB**
 - **down from 3,17 GB!**
 - **ONLY ~15% OF THE ORIGINAL SIZE*.**

* - original size didn't counted in passage lengths, but that is negligible in terms of size

COLBERT Retrieval



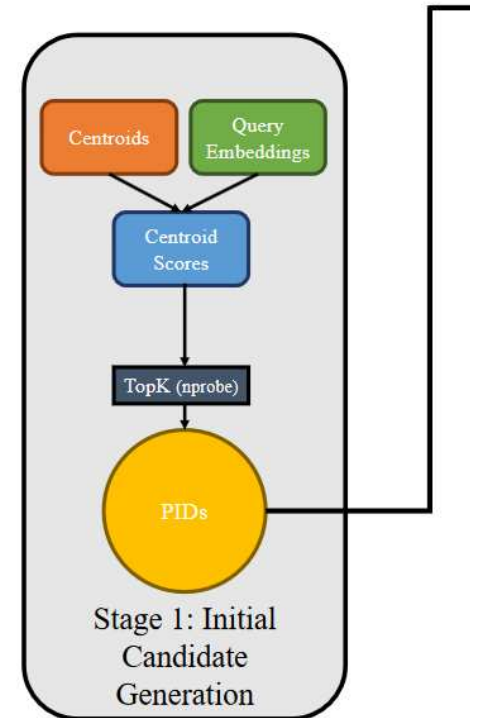
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COLBERT Retrieval

- Stage 1

- Let C be the matrix of all centroid embeddings.
- Let Q be the query embeddings, obtained after encoding query.
- Compute similarities between each $S = CQ^T$

- the passages “close” to the **top-nprobe** centroids per query token are the **initial**



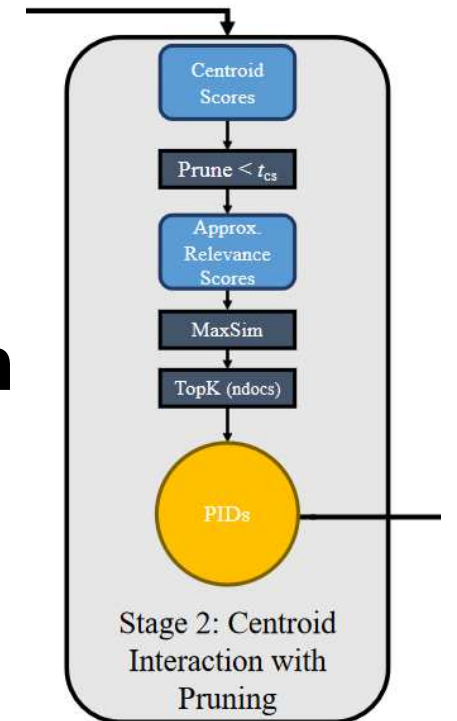
COLBERT Retrieval

- Stage 2: Representational Composition

- Suppose \mathbf{I} is the list of the centroid indices mapped to each of the tokens in the candidate set

- Compute approximate similarity, where **each token is represented by its nearest centroid embedding**

$$\tilde{D} = \begin{bmatrix} S[I_1] \\ S[I_2] \\ \vdots \\ S[I_{|P|}] \end{bmatrix} \quad S_{\tilde{D}} = \sum_{i=1}^{|\mathcal{Q}|} \max_{j=1}^{|\tilde{D}|} \tilde{D}_{i,j}$$



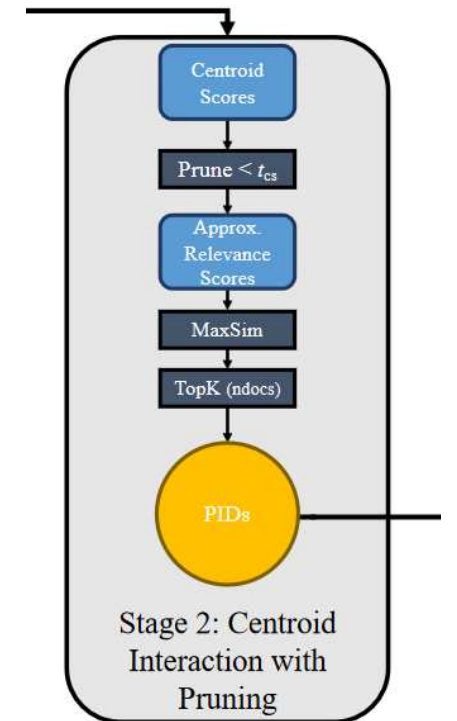
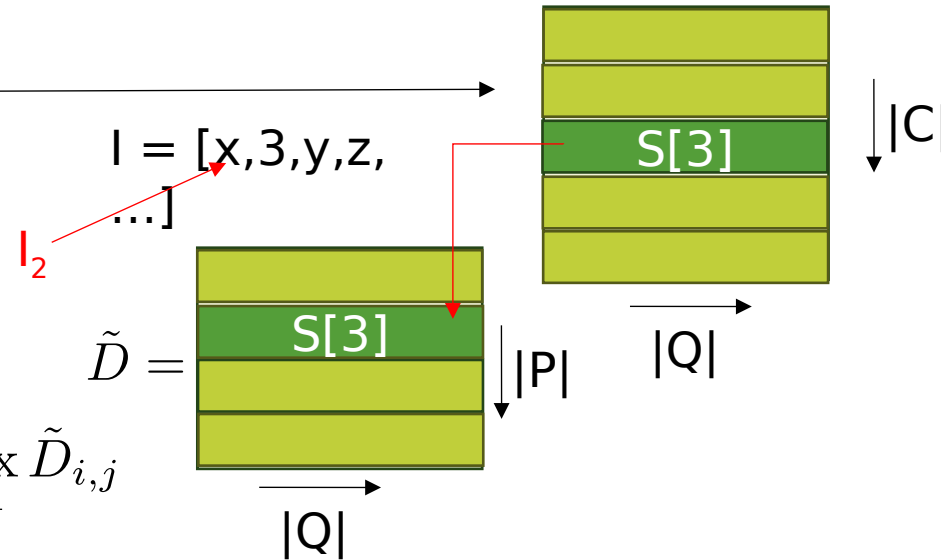
COLBERT Retrieval

- Stage 2: Representational Composition
 - Suppose \mathbf{I} is the list of the centroid indices mapped to each of the tokens in the candidate set

$$S = CQ^T$$

$$\tilde{D} = \begin{bmatrix} S[I_1] \\ S[I_2] \\ \vdots \\ S[I_{|P|}] \end{bmatrix}$$

$$S_{\tilde{D}} = \sum_{i=1}^{|\tilde{D}|} \max_{j=1}^{|\tilde{D}_i|} \tilde{D}_{i,j}$$



Santhanam, Keshav, et al. "PLAID: an efficient engine for late interaction retrieval." *Proceedings of the 31st ACM International Conference on Information & Knowledge Management*. 2022.

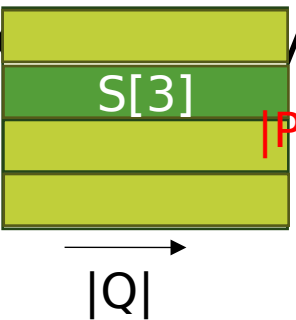
COLBERT Retrieval

- Stage 2: Pruning

- To make matrix \tilde{D} even smaller, only tokens, whose corresponding centroid i has max similarity to query higher than threshold are considered

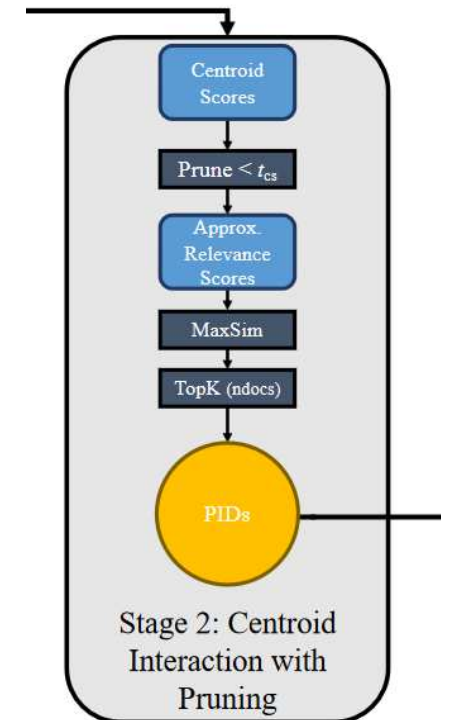
- In implementation,

these rows can be pre-flagged in S

$$\max_{j=1}^{|Q|} S_{i,j} \geq t_{cs} \quad \tilde{D} =$$


$|P|$ - (# of filtered by threshold)

The diagram shows a matrix \tilde{D} with 5 rows and $|Q|$ columns. The second row is highlighted in green and labeled $S[3]$. A red vertical bar on the right side of the matrix indicates the number of filtered rows, labeled $|P|$. An arrow below the matrix points to the right and is labeled $|Q|$.



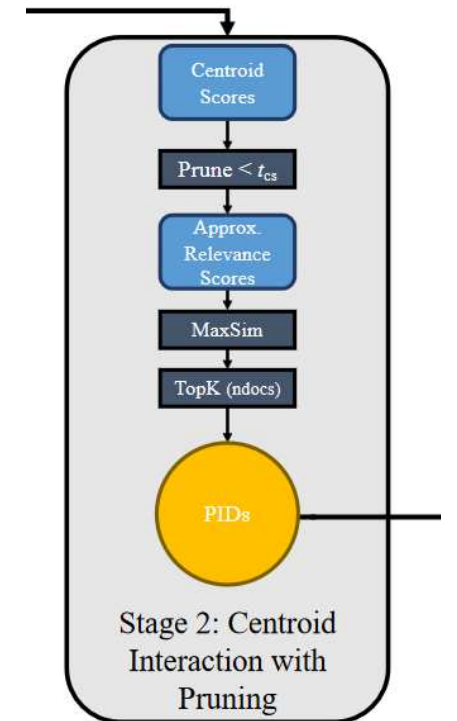
COLBERT Retrieval

- Stage 2

- Top-ndocs scoring documents are selected into

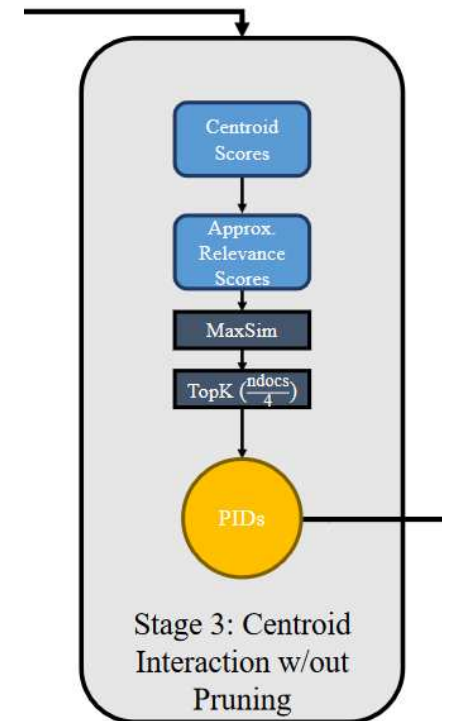
passage IDs (PIDs) candidate set for stage 3

$$S_{\tilde{D}} = \sum_{i=1}^{|\tilde{D}|} \max_{j=1}^{|\tilde{D}|} \tilde{D}_{i,j}$$



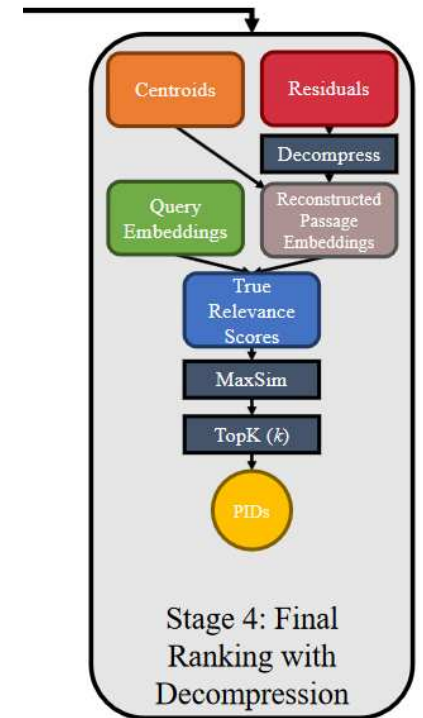
COLBERT Retrieval

- Stage 3
 - Same as stage 2, but without filtering, considering all rows of S.
 - Top-(ndocs/4) passages are selected for final processing (**Stage 4**).



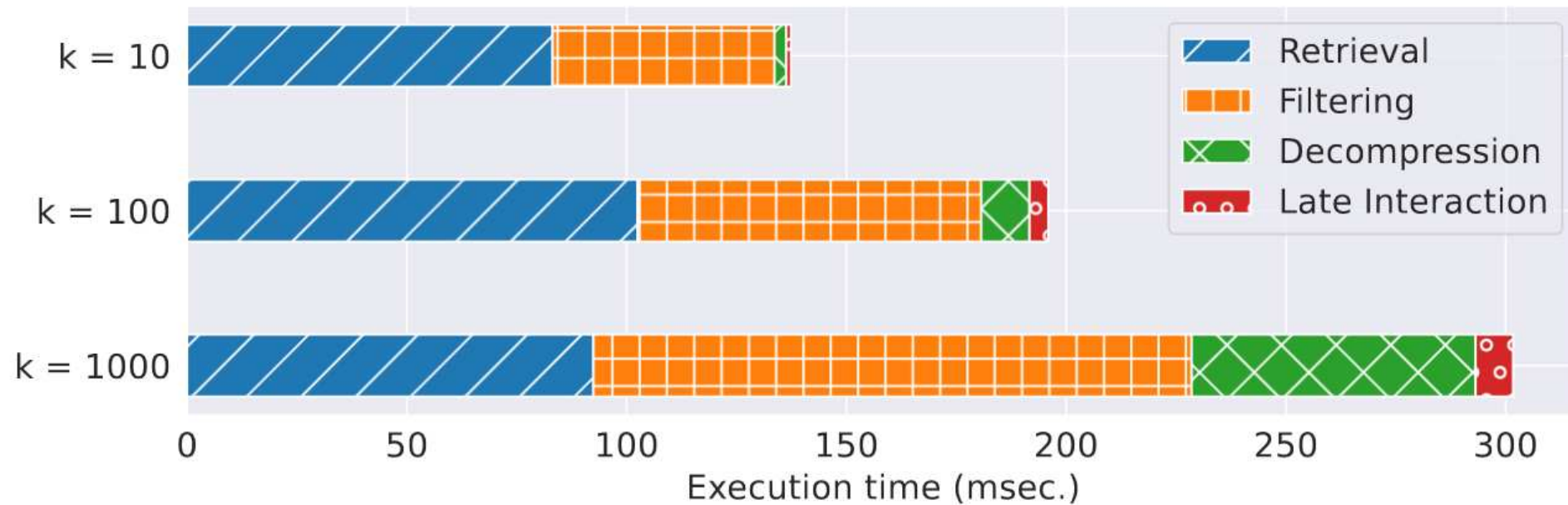
COLBERT Retrieval

- Stage 4
 - Final set of candidates is decompressed, and exact max-sim operation is computed for these in FP32.
 - All steps are done to minimize
 - candidate index lookup (looking for cluster/residual of particular passage)
 - decompressed of candidates (both steps are very slow).
 - **Board: How to do dequantization?**
 - Final **top-k** results are returned, along with similarities.



COLBERT

Retrieval Speed on MS-MARCO



PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 9: Relevance feedback & Query expansion Handout version

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Center for Information and Language Processing, University of Munich

2024-04-24

(compiled on 2024-04-24 10:06:17)

Overview

- 1 Motivation
- 2 Relevance feedback: Basics
- 3 Relevance feedback: Details
- 4 Query expansion

Take-away today

- **Interactive relevance feedback:** improve initial retrieval results by telling the IR system which docs are relevant / non-relevant
- Best known relevance feedback method: **Rocchio feedback**
- **Query expansion:** improve retrieval results by adding synonyms / related terms to the query
 - **Sources for related terms:** Manual thesauri, automatic thesauri, query logs

How can we improve recall in search?

- Main topic today: two ways of improving recall: relevance feedback and query expansion
- As an example consider query q : [aircraft] ...
- ... and document d containing “plane”, but not containing “aircraft”
- A simple IR system will not return d for q .
- Even if d is the most relevant document for q !
- We want to change this:
 - Return relevant documents even if there is no term match with the (original) query

Recall

- Loose definition of recall in this lecture: “increasing the number of relevant documents returned to user”
- This may actually decrease recall on some measures, e.g., when expanding “jaguar” with “panthera”
 - . . . which eliminates some relevant documents, but increases relevant documents returned on top pages

Options for improving recall

- Local: Do a “local”, on-demand analysis for a user query
 - Main local method: [relevance feedback](#)
 - Part 1
- Global: Do a global analysis once (e.g., of collection) to produce [thesaurus](#)
 - Use thesaurus for [query expansion](#)
 - Part 2

Google examples for query expansion

- One that works well
 - *~flights -flight*
- One that doesn't work so well
 - *~dogs -dog*

Relevance feedback: Basic idea

- The user issues a (short, simple) query.
- The search engine returns a set of documents.
- User marks some docs as relevant, some as non-relevant.
- Search engine computes a new representation of the information need. Hope: better than the initial query.
- Search engine runs new query and returns new results.
- New results have (hopefully) better recall.
- We can iterate this: several rounds of relevance feedback.
- We will use the term **ad hoc retrieval** to refer to regular retrieval without relevance feedback.

Relevance feedback: Examples













- We will now look at three different examples of relevance feedback that highlight different aspects of the process.

Relevance Feedback: Example 1















Results for initial query

[Browse](#)
[Search](#)
[Prev](#)
[Next](#)
[Random](#)













| | | | | | |
|---|---|---|---|--|---|
|  |  |  |  |  |  |
| (144473, 16458) | (144457, 252140) | (144456, 262857) | (144456, 262863) | (144457, 252134) | (144483, 265154) |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
|  |  |  |  |  |  |
| (144483, 264644) | (144483, 265153) | (144518, 257752) | (144538, 525937) | (144456, 249611) | (144456, 250064) |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |

User feedback: Select what is relevant

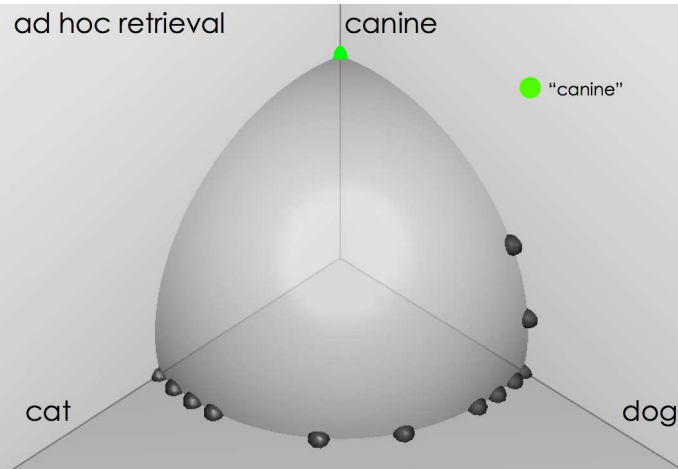
[Browse](#)
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| | | | | | |
|---|---|---|---|--|---|
|  |  |  |  |  |  |
| (144473, 16458) | (144457, 252140) | (144456, 262857) | (144456, 262863) | (144457, 252134) | (144483, 265154) |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
|  |  |  |  |  |  |
| (144483, 264644) | (144483, 265153) | (144518, 257752) | (144538, 525937) | (144456, 249611) | (144456, 250064) |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |

Results after relevance feedback

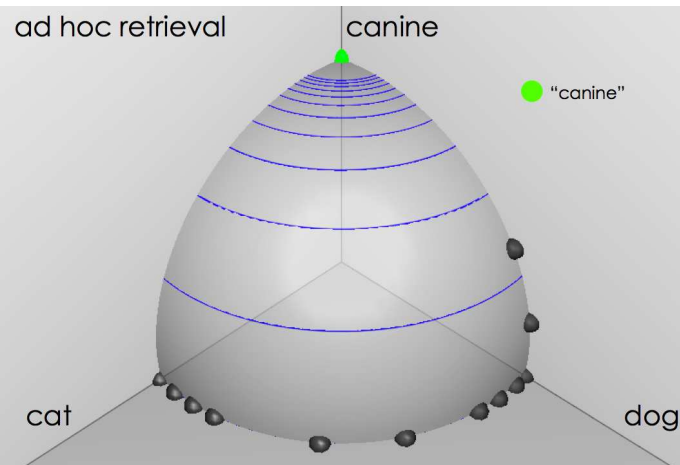
| Browse Search Prev Next Random | | | | | |
|--|---|---|---|--|---|
|  |  |  |  |  |  |
| (144538, 523493) 0.54182 0.231944 0.309876 | (144538, 523835) 0.56319296 0.267304 0.295889 | (144538, 523529) 0.584279 0.280881 0.303398 | (144456, 253569) 0.64501 0.351395 0.293615 | (144456, 253568) 0.650275 0.411745 0.23853 | (144538, 523799) 0.66709197 0.358033 0.309059 |
|  |  |  |  |  |  |
| (144473, 16249) 0.6721 0.393922 0.278178 | (144456, 249634) 0.675018 0.4659 0.211118 | (144456, 253693) 0.676901 0.47645 0.200451 | (144473, 16328) 0.700339 0.309002 0.391337 | (144483, 265264) 0.70170796 0.36176 0.339948 | (144478, 512410) 0.70297 0.469111 0.233859 |

Vector space example: query “canine” (1)



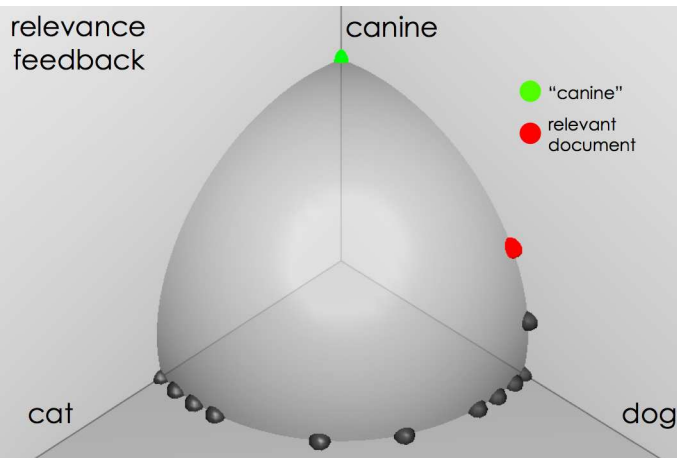
source:
Fernando Díaz

Similarity of docs to query "canine"



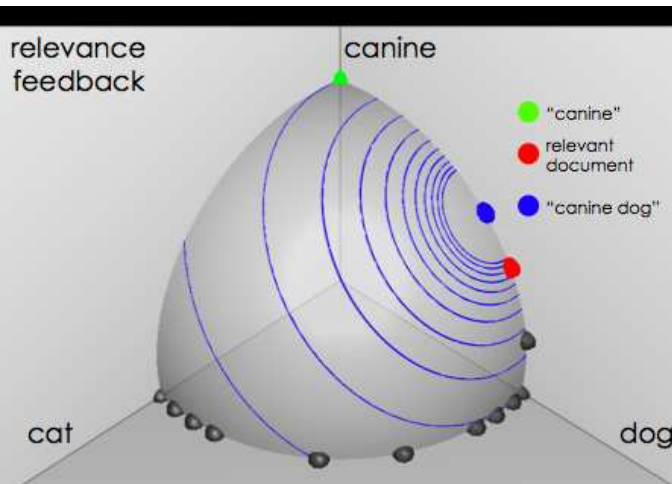
source:
Fernando Díaz

User feedback: Select relevant documents



source:
Fernando Díaz

Results after relevance feedback



source:
Fernando Díaz

Example 3: A real (non-image) example

Initial query: [new space satellite applications]

Results for initial query: (r = rank)

| | r | | |
|---|-----|-------|--|
| + | 1 | 0.539 | NASA Hasn't Scrapped Imaging Spectrometer |
| + | 2 | 0.533 | NASA Scratches Environment Gear From Satellite Plan |
| | 3 | 0.528 | Science Panel Backs NASA Satellite Plan, But Urges Launches of Smaller Probes |
| | 4 | 0.526 | A NASA Satellite Project Accomplishes Incredible Feat: Staying Within Budget |
| | 5 | 0.525 | Scientist Who Exposed Global Warming Proposes Satellites for Climate Research |
| | 6 | 0.524 | Report Provides Support for the Critics Of Using Big Satellites to Study Climate |
| | 7 | 0.516 | Arianespace Receives Satellite Launch Pact From Telesat Canada |
| + | 8 | 0.509 | Telecommunications Tale of Two Companies |

User then marks relevant documents with “+”.

Expanded query after relevance feedback

| | | | |
|--------|------------|--------|-------------|
| 2.074 | new | 15.106 | space |
| 30.816 | satellite | 5.660 | application |
| 5.991 | nasa | 5.196 | eos |
| 4.196 | launch | 3.972 | aster |
| 3.516 | instrument | 3.446 | arianespace |
| 3.004 | bundespost | 2.806 | ss |
| 2.790 | rocket | 2.053 | scientist |
| 2.003 | broadcast | 1.172 | earth |
| 0.836 | oil | 0.646 | measure |

Compare to original query: [new space satellite applications]

Results for expanded query (old ranks in parens)

| | r | | |
|---|-------|-------|--|
| * | 1 (2) | 0.513 | NASA Scratches Environment Gear From Satellite Plan |
| * | 2 (1) | 0.500 | NASA Hasn't Scrapped Imaging Spectrometer |
| | 3 | 0.493 | When the Pentagon Launches a Secret Satellite, Space Sleuths Do Some Spy Work of Their Own |
| | 4 | 0.493 | NASA Uses 'Warm' Superconductors For Fast Circuit |
| * | 5 (8) | 0.492 | Telecommunications Tale of Two Companies |
| | 6 | 0.491 | Soviets May Adapt Parts of SS-20 Missile For Commercial Use |
| | 7 | 0.490 | Gaping Gap: Pentagon Lags in Race To Match the Soviets In Rocket Launchers |
| | 8 | 0.490 | Rescue of Satellite By Space Agency To Cost \$90 Million |

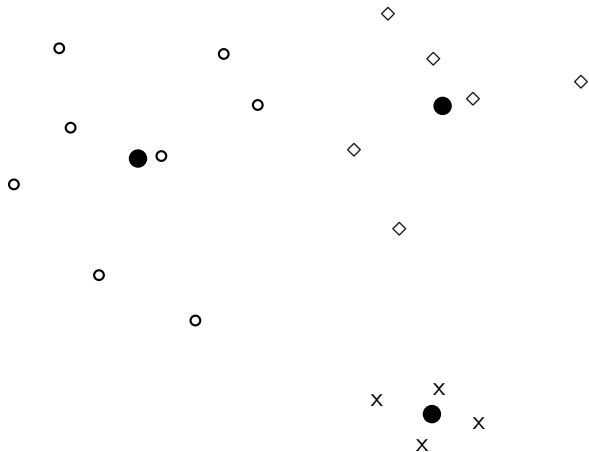
Key concept for relevance feedback: Centroid

- The centroid is the center of mass of a set of points.
- Recall that we represent documents as points in a high-dimensional space.
- Thus: we can compute centroids of documents.
- Definition:

$$\vec{\mu}(D) = \frac{1}{|D|} \sum_{d \in D} \vec{v}(d)$$

where D is a set of documents and $\vec{v}(d) = \vec{d}$ is the vector we use to represent document d .

Centroid: Examples



Rocchio algorithm

- The Rocchio algorithm implements relevance feedback in the vector space model.
- Rocchio chooses the query \vec{q}_{opt} that maximizes

$$\vec{q}_{opt} = \arg \max_{\vec{q}} [\text{sim}(\vec{q}, \mu(D_r)) - \text{sim}(\vec{q}, \mu(D_{nr}))]$$

D_r : set of relevant docs; D_{nr} : set of nonrelevant docs

- Intent: \vec{q}_{opt} is the vector that separates relevant and non-relevant docs maximally.
- Making some additional assumptions, we can rewrite \vec{q}_{opt} as:

$$\vec{q}_{opt} = \mu(D_r) + [\mu(D_r) - \mu(D_{nr})]$$

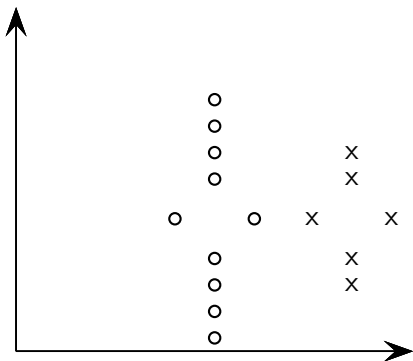
Rocchio algorithm

- The optimal query vector is:

$$\begin{aligned}\vec{q}_{opt} &= \mu(D_r) + [\mu(D_r) - \mu(D_{nr})] \\ &= \frac{1}{|D_r|} \sum_{\vec{d}_j \in D_r} \vec{d}_j + \left[\frac{1}{|D_r|} \sum_{\vec{d}_j \in D_r} \vec{d}_j - \frac{1}{|D_{nr}|} \sum_{\vec{d}_j \in D_{nr}} \vec{d}_j \right]\end{aligned}$$

- We move the centroid of the relevant documents by the difference between the two centroids.

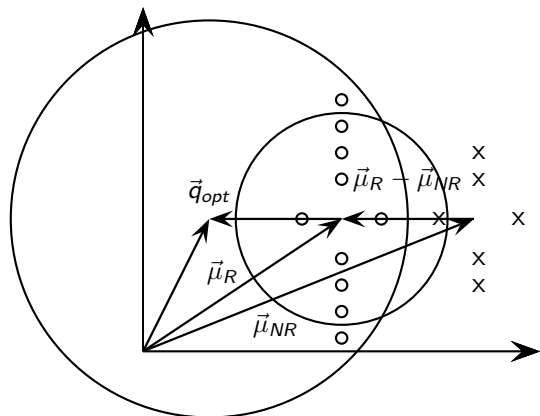
Exercise: Compute Rocchio vector



circles: relevant documents, Xs: nonrelevant documents

compute: $\vec{q}_{opt} = \mu(D_r) + [\mu(D_r) - \mu(D_{nr})]$

Rocchio illustrated



circles: relevant documents, Xs: non-relevant documents $\vec{\mu}_R$:
 centroid of relevant documents $\vec{\mu}_R$ does not separate
 relevant/non-relevant. $\vec{\mu}_{NR}$: centroid of non-relevant documents
 $\vec{\mu}_R - \vec{\mu}_{NR}$: difference vector Add difference vector to $\vec{\mu}_R$ to
 get \vec{q}_{opt} \vec{q}_{opt} separates relevant/non-relevant perfectly.

Terminology

- So far, we have used the name Rocchio for the theoretically better motivated original version of Rocchio.
- The implementation that is actually used in most cases is the SMART implementation – this SMART version of Rocchio is what we will refer to from now on.

Rocchio 1971 algorithm (SMART)

- Used in practice:

$$\begin{aligned}\vec{q}_m &= \alpha \vec{q}_0 + \beta \mu(D_r) - \gamma \mu(D_{nr}) \\ &= \alpha \vec{q}_0 + \beta \frac{1}{|D_r|} \sum_{\vec{d}_j \in D_r} \vec{d}_j - \gamma \frac{1}{|D_{nr}|} \sum_{\vec{d}_j \in D_{nr}} \vec{d}_j\end{aligned}$$

q_m : modified query vector; q_0 : original query vector; D_r and D_{nr} : sets of known relevant and non-relevant documents respectively; α , β , and γ : weights

- New query moves towards relevant documents and away from non-relevant documents.
- Tradeoff α vs. β/γ : If we have a lot of judged documents, we want a higher β/γ .
- **Set negative term weights to 0.**
- “Negative weight” for a term doesn’t make sense in the vector space model.

Positive vs. negative relevance feedback

- Positive feedback is more valuable than negative feedback.
- For example, set $\beta = 0.75$, $\gamma = 0.25$ to give higher weight to positive feedback.
- Many systems only allow positive feedback.

Relevance feedback: Assumptions

- When can relevance feedback enhance recall?
- Assumption A1: The user knows the terms in the collection well enough for an initial query.
- Assumption A2: Relevant documents contain similar terms (so I can “hop” from one relevant document to a different one when giving relevance feedback).

Violation of A1

- Assumption A1: The user knows the terms in the collection well enough for an initial query.
- Violation: Mismatch of searcher's vocabulary and collection vocabulary
- Example: cosmonaut / astronaut

Violation of A2

- Assumption A2: Relevant documents are similar.
- Example for violation: [contradictory government policies]
- Several unrelated “prototypes”
 - Subsidies for tobacco farmers vs. anti-smoking campaigns
 - Aid for developing countries vs. high tariffs on imports from developing countries
- Relevance feedback on tobacco docs will not help with finding docs on developing countries.

Relevance feedback: Assumptions

- When can relevance feedback enhance recall?
- Assumption A1: The user knows the terms in the collection well enough for an initial query.
- Assumption A2: Relevant documents contain similar terms (so I can “hop” from one relevant document to a different one when giving relevance feedback).

Relevance feedback: Evaluation

- Pick an evaluation measure, e.g., precision in top 10: $P@10$
- Compute $P@10$ for original query q_0
- Compute $P@10$ for modified relevance feedback query q_1
- In most cases: q_1 is spectacularly better than q_0 !
- Is this a fair evaluation?

Relevance feedback: Evaluation

- Fair evaluation must be on “residual” collection: docs not yet judged by user.
- Studies have shown that relevance feedback is successful when evaluated this way.
- Empirically, one round of relevance feedback is often very useful. Two rounds are marginally useful.

Evaluation: Caveat

- True evaluation of usefulness must compare to other methods taking **the same amount of time**.
- Alternative to relevance feedback: User revises and resubmits query.
- Users may prefer revision/resubmission to having to judge relevance of documents.
- There is no clear evidence that relevance feedback is the “best use” of the user’s time.

Exercise

- Do search engines use relevance feedback?
- Why?

Relevance feedback: Problems

- Relevance feedback is expensive.
 - Relevance feedback creates long modified queries.
 - Long queries are expensive to process.
- Users are reluctant to provide explicit feedback.
- It's often hard to understand why a particular document was retrieved after applying relevance feedback.
- The search engine Excite had full relevance feedback at one point, but abandoned it later.

Pseudo-relevance feedback

- Pseudo-relevance feedback automates the “manual” part of true relevance feedback.
- Pseudo-relevance feedback algorithm:
 - Retrieve a ranked list of hits for the user’s query
 - Assume that the top k documents are relevant.
 - Do relevance feedback (e.g., Rocchio)
- Works very well on average
- But can go horribly wrong for some queries.
 - Because of query drift
 - If you do several iterations of pseudo-relevance feedback, then you will get query drift for a large proportion of queries.

Pseudo-relevance feedback at TREC4

- Cornell SMART system
- Results show number of relevant documents out of top 100 for 50 queries (so total number of documents is 5000):

| method | number of relevant documents |
|--------------|------------------------------|
| Inc.ltc | 3210 |
| Inc.ltc-PsRF | 3634 |
| Lnu.ltu | 3709 |
| Lnu.ltu-PsRF | 4350 |

- Results contrast two length normalization schemes (L vs. l) and pseudo-relevance feedback (PsRF).
- The pseudo-relevance feedback method used added only 20 terms to the query. (Rocchio will add many more.)
- This demonstrates that pseudo-relevance feedback is effective on average.

Query expansion: Example

YAHOO! SEARCH

[Web](#) | [Images](#) | [Video](#) | [Audio](#) | [Directory](#) | [Local](#) | [News](#) | [Shopping](#) | [More »](#)

[Answers](#) | [My Web](#) | [Search Services](#) | [Advanced Search](#) | [Preferences](#)

Search Results 1 - 10 of about 160,000,000 for [palm](#) - 0.07 sec. ([About this page](#))

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Types of user feedback

- User gives feedback on **documents**.
 - More common in relevance feedback
- User gives feedback on **words** or **phrases**.
 - More common in query expansion

Query expansion

- Query expansion is another method for **increasing recall**.
- We use “global query expansion” to refer to “global methods for query reformulation”.
- In global query expansion, the query is modified based on some global resource, i.e. a resource that is not query-dependent.
- Main information we use: (near-)synonymy

“Global” resources used for query expansion

- A publication or database that collects (near-)synonyms is called a [thesaurus](#).
- Manual thesaurus (maintained by editors, e.g., PubMed)
- Automatically derived thesaurus (e.g., based on co-occurrence statistics)
- Query-equivalence based on query log mining (common on the web as in the “palm” example)

Thesaurus-based query expansion

- For each term t in the query, expand the query with words the thesaurus lists as semantically related with t .
- Example from earlier: HOSPITAL \rightarrow MEDICAL
- Generally increases recall
- May significantly decrease precision, particularly with ambiguous terms
 - INTEREST RATE \rightarrow INTEREST RATE FASCINATE
- Widely used in specialized search engines for science and engineering
- It's very expensive to create a manual thesaurus and to maintain it over time.

Example for manual thesaurus: PubMed

The screenshot displays the PubMed search interface. At the top left is the NCBI logo. In the center is the PubMed logo. On the right is the National Library of Medicine (NLM) logo. Below the logos is a navigation bar with tabs for PubMed, Nucleotide, Protein, Genome, Structure, PopSet, and Taxonomy. The search bar contains the text "Search PubMed" followed by a dropdown menu set to "PubMed" and the word "for cancer". To the right of the search bar are "Go" and "Clear" buttons. Below the search bar are links for "Limits", "Preview/Index", "History", "Clipboard", and "Details". On the left side, there is a vertical menu with links for "About Entrez", "Text Version", "Entrez PubMed", "Overview", "Help | FAQ", "Tutorial", "New/Noteworthy", "E-Utilities", "PubMed Services", "Journals Database", "MeSH Browser", and "Single Citation". The main content area shows the "PubMed Query:" section with a text box containing the query: `("neoplasms"[MeSH Terms] OR cancer[Text Word])`. Below the text box are "Search" and "URL" buttons.

Automatic thesaurus generation

- Attempt to generate a thesaurus automatically by analyzing the distribution of words in documents
- Fundamental notion: similarity between two words
- Definition 1: Two words are **similar if they co-occur with similar words**.
 - “car” \approx “motorcycle” because both occur with “road”, “gas” and “license”, so they must be similar.
- Definition 2: Two words are **similar if they occur in a given grammatical relation with the same words**.
 - You can harvest, peel, eat, prepare, etc., apples and pears, so apples and pears must be similar.
- Co-occurrence is more robust, grammatical relations are more accurate.

Co-occurrence-based thesaurus: Examples

| Word | Nearest neighbors |
|-------------|--|
| absolutely | absurd whatsoever totally exactly nothing |
| bottomed | dip copper drops topped slide trimmed |
| captivating | shimmer stunningly superbly plucky witty |
| doghouse | dog porch crawling beside downstairs |
| makeup | repellent lotion glossy sunscreen skin gel |
| mediating | reconciliation negotiate case conciliation |
| keeping | hoping bring wiping could some would |
| lithographs | drawings Picasso Dali sculptures Gauguin |
| pathogens | toxins bacteria organisms bacterial parasite |
| senses | grasp psyche truly clumsy naive innate |

WordSpace demo on web

Soft cosine measure

- Use a matrix \mathbf{S} that specifies the cosine similarity of basis vectors (i.e. of words) in Salton's vector space model.
- Definition 3: The similarity of two words is proportional to their cosine similarity.
 - “car” \approx “motorcycle” iff $\cos(\text{“car”}, \text{“motorcycle”}) \approx 1$.
- When the search engine supports non-orthogonal vector space model, then we can directly compute the soft cosine measure (SCM) between document vectors \vec{u} and \vec{v} by computing the matrix product $\vec{u}^T \mathbf{S} \vec{v}$.
- Otherwise, we can expand the text query as follows:
 - 1 Translate the text query to a query vector \vec{u} .
 - 2 Compute $\vec{u}' = \vec{u} \mathbf{S}$.
 - 3 Translate \vec{u}' back to a (now expanded) text query.
- Unlike a thesaurus based on word co-occurrences, the matrix \mathbf{S} can be derived from word embeddings, the Levenshtein distance, and other measures of word similarity / relatedness.

SCM query expansion: Example

Query expansion using a Gramm matrix \mathbf{S} that was built from the Google News word embeddings distributed with Word2Vec:

Original query : “**I did enact Julius Caesar: I was killed i' the Capitol**”

Expanded query : “Give_onto_Caesar Brutus_Cassius choreographers_Bosco
Julius_Caesar therefore_onto_Caesar Marcus_Antonius
Caesarion Gallic_Wars Marcus_Crassus Antoninus Catiline
Seleucus Gaius_Julius_Caesar Theodoric Marcus_Tullius_Cicero

⋮

Kenneth Philip Marcus Arthur Carl Fred Edward Jonathan
Eric Frank Anthony William Richard Robert **enact Capitol
killed** I didn't honestly myself I I my we **the 'd 'm did was**”

We can include only highly similar words in the expanded query. Search engines such as Apache Lucene make it possible to assign weights to words in text queries.

Query expansion at search engines

- Main source of query expansion at search engines: query logs
- Example 1: After issuing the query [herbs], users frequently search for [herbal remedies].
 - → “herbal remedies” is potential expansion of “herb”.
- Example 2: Users searching for [flower pix] frequently click on the URL photobucket.com/flower. Users searching for [flower clipart] frequently click on the [same URL](#).
 - → “flower clipart” and “flower pix” are potential expansions of each other.

Take-away today

- **Interactive relevance feedback:** improve initial retrieval results by telling the IR system which docs are relevant / non-relevant
- Best known relevance feedback method: **Rocchio feedback**
- **Query expansion:** improve retrieval results by adding synonyms / related terms to the query
 - **Sources for related terms:** Manual thesauri, automatic thesauri, query logs

Resources

- Chapter 9 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - Daniel Tunkelang's articles on query understanding, namely on query relaxation and query expansion.
 - Salton and Buckley 1990 (original relevance feedback paper)
 - Spink, Jansen, Ozmultu 2000: Relevance feedback at Excite
 - Justin Bieber: related searches fail
 - Word Space
 - Schütze 1998: Automatic word sense discrimination (describes a simple method for automatic thesaurus generation)
 - Sidorov et al. 2014: Soft similarity and soft cosine measure: Similarity of features in vector space model
 - Charlet and Damnati 2017: SimBow at SemEval-2017 Task 3: Soft-Cosine Semantic Similarity between Questions for Community Question Answering (describes two matrices **S**)

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 13: Text Classification & Naive Bayes Handout version

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2024-04-25

(compiled on 2024-04-24 10:06:55)

Overview

- 1 Text classification
- 2 Naive Bayes
- 3 NB theory
- 4 Evaluation of TC

Take-away today

- Text classification: definition & relevance to information retrieval
- Naive Bayes: simple baseline text classifier
- Theory: derivation of Naive Bayes classification rule & analysis
- Evaluation of text classification: how do we know it worked / didn't work?

A text classification task: Email spam filtering

From: '' <takworlld@hotmail.com>

Subject: real estate is the only way... gem oalvgkay

Anyone can buy real estate with no money down

Stop paying rent TODAY !

There is no need to spend hundreds or even thousands for similar courses

I am 22 years old and I have already purchased 6 properties using the methods outlined in this truly INCREDIBLE ebook.

Change your life NOW !

=====
Click Below to order:

<http://www.wholesaledaily.com/sales/nmd.htm>

=====
How would you write a program that would automatically detect and delete this type of message?

Formal definition of TC: Training

Given:

- A **document space** \mathbb{X}
 - Documents are represented in this space – typically some type of high-dimensional space.
- A fixed set of **classes** $\mathbb{C} = \{c_1, c_2, \dots, c_J\}$
 - The classes are human-defined for the needs of an application (e.g., spam vs. nonspam).
- A **training set** \mathbb{D} of labeled documents. Each labeled document $\langle d, c \rangle \in \mathbb{X} \times \mathbb{C}$

Using a learning method or **learning algorithm**, we then wish to learn a **classifier** γ that maps documents to classes:

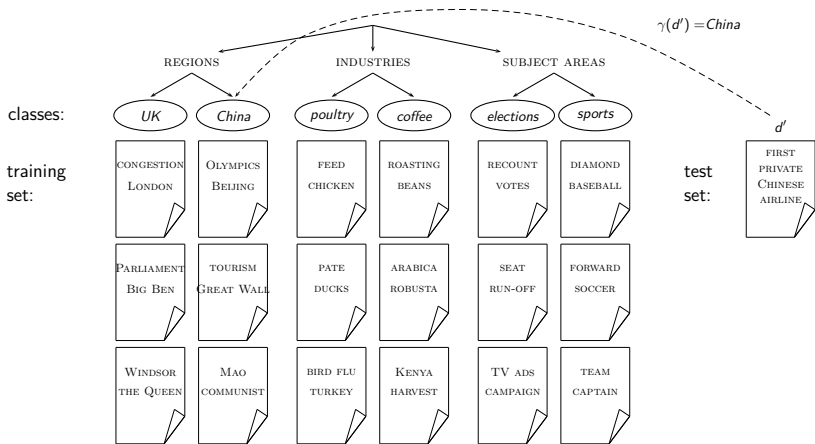
$$\gamma : \mathbb{X} \rightarrow \mathbb{C}$$

Formal definition of TC: Application/Testing

Given: a description $d \in \mathbb{X}$ of a document

Determine: $\gamma(d) \in \mathbb{C}$, that is, the class that is most appropriate for d

Topic classification



Exercise

- Find examples of uses of text classification in information retrieval

Examples of how search engines use classification

- Language identification (classes: English vs. French, etc.)
- The automatic detection of spam pages (spam vs. nonspam)
- Sentiment detection: is a movie or product review positive or negative (positive vs. negative)
- Topic-specific or *vertical* search – restrict search to a “vertical” like “related to health” (relevant to vertical vs. not)

Classification methods: 1. Manual

- Manual classification was used by Yahoo in the beginning of the web. Also: MathSciNet (MSC), DMOZ – the Open Directory Project, PubMed
- Very accurate if job is done by experts.
- Consistent when the problem size and team is small.
- Scaling manual classification is difficult and expensive.
- → We need automatic methods for classification.

Classification methods: 2. Rule-based

- E.g., Google Alerts is rule-based classification.
- There are IDE-type development environments for writing very complex rules efficiently. (e.g., Verity)
- Often: Boolean combinations (as in Google Alerts).
- Accuracy is very high if a rule has been carefully refined over time by a subject expert.
- Building and maintaining rule-based classification systems is cumbersome and expensive.

A Verity topic (a complex classification rule)

```

comment line      # Beginning of art topic definition
top-level topic  art ACCRUE
                 /author = "fsmith"
topic definition modifiers } /date = "30-Dec-01"
                           /annotation = "Topic created
                             by fsmith"
subtopic topic   * 0.70 performing-arts ACCRUE
evidencetopic   ** 0.50 WORD
topic definition modifier /wordtext = ballet
evidencetopic   ** 0.50 STEM
topic definition modifier /wordtext = dance
evidencetopic   ** 0.50 WORD
topic definition modifier /wordtext = opera
evidencetopic   ** 0.30 WORD
topic definition modifier /wordtext = symphony
subtopic        * 0.70 visual-arts ACCRUE
                 ** 0.50 WORD
                 /wordtext = painting
                 ** 0.50 WORD
                 /wordtext = sculpture
subtopic        * 0.70 film ACCRUE
                 ** 0.50 STEM
                 /wordtext = film
subtopic        ** 0.50 motion-picture PHRASE
                 *** 1.00 WORD
                 /wordtext = motion
                 *** 1.00 WORD
                 /wordtext = picture

```

Classification methods: 3. Statistical/Probabilistic

- This was our definition of the classification problem – text classification as a learning problem.
- (i) Supervised learning of the classification function γ and (ii) application of γ to classifying new documents.
- We will look at two methods for doing this: Naive Bayes and SVMs
- No free lunch: requires hand-classified training data.
- But this manual classification can be done by non-experts.

The Naive Bayes classifier

- The Naive Bayes classifier is a probabilistic classifier.
- We compute the probability of a document d being in a class c as follows:

$$P(c|d) \propto P(c) \prod_{1 \leq k \leq n_d} P(t_k|c)$$

- n_d is the length of the document. (number of tokens)
- $P(t_k|c)$ is the conditional probability of term t_k occurring in a document of class c
- $P(t_k|c)$ as a measure of **how much evidence** t_k contributes that c is the correct class.
- $P(c)$ is the prior probability of c .
- If a document's terms do not provide clear evidence for one class vs. another, we choose the c with highest $P(c)$.

Maximum a posteriori class

- Our goal in Naive Bayes classification is to find the “best” class.
- The best class is the most likely or **maximum a posteriori (MAP) class** c_{map} :

$$c_{\text{map}} = \arg \max_{c \in \mathbb{C}} \hat{P}(c|d) = \arg \max_{c \in \mathbb{C}} \hat{P}(c) \prod_{1 \leq k \leq n_d} \hat{P}(t_k|c)$$

- We write \hat{P} for P since these values are **estimates** from the training set.

Taking the log

- Multiplying lots of small probabilities can result in floating point underflow.
- Since $\log(xy) = \log(x) + \log(y)$, we can sum log probabilities instead of multiplying probabilities.
- Since log is a monotonic function, the class with the highest score does not change.
- So what we usually compute in practice is:

$$c_{\text{map}} = \arg \max_{c \in \mathbb{C}} [\log \hat{P}(c) + \sum_{1 \leq k \leq n_d} \log \hat{P}(t_k | c)]$$

Naive Bayes classifier

- Classification rule:

$$c_{\text{map}} = \arg \max_{c \in \mathbb{C}} [\log \hat{P}(c) + \sum_{1 \leq k \leq n_d} \log \hat{P}(t_k | c)]$$

- Simple interpretation:

- Each conditional parameter $\log \hat{P}(t_k | c)$ is a weight that indicates how good an indicator t_k is for c .
- The prior $\log \hat{P}(c)$ is a weight that indicates the relative frequency of c .
- The sum of log prior and term weights is then a measure of how much evidence there is for the document being in the class.
- We select the class with the most evidence.

Parameter estimation take 1: Maximum likelihood

- Estimate parameters $\hat{P}(c)$ and $\hat{P}(t_k|c)$ from train data: How?
- Prior:

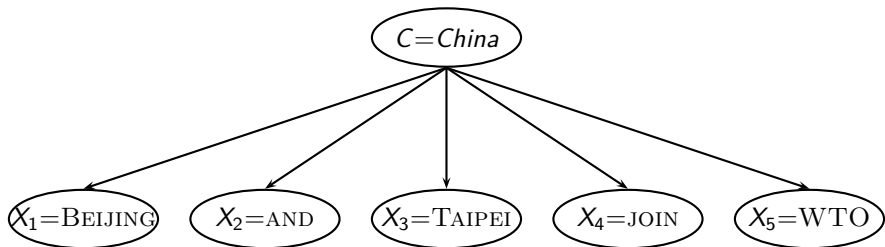
$$\hat{P}(c) = \frac{N_c}{N}$$

- N_c : number of docs in class c ; N : total number of docs
- Conditional probabilities:

$$\hat{P}(t|c) = \frac{T_{ct}}{\sum_{t' \in V} T_{ct'}}$$

- T_{ct} is the number of tokens of t in training documents from class c (includes multiple occurrences)
- We have made a **Naive Bayes independence assumption** here:
 $\hat{P}(X_{k_1} = t|c) = \hat{P}(X_{k_2} = t|c)$, independent of position

The problem with maximum likelihood estimates: Zeros



$$P(\text{China}|d) \propto P(\text{China}) \cdot P(\text{BEIJING}|\text{China}) \cdot P(\text{AND}|\text{China}) \\ \cdot P(\text{TAIPEI}|\text{China}) \cdot P(\text{JOIN}|\text{China}) \cdot P(\text{WTO}|\text{China})$$

- If WTO never occurs in class China in the train set:

$$\hat{P}(\text{WTO}|\text{China}) = \frac{T_{\text{China},\text{WTO}}}{\sum_{t' \in V} T_{\text{China},t'}} = \frac{0}{\sum_{t' \in V} T_{\text{China},t'}} = 0$$

The problem with maximum likelihood estimates: Zeros (cont)

- If there are no occurrences of *WTO* in documents in class *China*, we get a zero estimate:

$$\hat{P}(\text{WTO}|\text{China}) = \frac{T_{\text{China},\text{WTO}}}{\sum_{t' \in V} T_{\text{China},t'}} = 0$$

- \rightarrow We will get $P(\text{China}|d) = 0$ for any document that contains *WTO*

To avoid zeros: Add-one smoothing

- Before:

$$\hat{P}(t|c) = \frac{T_{ct}}{\sum_{t' \in V} T_{ct'}}$$

- Now: Add one to each count to avoid zeros:

$$\hat{P}(t|c) = \frac{T_{ct} + 1}{\sum_{t' \in V} (T_{ct'} + 1)} = \frac{T_{ct} + 1}{(\sum_{t' \in V} T_{ct'}) + B}$$

- B is the number of bins – in this case the number of different words or the size of the vocabulary $|V| = M$

Naive Bayes: Summary

- Estimate parameters from the training corpus using add-one smoothing
- For a new document, for each class, compute sum of (i) log of prior and (ii) logs of conditional probabilities of the terms
- Assign the document to the class with the largest score

Naive Bayes: Training

TRAINMULTINOMIALNB(\mathbb{C}, \mathbb{D})

```
1   $V \leftarrow \text{EXTRACTVOCABULARY}(\mathbb{D})$ 
2   $N \leftarrow \text{COUNTDOCS}(\mathbb{D})$ 
3  for each  $c \in \mathbb{C}$ 
4  do  $N_c \leftarrow \text{COUNTDOCSINCLASS}(\mathbb{D}, c)$ 
5      $\text{prior}[c] \leftarrow N_c/N$ 
6      $\text{text}_c \leftarrow \text{CONCATENATETEXTOFALLDOCSINCLASS}(\mathbb{D}, c)$ 
7     for each  $t \in V$ 
8     do  $T_{ct} \leftarrow \text{COUNTTOKENSOFTERM}(\text{text}_c, t)$ 
9     for each  $t \in V$ 
10    do  $\text{condprob}[t][c] \leftarrow \frac{T_{ct}+1}{\sum_{t'} (T_{ct'}+1)}$ 
11  return  $V, \text{prior}, \text{condprob}$ 
```


Naive Bayes: Testing

```
APPLYMULTINOMIALNB( $\mathbb{C}$ ,  $V$ , prior, condprob,  $d$ )
1   $W \leftarrow \text{EXTRACTTOKENSFROMDOC}(V, d)$ 
2  for each  $c \in \mathbb{C}$ 
3  do  $\text{score}[c] \leftarrow \log \text{prior}[c]$ 
4    for each  $t \in W$ 
5    do  $\text{score}[c] + = \log \text{condprob}[t][c]$ 
6  return  $\arg \max_{c \in \mathbb{C}} \text{score}[c]$ 
```

Exercise

| | docID | words in document | in $c = \textit{China}$? |
|--------------|-------|-------------------------------------|---------------------------|
| training set | 1 | Chinese Beijing Chinese | yes |
| | 2 | Chinese Chinese Shanghai | yes |
| | 3 | Chinese Macao | yes |
| | 4 | Tokyo Japan Chinese | no |
| test set | 5 | Chinese Chinese Chinese Tokyo Japan | ? |

- Estimate parameters of Naive Bayes classifier
- Classify test document

Example: Parameter estimates

Priors: $\hat{P}(c) = 3/4$ and $\hat{P}(\bar{c}) = 1/4$

Conditional probabilities:

$$\hat{P}(\text{CHINESE}|c) = (5 + 1)/(8 + 6) = 6/14 = 3/7$$

$$\hat{P}(\text{TOKYO}|c) = \hat{P}(\text{JAPAN}|c) = (0 + 1)/(8 + 6) = 1/14$$

$$\hat{P}(\text{CHINESE}|\bar{c}) = (1 + 1)/(3 + 6) = 2/9$$

$$\hat{P}(\text{TOKYO}|\bar{c}) = \hat{P}(\text{JAPAN}|\bar{c}) = (1 + 1)/(3 + 6) = 2/9$$

The denominators are $(8 + 6)$ and $(3 + 6)$ because the lengths of text_c and $\text{text}_{\bar{c}}$ are 8 and 3, respectively, and because the constant B is 6 as the vocabulary consists of six terms.

Example: Classification

$$\hat{P}(c|d_5) \propto 3/4 \cdot (3/7)^3 \cdot 1/14 \cdot 1/14 \approx 0.0003$$

$$\hat{P}(\bar{c}|d_5) \propto 1/4 \cdot (2/9)^3 \cdot 2/9 \cdot 2/9 \approx 0.0001$$

Thus, the classifier assigns the test document to $c = \textit{China}$. The reason for this classification decision is that the three occurrences of the positive indicator `CHINESE` in d_5 outweigh the occurrences of the two negative indicators `JAPAN` and `TOKYO`.

Time complexity of Naive Bayes

| mode | time complexity |
|----------|---|
| training | $\Theta(\mathbb{D} L_{ave} + \mathbb{C} V)$ |
| testing | $\Theta(L_a + \mathbb{C} M_a) = \Theta(\mathbb{C} M_a)$ |

- L_{ave} : average length of a training doc, L_a : length of the test doc, M_a : number of distinct terms in the test doc, \mathbb{D} : training set, V : vocabulary, \mathbb{C} : set of classes
- $\Theta(|\mathbb{D}|L_{ave})$ is the time it takes to compute all counts.
- $\Theta(|\mathbb{C}||V|)$ is the time it takes to compute the parameters from the counts.
- Generally: $|\mathbb{C}||V| < |\mathbb{D}|L_{ave}$
- Test time is also linear (in the length of the test document).
- Thus: **Naive Bayes is linear** in the size of the training set (training) and the test document (testing). This is **optimal**.

Naive Bayes: Analysis

- Now we want to gain a better understanding of the properties of Naive Bayes.
- We will formally derive the classification rule ...
- ... and make our assumptions explicit.

Derivation of Naive Bayes rule

We want to find the class that is most likely given the document:

$$c_{\text{map}} = \arg \max_{c \in \mathbb{C}} P(c|d)$$

Apply Bayes rule $P(A|B) = \frac{P(B|A)P(A)}{P(B)}$:

$$c_{\text{map}} = \arg \max_{c \in \mathbb{C}} \frac{P(d|c)P(c)}{P(d)}$$

Drop denominator since $P(d)$ is the same for all classes:

$$c_{\text{map}} = \arg \max_{c \in \mathbb{C}} P(d|c)P(c)$$

Too many parameters / sparseness

$$\begin{aligned}c_{\text{map}} &= \arg \max_{c \in \mathbb{C}} P(d|c)P(c) \\ &= \arg \max_{c \in \mathbb{C}} P(\langle t_1, \dots, t_k, \dots, t_{n_d} \rangle | c)P(c)\end{aligned}$$

- There are too many parameters $P(\langle t_1, \dots, t_k, \dots, t_{n_d} \rangle | c)$, one for each unique combination of a class and a sequence of words.
- We would need a very, very large number of training examples to estimate that many parameters.
- This is the problem of **data sparseness**.

Naive Bayes conditional independence assumption

To reduce the number of parameters to a manageable size, we make the **Naive Bayes conditional independence assumption**:

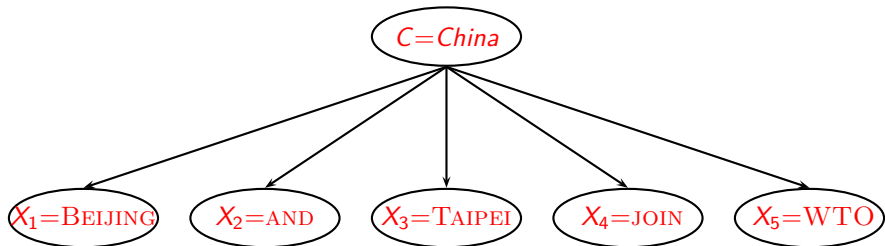
$$P(d|c) = P(\langle t_1, \dots, t_{n_d} \rangle | c) = \prod_{1 \leq k \leq n_d} P(X_k = t_k | c)$$

We assume that the probability of observing the conjunction of attributes is equal to the product of the individual probabilities $P(X_k = t_k | c)$.

Recall from earlier the estimates for these conditional probabilities:

$$\hat{P}(t|c) = \frac{T_{ct} + 1}{(\sum_{t' \in V} T_{ct'}) + B}$$

Generative model



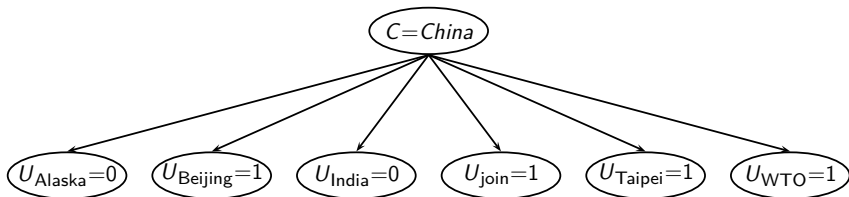
$$P(c|d) \propto P(c) \prod_{1 \leq k \leq n_d} P(t_k|c)$$

- Generate a class with probability $P(c)$
- Generate each of the words (in their respective positions), conditional on the class, but independent of each other, with probability $P(t_k|c)$
- To classify docs, we “reengineer” this process and find the class that is most likely to have generated the doc.

Second independence assumption

- $\hat{P}(X_{k_1} = t|c) = \hat{P}(X_{k_2} = t|c)$
- For example, for a document in the class *UK*, the probability of generating QUEEN in the first position of the document is the same as generating it in the last position.
- The two independence assumptions amount to the **bag of words** model.

A different Naive Bayes model: Bernoulli model



Violation of Naive Bayes independence assumptions

- Conditional independence:

$$P(\langle t_1, \dots, t_{n_d} \rangle | c) = \prod_{1 \leq k \leq n_d} P(X_k = t_k | c)$$

- Positional independence:
- $\hat{P}(X_{k_1} = t | c) = \hat{P}(X_{k_2} = t | c)$
- The independence assumptions do not really hold of documents written in natural language.
- Exercise
 - Examples for why conditional independence assumption is not really true?
 - Examples for why positional independence assumption is not really true?
- How can Naive Bayes work if it makes such inappropriate assumptions?

Why does Naive Bayes work?

- Naive Bayes can work well even though conditional independence assumptions are **badly** violated.
- Example:

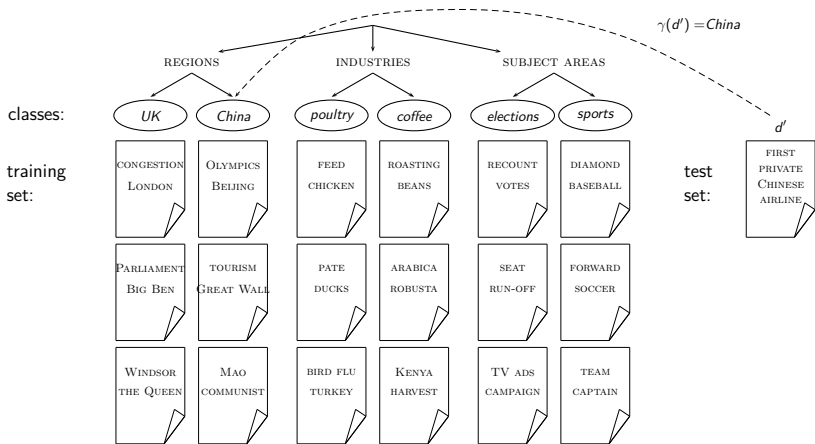
| | c_1 | c_2 | class selected |
|---|---------|---------|----------------|
| true probability $P(c d)$ | 0.6 | 0.4 | c_1 |
| $\hat{P}(c) \prod_{1 \leq k \leq n_d} \hat{P}(t_k c)$ | 0.00099 | 0.00001 | |
| NB estimate $\hat{P}(c d)$ | 0.99 | 0.01 | c_1 |

- Double counting of evidence causes underestimation (0.01) and overestimation (0.99).
- Classification is about predicting the correct class and **not** about accurately estimating probabilities.
- Naive Bayes is terrible for correct estimation ...
- ... but it often performs well at accurate prediction (choosing the correct class).

Naive Bayes is not so naive

- Naive Bayes has won some bakeoffs (e.g., KDD-CUP 97)
- More robust to irrelevant features than some more complex learning methods
- More robust to concept drift (changing of definition of class over time) than some more complex learning methods
- Better than methods like decision trees when we have **many equally important features**
- A good dependable baseline for text classification (but not the best)
- Optimal if independence assumptions hold (never true for text, but true for some domains)
- Very fast
- Low storage requirements

Evaluation on Reuters



Example: The Reuters collection

| symbol | statistic | value |
|--------|---------------------------------|---------|
| N | documents | 800,000 |
| L | avg. # word tokens per document | 200 |
| M | word types | 400,000 |

| type of class | number | examples |
|---------------|--------|-------------------|
| region | 366 | UK, China |
| industry | 870 | poultry, coffee |
| subject area | 126 | elections, sports |

A Reuters document



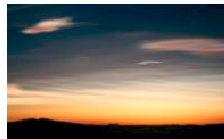
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Extreme conditions create rare Antarctic clouds

Tue Aug 1, 2006 3:20am ET

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SYDNEY (Reuters) - Rare, mother-of-pearl colored clouds caused by extreme weather conditions above Antarctica are a possible indication of global warming, Australian scientists said on Tuesday.

Known as nacreous clouds, the spectacular formations showing delicate wisps of colors were photographed in the sky over an Australian

[\[-\] Text \[+\]](#)

Evaluating classification

- Evaluation must be done on test data that are independent of the training data, i.e., training and test sets are disjoint.
- It's easy to get good performance on a test set that was available to the learner during training (e.g., just memorize the test set).
- Measures: Precision, recall, F_1 , classification accuracy
- Average measures over multiple training and test sets (splits of the overall data) for best results.

Precision P and recall R

| | in the class | not in the class |
|----------------------------------|----------------------|----------------------|
| predicted to be in the class | true positives (TP) | false positives (FP) |
| predicted to not be in the class | false negatives (FN) | true negatives (TN) |

TP, FP, FN, TN are counts of documents. The sum of these four counts is the total number of documents.

$$\text{precision: } P = TP / (TP + FP)$$

$$\text{recall: } R = TP / (TP + FN)$$

A combined measure: F

- F_1 allows us to trade off precision against recall.



$$F_1 = \frac{1}{\frac{1}{2} \frac{1}{P} + \frac{1}{2} \frac{1}{R}} = \frac{2PR}{P + R}$$

- This is the **harmonic mean** of P and R : $\frac{1}{F} = \frac{1}{2} \left(\frac{1}{P} + \frac{1}{R} \right)$

Averaging: Micro vs. Macro

- We now have an evaluation measure (F_1) for **one class**.
- But we also want a single number that measures the **aggregate performance** over all classes in the collection.
- **Macroaveraging**
 - Compute F_1 for each of the C classes
 - Average these C numbers
- **Microaveraging**
 - Compute TP, FP, FN for each of the C classes
 - Sum these C numbers (e.g., all TP to get aggregate TP)
 - Compute F_1 for aggregate TP, FP, FN

Naive Bayes vs. other methods

| (a) | NB | Rocchio | kNN | SVM | |
|--------------------------|----|---------|-----|-----|--|
| micro-avg-L (90 classes) | 80 | 85 | 86 | 89 | |
| macro-avg (90 classes) | 47 | 59 | 60 | 60 | |

| (b) | NB | Rocchio | kNN | trees | SVM |
|---------------------------|----|---------|-----|-------|-----|
| earn | 96 | 93 | 97 | 98 | 98 |
| acq | 88 | 65 | 92 | 90 | 94 |
| money-fx | 57 | 47 | 78 | 66 | 75 |
| grain | 79 | 68 | 82 | 85 | 95 |
| crude | 80 | 70 | 86 | 85 | 89 |
| trade | 64 | 65 | 77 | 73 | 76 |
| interest | 65 | 63 | 74 | 67 | 78 |
| ship | 85 | 49 | 79 | 74 | 86 |
| wheat | 70 | 69 | 77 | 93 | 92 |
| corn | 65 | 48 | 78 | 92 | 90 |
| micro-avg (top 10) | 82 | 65 | 82 | 88 | 92 |
| micro-avg-D (118 classes) | 75 | 62 | n/a | n/a | 87 |

Evaluation measure: F_1

Naive Bayes does pretty well, but some methods beat it consistently (e.g., SVM).

Take-away today

- Text classification: definition & relevance to information retrieval
- Naive Bayes: simple baseline text classifier
- Theory: derivation of Naive Bayes classification rule & analysis
- Evaluation of text classification: how do we know it worked / didn't work?

Resources

- Chapter 13 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - Weka: A data mining software package that includes an implementation of Naive Bayes
 - Reuters-21578 – text classification evaluation set
 - Vulgarity classifier fail

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 14: Vector Space Classification Handout version

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Overview

- 1 Intro vector space classification
- 2 Rocchio
- 3 kNN
- 4 Linear classifiers
- 5 > two classes

Take-away today

- **Vector space classification:** Basic idea of doing text classification for documents that are represented as vectors
- **Rocchio classifier:** Rocchio relevance feedback idea applied to text classification
- k nearest neighbor classification
- Linear classifiers
- More than two classes

Roadmap for today

- Naive Bayes is simple and a good baseline.
- Use it if you want to get a text classifier up and running in a hurry.
- But other classification methods are more accurate.
- Perhaps the simplest well performing alternative: kNN
- kNN is a vector space classifier.
- Plan for rest of today
 - 1 intro vector space classification
 - 2 very simple vector space classification: Rocchio
 - 3 kNN
 - 4 general properties of classifiers

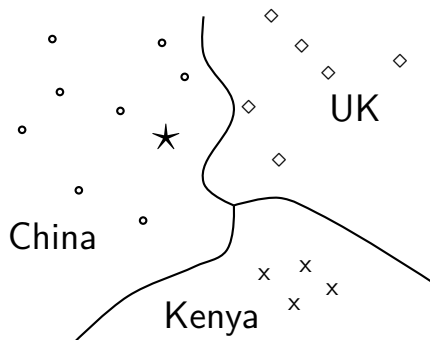
Recall vector space representation

- Each document is a vector, one component for each term.
- Terms are axes.
- High dimensionality: 100,000s of dimensions
- Normalize vectors (documents) to unit length
- How can we do classification in this space?

Vector space classification

- As before, the training set is a set of documents, each labeled with its class.
- In vector space classification, this set corresponds to a labeled set of points or vectors in the vector space.
- Premise 1: Documents in the same class form a **contiguous region**.
- Premise 2: Documents from different classes **don't overlap**.
- We define lines, surfaces, hyper-surfaces to divide regions.

Classes in the vector space



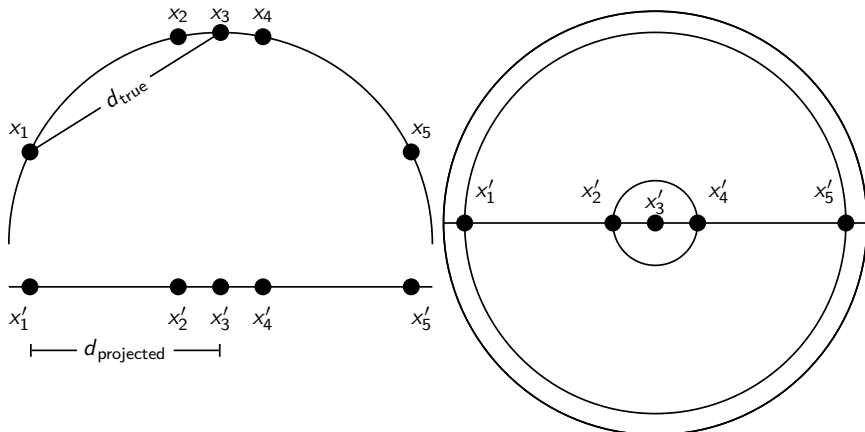
Should the document \star be assigned to *China*, *UK* or *Kenya*?

Find separators between the classes

Based on these separators: \star should be assigned to *China*

How do we find separators that do a good job at classifying new documents like \star ? – Main topic of today

Aside: 2D/3D graphs can be misleading



Left: A projection of the 2D semicircle to 1D. For the points x_1, x_2, x_3, x_4, x_5 at x coordinates $-0.9, -0.2, 0, 0.2, 0.9$ the distance $|x_2x_3| \approx 0.201$ only differs by 0.5% from $|x'_2x'_3| = 0.2$; but $|x_1x_3|/|x'_1x'_3| = d_{\text{true}}/d_{\text{projected}} \approx 1.06/0.9 \approx 1.18$ is an example of a large distortion (18%) when projecting a large area. *Right:* The corresponding projection of the 3D hemisphere to 2D.

Relevance feedback

- In relevance feedback, the user marks documents as relevant/non-relevant.
- Relevant/non-relevant can be viewed as [classes](#) or [categories](#).
- For each document, the user decides which of these two classes is correct.
- The IR system then uses these class assignments to build a better query (“model”) of the information need . . .
- . . . and returns better documents.
- Relevance feedback is a form of [text classification](#).
- The notion of text classification (TC) is very general and has many applications within and beyond information retrieval.

Using Rocchio for vector space classification

- The principal difference between relevance feedback and text classification:
 - The training set is given as part of the input in text classification.
 - It is interactively created in relevance feedback.

Rocchio classification: Basic idea

- Compute a centroid for each class
 - The centroid is the average of all documents in the class.
- Assign each test document to the class of its closest centroid.

Recall definition of centroid

$$\vec{\mu}(c) = \frac{1}{|D_c|} \sum_{d \in D_c} \vec{v}(d)$$

where D_c is the set of all documents that belong to class c and $\vec{v}(d)$ is the vector space representation of d .

Rocchio algorithm

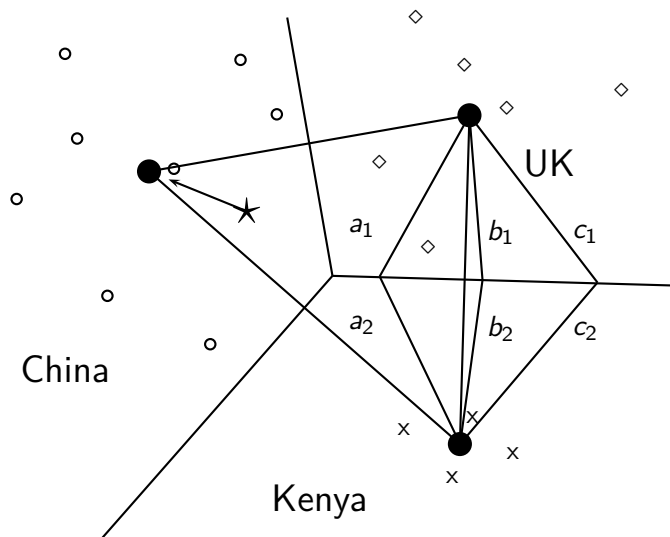
TRAINROCCHIO(\mathbb{C}, \mathbb{D})

- 1 **for each** $c_j \in \mathbb{C}$
- 2 **do** $D_j \leftarrow \{d : \langle d, c_j \rangle \in \mathbb{D}\}$
- 3 $\vec{\mu}_j \leftarrow \frac{1}{|D_j|} \sum_{d \in D_j} \vec{v}(d)$
- 4 **return** $\{\vec{\mu}_1, \dots, \vec{\mu}_J\}$

APPLYROCCHIO($\{\vec{\mu}_1, \dots, \vec{\mu}_J\}, d$)

- 1 **return** $\arg \min_j |\vec{\mu}_j - \vec{v}(d)|$

Rocchio illustrated: $a_1 = a_2, b_1 = b_2, c_1 = c_2$



Rocchio properties

- Rocchio forms a simple representation for each class: the **centroid**
 - We can interpret the centroid as the **prototype** of the class.
- Classification is based on similarity to / distance from centroid/prototype.
- Does not guarantee that classifications are consistent with the training data!

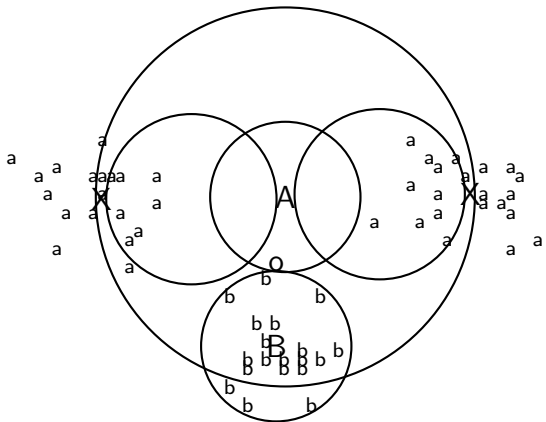
Time complexity of Rocchio

| mode | time complexity |
|----------|---|
| training | $\Theta(\mathbb{D} L_{\text{ave}} + \mathbb{C} V) \approx \Theta(\mathbb{D} L_{\text{ave}})$ |
| testing | $\Theta(L_a + \mathbb{C} M_a) \approx \Theta(\mathbb{C} M_a)$ |

Rocchio vs. Naive Bayes

- In many cases, Rocchio performs worse than Naive Bayes.
- One reason: Rocchio does not handle nonconvex, multimodal classes correctly.

Rocchio cannot handle nonconvex, multimodal classes



Exercise: Why is Rocchio not expected to do well for the classification task a vs. b here?

- A is centroid of the a's, B is centroid of the b's.
- The point o is closer to A than to B.
- But o is a better fit for the b class.
- A is a multimodal class with two prototypes.
- But in Rocchio we only have one prototype.

kNN classification

- kNN classification is another vector space classification method.
- It also is very simple and easy to implement.
- kNN is more accurate (in most cases) than Naive Bayes and Rocchio.
- If you need to get a pretty accurate classifier up and running in a short time ...
- ...and you don't care about efficiency that much ...
- ...use kNN.

kNN classification

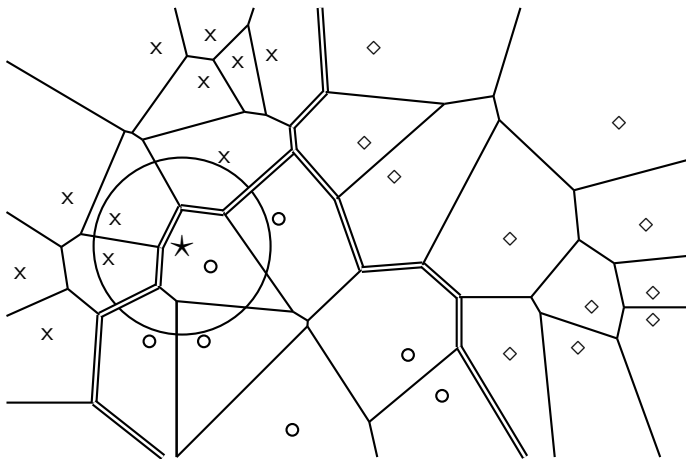
- kNN = k nearest neighbors
- kNN classification rule for $k = 1$ (1NN): Assign each test document to the class of its nearest neighbor in the training set.
- 1NN is not very robust – one document can be mislabeled or atypical.
- kNN classification rule for $k > 1$ (kNN): Assign each test document to the majority class of its k nearest neighbors in the training set.
- Rationale of kNN: contiguity hypothesis
 - We expect a test document d to have the same label as the training documents located in the local region surrounding d .

Probabilistic kNN

- Probabilistic version of kNN: $P(c|d)$ = fraction of k neighbors of d that are in c
- **kNN classification rule for probabilistic kNN:** Assign d to class c with highest $P(c|d)$

kNN is based on Voronoi tessellation

1NN, 3NN
classification
decision for
star?



kNN algorithm

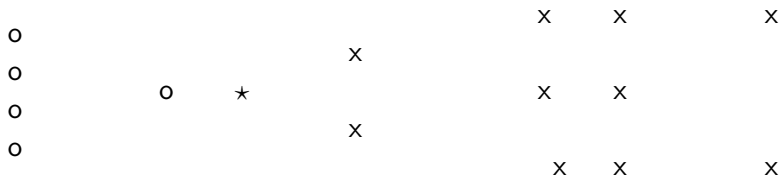
TRAIN-KNN(\mathbb{C}, \mathbb{D})

- 1 $\mathbb{D}' \leftarrow \text{PREPROCESS}(\mathbb{D})$
- 2 $k \leftarrow \text{SELECT-K}(\mathbb{C}, \mathbb{D}')$
- 3 **return** \mathbb{D}', k

APPLY-KNN(\mathbb{D}', k, d)

- 1 $S_k \leftarrow \text{COMPUTENEARESTNEIGHBORS}(\mathbb{D}', k, d)$
- 2 **for each** $c_j \in \mathbb{C}(\mathbb{D}')$
- 3 **do** $p_j \leftarrow |S_k \cap c_j|/k$
- 4 **return** $\arg \max_j p_j$

Exercise



How is star classified by:

(i) 1-NN (ii) 3-NN (iii) 9-NN (iv) 15-NN (v) Rocchio?

Time complexity of kNN

kNN with preprocessing of training set

training $\Theta(|\mathbb{D}|L_{\text{ave}})$

testing $\Theta(L_a + |\mathbb{D}|M_{\text{ave}}M_a) = \Theta(|\mathbb{D}|M_{\text{ave}}M_a)$

- kNN test time proportional to the size of the training set!
- The larger the training set, the longer it takes to classify a test document.
- kNN is inefficient for very large training sets.
- Question: Can we divide up the training set into regions, so that we only have to search in one region to do kNN classification for a given test document? (which perhaps would give us better than linear time complexity)

Curse of dimensionality

- Our intuitions about space are based on the 3D world we live in.
- Intuition 1: some things are close by, some things are distant.
- Intuition 2: we can carve up space into areas such that: within an area things are close, distances between areas are large.
- These two intuitions don't necessarily hold for high dimensions.
- In particular: for a set of k uniformly distributed points, let d_{\min} be the smallest distance between any two points and d_{\max} be the largest distance between any two points.
- Then

$$\lim_{d \rightarrow \infty} \frac{d_{\max} - d_{\min}}{d_{\min}} = 0$$

Curse of dimensionality: Simulation

- Simulate

$$\lim_{d \rightarrow \infty} \frac{d_{\max} - d_{\min}}{d_{\min}} = 0$$

- Pick a dimensionality d
- Generate 10 random points in the d -dimensional hypercube (uniform distribution)
- Compute all 45 distances
- Compute $\frac{d_{\max} - d_{\min}}{d_{\min}}$
- We see that intuition 1 (some things are close, others are distant) is not true for high dimensions.

Intuition 2: Space can be carved up

- Intuition 2: we can carve up space into areas such that: within an area things are close, distances between areas are large.
- If this is true, then we have a simple and efficient algorithm for kNN.
- To find the k closest neighbors of data point $\langle x_1, x_2, \dots, x_d \rangle$ do the following.
- Using binary search find all data points whose first dimension is in $[x_1 - \epsilon, x_1 + \epsilon]$. This is $O(\log n)$ where n is the number of data points.
- Do this for each dimension, then intersect the d subsets.

Intuition 2: Space can be carved up

- Size of data set $n = 100$
- Again, assume uniform distribution in hypercube
- Set $\epsilon = 0.05$: we will look in an interval of length 0.1 for neighbors on each dimension.
- What is the probability that the nearest neighbor of a new data point \vec{x} is in this neighborhood in $d = 1$ dimension?
- for $d = 1$: $1 - (1 - 0.1)^{100} \approx 0.99997$
- In $d = 2$ dimensions?
- for $d = 2$: $1 - (1 - 0.1^2)^{100} \approx 0.63$
- In $d = 3$ dimensions?
- for $d = 3$: $1 - (1 - 0.1^3)^{100} \approx 0.095$
- In $d = 4$ dimensions?
- for $d = 4$: $1 - (1 - 0.1^4)^{100} \approx 0.0095$
- In $d = 5$ dimensions?
- for $d = 5$: $1 - (1 - 0.1^5)^{100} \approx 0.0009995$

Intuition 2: Space can be carved up

- In $d = 5$ dimensions?
- for $d = 5$: $1 - (1 - 0.1^5)^{100} \approx 0.0009995$
- In other words: with enough dimensions, there is only one “local” region that will contain the nearest neighbor with high certainty: the entire search space.
- We cannot carve up high-dimensional space into neat neighborhoods . . .
- . . . unless the “true” dimensionality is much lower than d .

kNN: Discussion

- No training necessary
 - But linear preprocessing of documents is as expensive as training Naive Bayes.
 - We always preprocess the training set, so in reality training time of kNN is linear.
- kNN is very accurate if training set is large.
- Optimality result: asymptotically zero error if Bayes rate is zero.
- But kNN can be very inaccurate if training set is small.

Linear classifiers

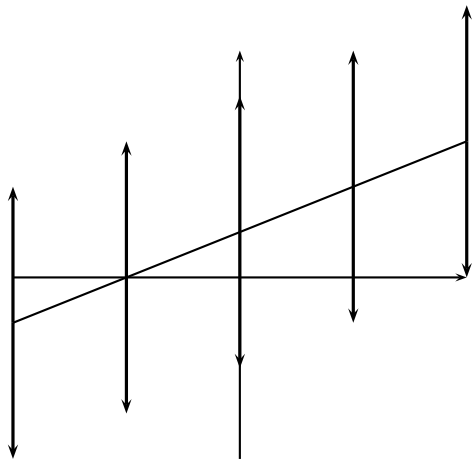
- Definition:
 - A linear classifier computes a linear combination or weighted sum $\sum_i w_i x_i$ of the feature values.
 - Classification decision: $\sum_i w_i x_i > \theta$?
 - ... where θ (the threshold) is a parameter.
- (First, we only consider binary classifiers.)
- Geometrically, this corresponds to a line (2D), a plane (3D) or a hyperplane (higher dimensionalities), the [separator](#).
- We find this separator based on training set.
- Methods for finding separator: Perceptron, Rocchio, Naive Bayes – as we will explain on the next slides
- Assumption: The classes are [linearly separable](#).

A linear classifier in 1D



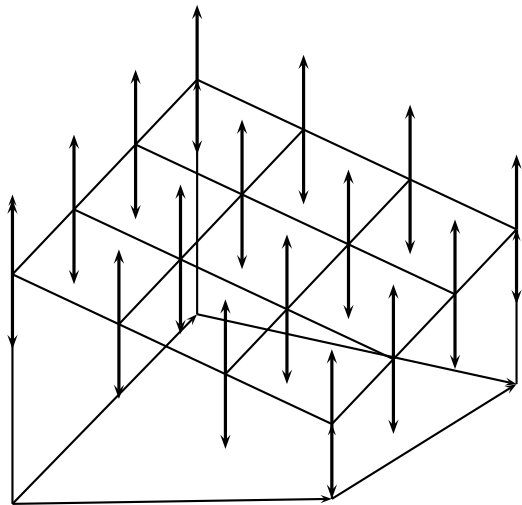
- A linear classifier in 1D is a point described by the equation $w_1 d_1 = \theta$
- The point at θ/w_1
- Points (d_1) with $w_1 d_1 \geq \theta$ are in the class c .
- Points (d_1) with $w_1 d_1 < \theta$ are in the complement class \bar{c} .

A linear classifier in 2D



- A linear classifier in 2D is a line described by the equation $w_1 d_1 + w_2 d_2 = \theta$
- Example for a 2D linear classifier
- Points $(d_1 \ d_2)$ with $w_1 d_1 + w_2 d_2 \geq \theta$ are in the class c .
- Points $(d_1 \ d_2)$ with $w_1 d_1 + w_2 d_2 < \theta$ are in the complement class \bar{c} .

A linear classifier in 3D



- A linear classifier in 3D is a plane described by the equation
$$w_1d_1 + w_2d_2 + w_3d_3 = \theta$$
- Example for a 3D linear classifier
- Points $(d_1 \ d_2 \ d_3)$ with $w_1d_1 + w_2d_2 + w_3d_3 \geq \theta$ are in the class c .
- Points $(d_1 \ d_2 \ d_3)$ with $w_1d_1 + w_2d_2 + w_3d_3 < \theta$ are in the complement class \bar{c} .

Rocchio as a linear classifier

- Rocchio is a linear classifier defined by:

$$\sum_{i=1}^M w_i d_i = \vec{w} \vec{d} = \theta$$

where \vec{w} is the **normal vector** $\vec{\mu}(c_1) - \vec{\mu}(c_2)$ and $\theta = 0.5 * (|\vec{\mu}(c_1)|^2 - |\vec{\mu}(c_2)|^2)$.

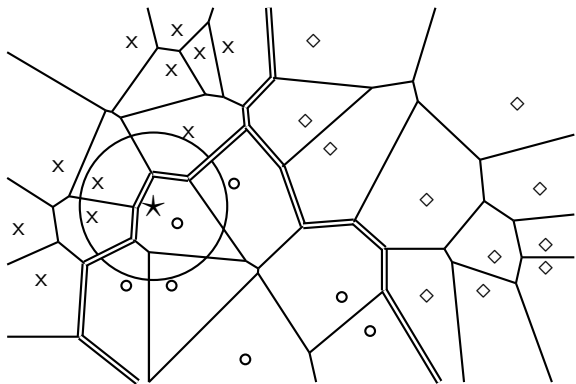
Naive Bayes as a linear classifier

Multinomial Naive Bayes is a linear classifier (in log space) defined by:

$$\sum_{i=1}^M w_i d_i = \theta$$

where $w_i = \log[\hat{P}(t_i|c)/\hat{P}(t_i|\bar{c})]$, $d_i =$ number of occurrences of t_i in d , and $\theta = -\log[\hat{P}(c)/\hat{P}(\bar{c})]$. Here, the index i , $1 \leq i \leq M$, refers to terms of the vocabulary (not to positions in d as k did in our original definition of Naive Bayes)

kNN is not a linear classifier



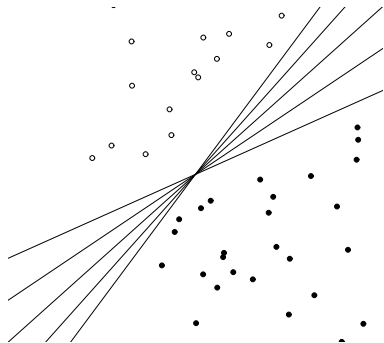
- Classification decision based on majority of k nearest neighbors.
- The decision boundaries between classes are piecewise linear ...
- ... but they are in general not linear classifiers that can be described as
$$\sum_{i=1}^M w_i d_i = \theta.$$

Example of a linear two-class classifier

| t_i | w_i | d_{1i} | d_{2i} | t_i | w_i | d_{1i} | d_{2i} |
|------------|-------|----------|----------|-------|-------|----------|----------|
| prime | 0.70 | 0 | 1 | dhrs | -0.71 | 1 | 1 |
| rate | 0.67 | 1 | 0 | world | -0.35 | 1 | 0 |
| interest | 0.63 | 0 | 0 | sees | -0.33 | 0 | 0 |
| rates | 0.60 | 0 | 0 | year | -0.25 | 0 | 0 |
| discount | 0.46 | 1 | 0 | group | -0.24 | 0 | 0 |
| bundesbank | 0.43 | 0 | 0 | dhr | -0.24 | 0 | 0 |

- This is for the class *interest* in Reuters-21578.
- For simplicity: assume a simple 0/1 vector representation
- d_1 : “rate discount dhrs world”
- d_2 : “prime dhrs”
- $\theta = 0$
- Exercise: Which class is d_1 assigned to? Which class is d_2 assigned to?
- We assign document \vec{d}_1 “rate discount dhrs world” to *interest* since $\vec{w}^T \vec{d}_1 = 0.67 \cdot 1 + 0.46 \cdot 1 + (-0.71) \cdot 1 + (-0.35) \cdot 1 = 0.07 > 0 = \theta$.
- We assign \vec{d}_2 “prime dhrs” to the complement class (not in *interest*) since $\vec{w}^T \vec{d}_2 = -0.01 \leq \theta$.

Which hyperplane?



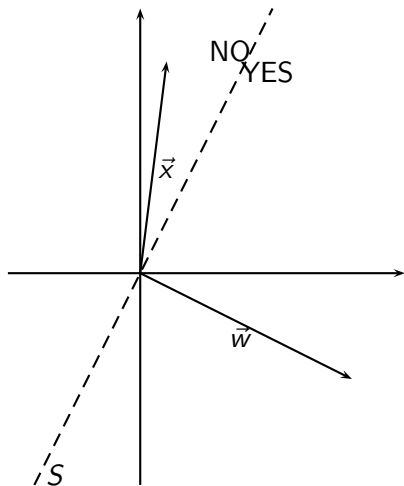
Learning algorithms for vector space classification

- In terms of actual computation, there are two types of learning algorithms.
- (i) **Simple** learning algorithms that estimate the parameters of the classifier directly from the training data, often **in one linear pass**.
 - Naive Bayes, Rocchio, kNN are all examples of this.
- (ii) **Iterative** algorithms
 - Support vector machines
 - Perceptron (example available as PDF on website: <http://cislmu.org>)
- **The best performing learning algorithms usually require iterative learning.**

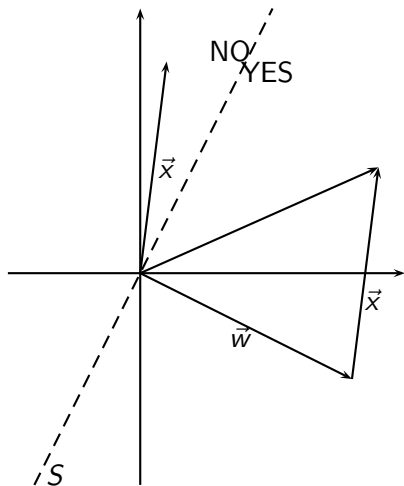
Perceptron update rule

- Randomly initialize linear separator \vec{w}
- Do until convergence:
 - Pick data point \vec{x}
 - If $\text{sign}(\vec{w}^T \vec{x})$ is correct class (1 or -1): do nothing
 - Otherwise: $\vec{w} = \vec{w} - \text{sign}(\vec{w}^T \vec{x})\vec{x}$

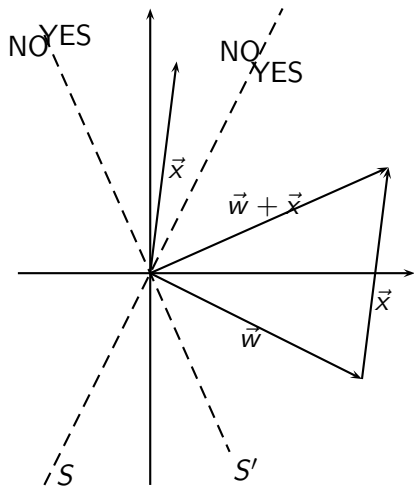
Perceptron



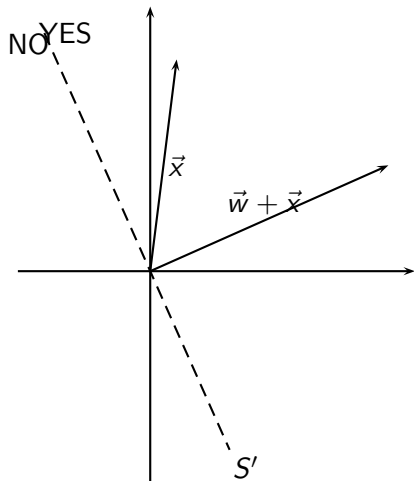
Perceptron



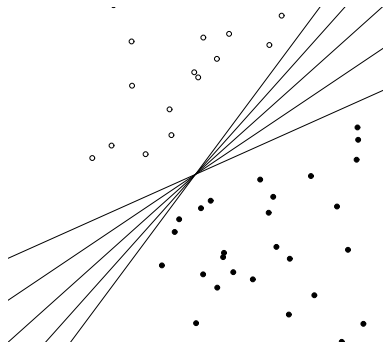
Perceptron



Perceptron



Which hyperplane?



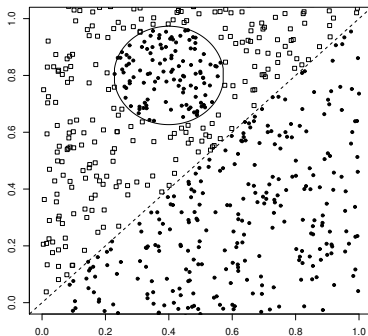
Which hyperplane?

- For linearly separable training sets: there are **infinitely** many separating hyperplanes.
- They all separate the training set perfectly ...
- ... but they behave differently on test data.
- Error rates on new data are low for some, high for others.
- How do we find a low-error separator?
- Perceptron: generally bad; Naive Bayes, Rocchio: ok; linear SVM: good

Linear classifiers: Discussion

- Many common text classifiers are linear classifiers: Naive Bayes, Rocchio, logistic regression, linear support vector machines, etc.
- Each method has a different way of selecting the separating hyperplane
 - Huge differences in performance on test documents
- Can we get better performance with more powerful nonlinear classifiers?
- Not in general: A given amount of training data may suffice for estimating a linear boundary, but not for estimating a more complex nonlinear boundary.

A nonlinear problem

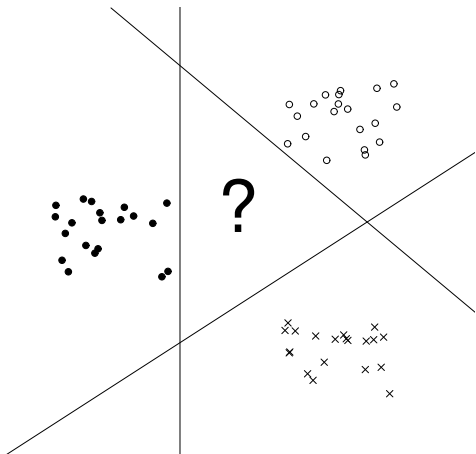


- Linear classifier like Rocchio does badly on this task.
- kNN will do well (assuming enough training data)

Which classifier do I use for a given TC problem?

- Is there a learning method that is optimal for all text classification problems?
- No, because there is a trade-off between bias and variance.
- Factors to take into account:
 - How much training data is available?
 - How simple/complex is the problem? (linear vs. nonlinear decision boundary)
 - How noisy is the problem?
 - How stable is the problem over time?
 - For an unstable problem, it's better to use a simple and robust classifier.

How to combine hyperplanes for > 2 classes?



One-of problems

- One-of or multiclass classification
 - Classes are mutually exclusive.
 - Each document belongs to exactly one class.
 - Example: language of a document (assumption: no document contains multiple languages)

One-of classification with linear classifiers

- Combine two-class linear classifiers as follows for one-of classification:
 - Run each classifier separately
 - Rank classifiers (e.g., according to score)
 - Pick the class with the highest score

Any-of problems

- Any-of or multilabel classification
 - A document can be a member of 0, 1, or many classes.
 - A decision on one class leaves decisions open on all other classes.
 - A type of “independence” (but not statistical independence)
 - Example: topic classification
 - Usually: make decisions on the region, on the subject area, on the industry and so on “independently”

Any-of classification with linear classifiers

- Combine two-class linear classifiers as follows for any-of classification:
 - Simply run each two-class classifier separately on the test document and assign document accordingly

Take-away today

- **Vector space classification:** Basic idea of doing text classification for documents that are represented as vectors
- **Rocchio classifier:** Rocchio relevance feedback idea applied to text classification
- k nearest neighbor classification
- Linear classifiers
- More than two classes

Resources

- Chapter 13 of IIR (feature selection)
- Chapter 14 of IIR
- Resources at <http://cis1mu.org>
 - Perceptron example
 - General overview of text classification: Sebastiani (2002)
 - Text classification chapter on decision trees and perceptrons: Manning & Schütze (1999)
 - One of the best machine learning textbooks: Hastie, Tibshirani & Friedman (2003)

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 15-2: Learning to rank Handout version

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2024-04-24

(compiled on 2024-04-24 10:20:55)

Overview

- 1 Zone scoring
- 2 Machine-learned scoring
- 3 Ranking SVMs

Take-away today

- Basic idea of learning to rank (LTR): We use machine learning to learn the relevance score (retrieval status value) of a document with respect to a query.
- Zone scoring: a particularly simple instance of LTR
- Machine-learned scoring as a general approach to ranking
- Ranking SVMs

Main idea

- The aim of term weights (e.g., tf-idf) is to measure term salience.
 - The sum of term weights is a measure of the relevance of a document to a query and the basis for ranking.
- Now we view this ranking problem as a machine learning problem – we will learn the weighting or, more generally, the ranking.
 - Term weights can be learned using training examples that have been judged.
- This methodology falls under a general class of approaches known as [machine learned relevance](#) or [learning to rank](#).

Learning weights

Main methodology

- Given a set of **training examples**, each of which is a tuple of: a query q , a document d , a relevance judgment for d on q
 - Simplest case: $R(d, q)$ is either relevant (1) or non-relevant (0)
 - More sophisticated cases: graded relevance judgments
- Learn weights from these examples, so that the learned scores approximate the relevance judgments in the training examples

Binary independence model (BIM)

- Is what BIM does a form of learning to rank?
- Recap BIM:
 - Estimate classifier of probability of relevance on training set
 - Apply to all documents
 - Rank documents according to probability of relevance

Learning to rank vs. Text classification

- Both are machine learning approaches
- Text classification, BIM and relevance feedback (if solved by text classification) are **query-specific**.
 - We need a query-specific training set to learn the ranker.
 - We need to learn a new ranker for each query.
- Learning to rank usually refers to **query-independent** ranking.
- We learn a single classifier.
- We can then rank documents for a query that we don't have any relevance judgments for.

Learning to rank: Exercise

- One approach to learning to rank is to represent each query-document pair as a data point, represented as a vector.
- We have two classes.
 - Class 1: the query is relevant to the document.
 - Class 2: the query is not relevant to the document.
- This is a standard classification problem, except that the data points are query-document pairs (as opposed to documents).
- Documents are ranked according to probability of relevance of corresponding document-query pairs.
- What features/dimensions would you use to represent a query-document pair?

Simple form of learning to rank: Zone scoring

- Given: a collection where documents have three **zones** (a.k.a. **fields**): `author`, `title`, `body`
- Weighted zone scoring requires a separate weight for each zone, e.g. g_1 , g_2 , g_3
- Not all zones are equally important:
e.g. `author` < `title` < `body`
→ $g_1 = 0.2$, $g_2 = 0.3$, $g_3 = 0.5$ (so that they add up to 1)
- Score for a zone = 1 if the query term occurs in that zone, 0 otherwise (**Boolean**)

Example

Query term appears in `title` and `body` only

Document score: $(0.3 \cdot 1) + (0.5 \cdot 1) = 0.8$.

General form of weighted zone scoring

Given query q and document d , weighted zone scoring assigns to the pair (q, d) a score in the interval $[0,1]$ by computing a **linear combination** of document zone scores, where each zone contributes a value.

- Consider a set of documents, which have l zones
- Let $g_1, \dots, g_l \in [0, 1]$, such that $\sum_{i=1}^l g_i = 1$
- For $1 \leq i \leq l$, let s_i be the Boolean score denoting a match (or non-match) between q and the i^{th} zone
 - $s_i = 1$ if a query term occurs in zone i , 0 otherwise

Weighted zone score a.k.a **ranked Boolean retrieval**

Rank documents according to $\sum_{i=1}^l g_i s_i$

Learning weights in weighted zone scoring

- Weighted zone scoring may be viewed as **learning a linear function** of the Boolean match scores contributed by the various zones.
- No free lunch: labor-intensive assembly of user-generated relevance judgments from which to learn the weights
 - Especially in a dynamic collection (such as the Web)
 - Major search engine put considerable resources into creating large training sets for learning to rank.
- Good news: once you have a large enough training set, the problem of learning the weights g_i reduces to a simple optimization problem.

Learning weights in weighted zone scoring: Simple case

- Let documents have two zones: title, body
- The weighted zone scoring formula we saw before:

$$\sum_{i=1}^I g_i s_i$$

- Given q, d , $s_T(d, q) = 1$ if a query term occurs in title, 0 otherwise; $s_B(d, q) = 1$ if a query term occurs in body, 0 otherwise
- We compute a score between 0 and 1 for each (d, q) pair using $s_T(d, q)$ and $s_B(d, q)$ by using a constant $g \in [0, 1]$:

$$\text{score}(d, q) = g \cdot s_T(d, q) + (1 - g) \cdot s_B(d, q)$$

Learning weights: determine g from training examples

Example

| Φ_j | d_j | q_j | s_T | s_B | $r(d_j, q_j)$ |
|----------|-------|---------|-------|-------|---------------|
| Φ_1 | 37 | linux | 1 | 1 | Relevant |
| Φ_2 | 37 | penguin | 0 | 1 | Nonrelevant |
| Φ_3 | 238 | system | 0 | 1 | Relevant |
| Φ_4 | 238 | penguin | 0 | 0 | Nonrelevant |
| Φ_5 | 1741 | kernel | 1 | 1 | Relevant |
| Φ_6 | 2094 | driver | 0 | 1 | Relevant |
| Φ_7 | 3194 | driver | 1 | 0 | Nonrelevant |

- Training examples: triples of the form $\Phi_j = (d_j, q_j, r(d_j, q_j))$
- A given training document d_j and a given training query q_j are assessed by a human who decides $r(d_j, q_j)$ (either relevant or nonrelevant)

Learning weights: determine g from training examples

Example

| Example | DocID | Query | s_T | s_B | Judgment |
|----------|-------|---------|-------|-------|-------------|
| Φ_1 | 37 | linux | 1 | 1 | Relevant |
| Φ_2 | 37 | penguin | 0 | 1 | Nonrelevant |
| Φ_3 | 238 | system | 0 | 1 | Relevant |
| Φ_4 | 238 | penguin | 0 | 0 | Nonrelevant |
| Φ_5 | 1741 | kernel | 1 | 1 | Relevant |
| Φ_6 | 2094 | driver | 0 | 1 | Relevant |
| Φ_7 | 3194 | driver | 1 | 0 | Nonrelevant |

- For each training example Φ_j we have Boolean values $s_T(d_j, q_j)$ and $s_B(d_j, q_j)$ that we use to compute a score:

$$\text{score}(d_j, q_j) = g \cdot s_T(d_j, q_j) + (1 - g) \cdot s_B(d_j, q_j)$$

Learning weights

- We compare this score $score(d_j, q_j)$ with the human relevance judgment for the same document-query pair (d_j, q_j) .
- We define the error of the scoring function with weight g as

$$\epsilon(g, \Phi_j) = (r(d_j, q_j) - score(d_j, q_j))^2$$

- Then, the total error of a set of training examples is given by

$$\sum_j \epsilon(g, \Phi_j)$$

- The problem of learning the constant g from the given training examples then reduces to picking the value of g that minimizes the total error.

Minimizing the total error ϵ : Example (1)

Training examples

| Example | DocID | Query | s_T | s_B | Judgment |
|----------|-------|---------|-------|-------|-----------------|
| Φ_1 | 37 | linux | 1 | 1 | 1 (relevant) |
| Φ_2 | 37 | penguin | 0 | 1 | 0 (nonrelevant) |
| Φ_3 | 238 | system | 0 | 1 | 1 (relevant) |
| Φ_4 | 238 | penguin | 0 | 0 | 0 (nonrelevant) |
| Φ_5 | 1741 | kernel | 1 | 1 | 1 (relevant) |
| Φ_6 | 2094 | driver | 0 | 1 | 1 (relevant) |
| Φ_7 | 3194 | driver | 1 | 0 | 0 (nonrelevant) |

- Compute score:

$$\text{score}(d_j, q_j) = g \cdot s_T(d_j, q_j) + (1 - g) \cdot s_B(d_j, q_j)$$
- Compute total error: $\sum_j \epsilon(g, \Phi_j)$, where

$$\epsilon(g, \Phi_j) = (r(d_j, q_j) - \text{score}(d_j, q_j))^2$$
- Pick the value of g that minimizes the total error

Minimizing the total error ϵ : Example (2)

- Compute score $score(d_j, q_j)$

$$score(d_1, q_1) = g \cdot 1 + (1 - g) \cdot 1 = g + 1 - g = 1$$

$$score(d_2, q_2) = g \cdot 0 + (1 - g) \cdot 1 = 0 + 1 - g = 1 - g$$

$$score(d_3, q_3) = g \cdot 0 + (1 - g) \cdot 1 = 0 + 1 - g = 1 - g$$

$$score(d_4, q_4) = g \cdot 0 + (1 - g) \cdot 0 = 0 + 0 = 0$$

$$score(d_5, q_5) = g \cdot 1 + (1 - g) \cdot 1 = g + 1 - g = 1$$

$$score(d_6, q_6) = g \cdot 0 + (1 - g) \cdot 1 = 0 + 1 - g = 1 - g$$

$$score(d_7, q_7) = g \cdot 1 + (1 - g) \cdot 0 = g + 0 = g$$

- Compute total error $\sum_j \epsilon(g, \Phi_j)$

$$(1-1)^2 + (0-1+g)^2 + (1-1+g)^2 + (0-0)^2 + (1-1)^2 + (1-1+g)^2 + (0-g)^2 = 0 + (-1+g)^2 + g^2 + 0 + 0 + g^2 + g^2 = 1 - 2g + 4g^2$$

- Pick the value of g that minimizes the total error

Setting derivative to 0, gives you a minimum of $g = \frac{1}{4}$.

Weight g that minimizes error in the general case



$$g = \frac{n_{10r} + n_{01n}}{n_{10r} + n_{10n} + n_{01r} + n_{01n}}$$

- $n_{...}$ are the counts of rows of the training set table with the corresponding properties:

n_{10r} $s_T = 1$ $s_B = 0$ document relevant

n_{10n} $s_T = 1$ $s_B = 0$ document nonrelevant

n_{01r} $s_T = 0$ $s_B = 1$ document relevant

n_{01n} $s_T = 0$ $s_B = 1$ document nonrelevant

- Derivation: see book
- Note that we ignore documents that have 0 match scores for both zones or 1 match scores for both zones – the value of g does not change their final score.

Exercise: Compute g that minimizes the error

| | DocID | Query | s_T | s_B | Judgment |
|----------|-------|---------|-------|-------|-------------|
| Φ_1 | 37 | linux | 0 | 0 | Relevant |
| Φ_2 | 37 | penguin | 1 | 1 | Nonrelevant |
| Φ_3 | 238 | system | 1 | 0 | Relevant |
| Φ_4 | 238 | penguin | 1 | 1 | Nonrelevant |
| Φ_5 | 238 | redmond | 0 | 1 | Nonrelevant |
| Φ_6 | 1741 | kernel | 0 | 0 | Relevant |
| Φ_7 | 2094 | driver | 1 | 0 | Relevant |
| Φ_8 | 3194 | driver | 0 | 1 | Nonrelevant |
| Φ_9 | 3194 | redmond | 0 | 0 | Nonrelevant |

More general setup of machine learned scoring

- So far, we have considered a case where we combined match scores (Boolean indicators of relevance).
- Now consider more general factors that go beyond Boolean functions of query term presence in document zones.

Two examples of typical features

- The vector space cosine similarity between query and document (denoted α)
- The minimum window width within which the query terms lie (denoted ω)
 - Query term proximity is often indicative of topical relevance.
- Thus, we have one feature that captures overall query-document similarity and one features that captures proximity of query terms in the document.

Learning to rank setup for these two features

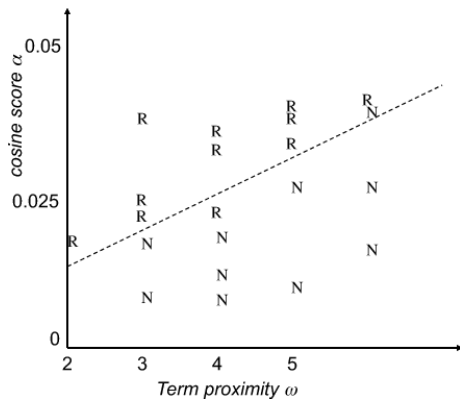
Example

| Example | DocID | Query | α | ω | Judgment |
|----------|-------|------------------|----------|----------|-------------|
| Φ_1 | 37 | linux | 0.032 | 3 | relevant |
| Φ_2 | 37 | penguin | 0.02 | 4 | nonrelevant |
| Φ_3 | 238 | operating system | 0.043 | 2 | relevant |
| Φ_4 | 238 | runtime | 0.004 | 2 | nonrelevant |
| Φ_5 | 1741 | kernel layer | 0.022 | 3 | relevant |
| Φ_6 | 2094 | device driver | 0.03 | 2 | relevant |
| Φ_7 | 3191 | device driver | 0.027 | 5 | nonrelevant |

α is the cosine score. ω is the window width.

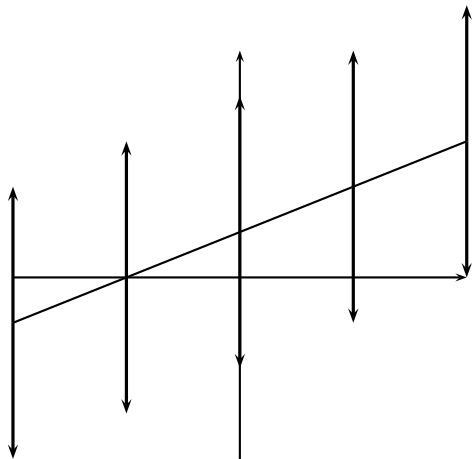
This is exactly the same setup as for zone scoring except we now have more complex features that capture whether a document is relevant to a query.

Graphic representation of the training set



This should look familiar.

In this case: LTR approach learns a linear classifier in 2D



- A linear classifier in 2D is a line described by the equation $w_1 d_1 + w_2 d_2 = \theta$
- Example for a 2D linear classifier
- Points $(d_1 \ d_2)$ with $w_1 d_1 + w_2 d_2 \geq \theta$ are in the class c .
- Points $(d_1 \ d_2)$ with $w_1 d_1 + w_2 d_2 < \theta$ are in the complement class \bar{c} .

Learning to rank setup for two features

- Again, two classes: relevant = 1 and nonrelevant = 0
- We now seek a scoring function that combines the values of the features to generate a value that is (close to) 0 or 1.
- We wish this function to be in agreement with our set of training examples as much as possible.
- A linear classifier is defined by an equation of the form:

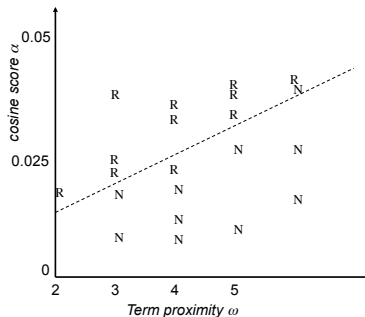
$$\text{Score}(d, q) = \text{Score}(\alpha, \omega) = a\alpha + b\omega + c,$$

where we learn the coefficients a, b, c from training data.

- Regression vs. classification
 - We have only covered binary classification so far.
 - We can also cast the problem as a regression problem.
 - This is what we did for zone scoring just now.

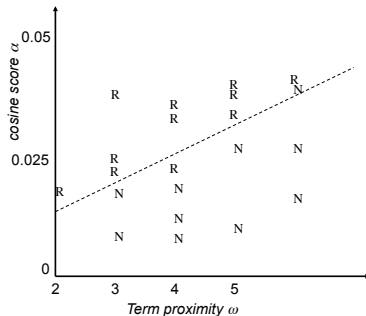
Different geometric interpretation of what's happening

- The function $Score(\alpha, \omega)$ represents a plane “hanging above” the figure.
- Ideally this plane assumes values close to 1 above the points marked R, and values close to 0 above the points marked N.



Linear classification in this case

- We pick a threshold θ .
- If $Score(\alpha, \omega) > \theta$, we declare the document **relevant**, otherwise we declare it **nonrelevant**.
- As before, all points that satisfy $Score(\alpha, \omega) = \theta$ form a line (dashed here) → linear classifier that separates relevant from nonrelevant instances.



Summary

- The problem of making a binary relevant/nonrelevant judgment is cast as a classification or regression problem, based on a training set of query-document pairs and associated relevance judgments.
- In the example: The classifier corresponds to a line $Score(\alpha, \omega) = \theta$ in the α - ω plane.
- In principle, any method learning a linear classifier (including least squares regression) can be used to find this line.
- Big advantage of learning to rank: we can avoid hand-tuning scoring functions and simply learn them from training data.
- Bottleneck of learning to rank: maintaining a representative set of training examples whose relevance assessments must be made by humans.

Learning to rank for more than two features

- The approach can be readily generalized to a large number of features.
- In addition to cosine similarity and query term window, there are lots of other indicators of relevance: PageRank-style measures, document age, zone contributions, document length, etc.
- If these measures can be calculated for a training document collection with relevance judgments, any number of such measures can be used to machine-learn a classifier.

LTR features used by Microsoft Research (1)

- Zones: body, anchor, title, url, whole document
- Features derived from standard IR models: query term number, query term ratio, length, idf, sum of term frequency, min of term frequency, max of term frequency, mean of term frequency, variance of term frequency, sum of length normalized term frequency, min of length normalized term frequency, max of length normalized term frequency, mean of length normalized term frequency, variance of length normalized term frequency, sum of tf-idf, min of tf-idf, max of tf-idf, mean of tf-idf, variance of tf-idf, boolean model, BM25

LTR features used by Microsoft Research (2)

- Language model features: LMIR.ABS, LMIR.DIR, LMIR.JM
- Web-specific features: number of slashes in url, length of url, inlink number, outlink number, PageRank, SiteRank
- Spam features: QualityScore
- Usage-based features: query-url click count, url click count, url dwell time
- See link in resources for more information

Shortcoming of our LTR approach so far

- Approaching IR ranking like we have done so far is not necessarily the right way to think about the problem.
- Statisticians normally first divide problems into **classification** problems (where a categorical variable is predicted) versus **regression** problems (where a real number is predicted).
- In between is the specialized field of **ordinal regression** where a ranking is predicted.
- Machine learning for ad hoc retrieval is most properly thought of as an ordinal regression problem, where the goal is to rank a set of documents for a query, given training data of the same sort.
- Next up: **ranking SVMs**, a machine learning method that learns an ordering directly.

Exercise

Example

| Example | DocID | Query | Cosine | ω | Judgment |
|----------|-------|------------------|--------|----------|-------------|
| Φ_1 | 37 | linux | 0.03 | 3 | relevant |
| Φ_2 | 37 | penguin | 0.04 | 5 | nonrelevant |
| Φ_3 | 238 | operating system | 0.04 | 2 | relevant |
| Φ_4 | 238 | runtime | 0.02 | 3 | nonrelevant |

Give parameters a, b, c of a line $a\alpha + b\omega + c$ that separates relevant from nonrelevant.

Basic setup for ranking SVMs

- As before we begin with a set of judged query-document pairs.
- But we do not represent them as query-document-judgment triples.
- Instead, we ask judges, for each training query q , to **order the documents** that were returned by the search engine with respect to relevance to the query.
- We again construct a vector of features $\psi_j = \psi(d_j, q)$ for each document-query pair – exactly as we did before.
- For two documents d_i and d_j , we then form the vector of feature differences:

$$\Phi(d_i, d_j, q) = \psi(d_i, q) - \psi(d_j, q)$$

Training a ranking SVM

- Vector of feature differences: $\Phi(d_i, d_j, q) = \psi(d_i, q) - \psi(d_j, q)$
- By hypothesis, one of d_i and d_j has been judged more relevant.
- Notation: We write $d_i \prec d_j$ for “ d_i precedes d_j in the results ordering”.
- If d_i is judged more relevant than d_j , then we will assign the vector $\Phi(d_i, d_j, q)$ the class $y_{ijq} = +1$; otherwise -1 .
- This gives us a training set of pairs of vectors and “precedence indicators”. Each of the vectors is computed as the difference of two document-query vectors.
- We can then train an SVM on this training set with the goal of obtaining a classifier that returns

$$\vec{w}^T \Phi(d_i, d_j, q) > 0 \quad \text{iff} \quad d_i \prec d_j$$

Advantages of Ranking SVMs vs. Classification/regression

- Documents can be evaluated **relative** to other candidate documents for the same query, rather than having to be mapped to a **global scale** of goodness.
- This often is an easier problem to solve since just a ranking is required rather than an absolute measure of relevance.
- Especially germane in web search, where the ranking at the very top of the results list is exceedingly important.

Why simple ranking SVMs don't work that well

- Ranking SVMs treat all ranking violations alike.
 - But some violations are minor problems, e.g., getting the order of two relevant documents wrong.
 - Other violations are big problems, e.g., ranking a nonrelevant document ahead of a relevant document.
- Some queries have many relevant documents, others few.
 - Depending on the training regime, too much emphasis may be put on queries with many relevant documents.
- In most IR settings, getting the order of the top documents right is key.
 - In the simple setting we have described, top and bottom ranks will not be treated differently.
- → Learning-to-rank frameworks actually used in IR are more complicated than what we have presented here.

Example for superior performance of LTR

SVM algorithm that directly optimizes MAP (as opposed to ranking).

Proposed by: Yue, Finley, Radlinski, Joachims, ACM SIGIR 2002.
Performance compared to state-of-the-art models: cosine, tf-idf, BM25, language models (Dirichlet and Jelinek-Mercer)

| Model | TREC 9 | | TREC 10 | |
|----------------------|--------|----------|---------|----------|
| | MAP | W/L | MAP | W/L |
| SVM_{map}^{Δ} | 0.242 | – | 0.236 | – |
| Best Func. | 0.204 | 39/11 ** | 0.181 | 37/13 ** |
| 2nd Best | 0.199 | 38/12 ** | 0.174 | 43/7 ** |
| 3rd Best | 0.188 | 34/16 ** | 0.174 | 38/12 ** |

Learning-to-rank clearly better than non-machine-learning approaches

Optimizing scaling/representation of features

- Both of the methods that we've seen treat the features as given and do not attempt to modify the basic representation of the document-query pairs.
- Much of traditional IR weighting involves **nonlinear** scaling of basic measurements (such as log-weighting of term frequency, or idf).
- At the present time, machine learning is very good at producing optimal weights for features in a linear combination, but it is not good at coming up with good nonlinear scalings of basic measurements.
- This area remains the domain of human feature engineering.

Assessment of learning to rank

- The idea of learning to rank is old.
 - Early work by Norbert Fuhr and William S. Cooper
- But it is only very recently that sufficient machine learning knowledge, training document collections, and computational power have come together to make this method practical and exciting.
- While skilled humans can do a very good job at defining ranking functions by hand, hand tuning is difficult, and it has to be done again for each new document collection and class of users.
- The more features are used in ranking, the more difficult it is to manually integrate them into one ranking function.
- Web search engines use a large number of features → web search engines need some form of learning to rank.

Exercise

Write down the training set from the last exercise as a training set for a ranking SVM.

Take-away today

- Basic idea of learning to rank (LTR): We use machine learning to learn the relevance score (retrieval status value) of a document with respect to a query.
- Zone scoring: a particularly simple instance of LTR
- Machine-learned scoring as a general approach to ranking
- Ranking SVMs

Resources

- Chapter 15-2 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - References to ranking SVM results
 - Microsoft learning to rank datasets

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 15-1: Support Vector Machines Handout version

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(compiled on 2024-06-10 08:54:14)

Overview

- 1 SVM intro
- 2 SVM details
- 3 Classification in the real world

Take-away today

- **Support vector machines:** State-of-the-art text classification methods (linear and nonlinear)
- Introduction to SVMs
- Formalization
- Soft margin case for nonseparable problems
- **Discussion:** Which classifier should I use for my problem?

Support vector machines

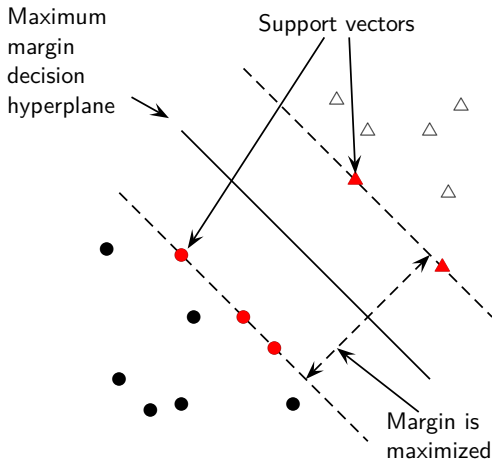
- Machine-learning research in the last two decades has improved classifier effectiveness.
- New generation of state-of-the-art classifiers: support vector machines (SVMs), boosted decision trees, regularized logistic regression, maximum entropy, neural networks, and random forests
- As we saw in IIR: Applications to IR problems, particularly text classification

What is a support vector machine – first take

- Vector space classification (similar to Rocchio, kNN, linear classifiers)
- Difference from previous methods: **large margin** classifier
- We aim to find a separating hyperplane (decision boundary) that is **maximally far** from any point in the training data
- In case of nonlinear separability: We may have to discount some points as outliers or noise.

(Linear) Support Vector Machines

- binary classification problem
- Decision boundary is **linear separator**.
- criterion: being maximally far away from any data point \rightarrow determines classifier **margin**
- Vectors on margin lines are called **support vectors**
- Set of support vectors are a complete specification of classifier

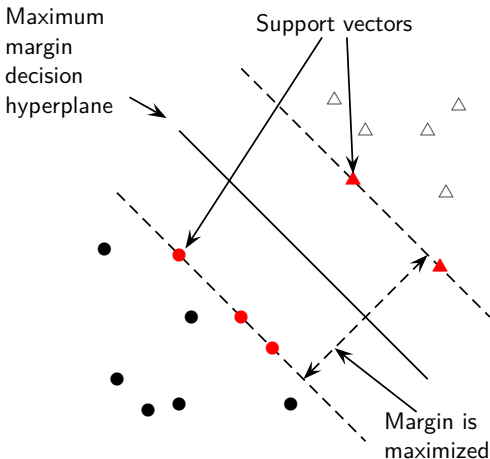


Why maximize the margin?

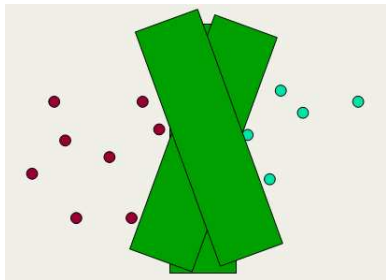
Points near the decision surface are **uncertain classification decisions**.

A classifier with a large margin makes **no low certainty classification decisions** (on the training set).

Gives classification safety margin with respect to errors and random variation



Why maximize the margin?



- SVM classification = large margin around decision boundary
- We can think of the margin as a “fat separator” – a fatter version of our regular decision hyperplane.
- unique solution
- decreased memory capacity
- increased ability to correctly generalize to test data

Separating hyperplane: Recap

Hyperplane

An n-dimensional generalization of a plane (point in 1-D space, line in 2-D space, ordinary plane in 3-D space).

Decision hyperplane

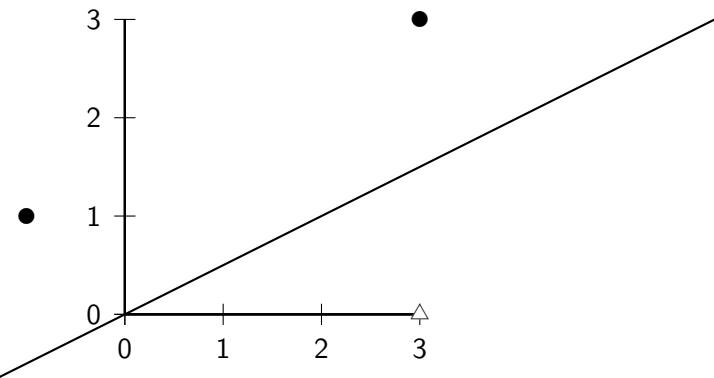
Can be defined by:

- intercept term b (we were calling this θ before)
- normal vector \vec{w} (**weight vector**) which is perpendicular to the hyperplane

All points \vec{x} on the hyperplane satisfy:

$$\vec{w}^T \vec{x} + b = 0$$

Exercise



Draw the maximum margin separator. Which vectors are the support vectors? Coordinates of dots: $(3,3)$, $(-1,1)$. Coordinates of triangle: $(3,0)$

Formalization of SVMs

Training set

Consider a binary classification problem:

- \vec{x}_i are the input vectors
- y_i are the labels

For SVMs, the two classes are $y_i = +1$ and $y_i = -1$.

The linear classifier is then:

$$f(\vec{x}) = \text{sign}(\vec{w}^T \vec{x} + b)$$

A value of -1 indicates one class, and a value of $+1$ the other class.

Functional margin of a point

SVM makes its decision based on the score $\vec{w}^T \vec{x} + b$.

Clearly, the larger $|\vec{w}^T \vec{x} + b|$ is, the more confidence we can have that the decision is correct.

Functional margin

- The functional margin of the vector \vec{x}_i w.r.t the hyperplane $\langle \vec{w}, b \rangle$ is: $y_i(\vec{w}^T \vec{x}_i + b)$
- The **functional margin of a data set** w.r.t a decision surface is **twice the functional margin of any of the points** in the data set with minimal functional margin
- Factor 2 comes from measuring across the whole width of the margin.

Problem: We can increase functional margin by scaling \vec{w} and b .

→ We need to place some constraint on the size of \vec{w} .

Geometric margin

Geometric margin of the classifier: maximum width of the band that can be drawn separating the support vectors of the two classes.

To compute the geometric margin, we need to compute the distance of a vector \vec{x} from the hyperplane:

$$r = y \frac{\vec{w}^T \vec{x} + b}{|\vec{w}|}$$

(why? we will see that this is so graphically in a few moments)
Distance is of course invariant to scaling: if we replace \vec{w} by $5\vec{w}$ and b by $5b$, then the distance is the same because it is normalized by the length of \vec{w} .

Optimization problem solved by SVMs

Assume canonical “functional margin” distance

Assume that every data point has at least distance 1 from the hyperplane, then:

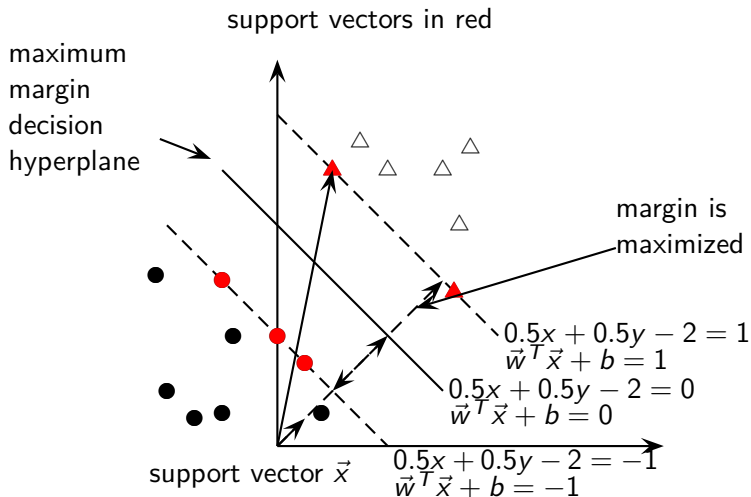
$$y_i(\vec{w}^T \vec{x}_i + b) \geq 1$$

Since each example's distance from the hyperplane is

$r_i = y_i(\vec{w}^T \vec{x}_i + b)/|\vec{w}|$, the margin is $\rho = 2/|\vec{w}|$. We want to maximize this margin. That is, we want to find \vec{w} and b such that:

- For all $(\vec{x}_i, y_i) \in \mathbb{D}$, $y_i(\vec{w}^T \vec{x}_i + b) \geq 1$
- $\rho = 2/|\vec{w}|$ is maximized

Support Vector Machines



$$\vec{w}^T \vec{w}' + b = 0$$

$$b = -\vec{w}^T \vec{w}'$$

$$\frac{b}{|\vec{w}|} = -\frac{\vec{w}^T \vec{w}'}{|\vec{w}|}$$

Distance of support vector from separator =
(length of projection of \vec{x} onto \vec{w}) minus (length of \vec{w}')

$$\frac{\vec{w}^T \vec{x}}{|\vec{w}|} - \frac{\vec{w}^T \vec{w}'}{|\vec{w}|}$$

$$= \frac{\vec{w}^T \vec{x}}{|\vec{w}|} + \frac{b}{|\vec{w}|}$$

$$= \frac{\vec{w}^T \vec{x} + b}{|\vec{w}|}$$

Distance of support vector from separator =
 (length of projection of $\vec{x} = (1 \ 5)^T$ onto \vec{w}) minus (length of \vec{w}')

$$\frac{\vec{w}^T \vec{x}}{|\vec{w}|} - \frac{\vec{w}^T \vec{w}'}{|\vec{w}|}$$

$$(1 \cdot 2 + 5 \cdot 2)/(1/\sqrt{2}) - (0.5 \cdot 2 + 0.5 \cdot 2)/(1/\sqrt{2})$$

$$3/(1/\sqrt{2}) - 2/(1/\sqrt{2})$$

$$\frac{\vec{w}^T \vec{x}}{|\vec{w}|} + \frac{b}{|\vec{w}|}$$

$$3/(1/\sqrt{2}) + (-2)/(1/\sqrt{2})$$

$$\frac{3 - 2}{1/\sqrt{2}}$$

$$\sqrt{2}$$

Optimization problem solved by SVMs (2)

Maximizing $2/|\vec{w}|$ is the same as minimizing $|\vec{w}|/2$.

This gives the final standard formulation of an SVM as a minimization problem:

Example

Find \vec{w} and b such that:

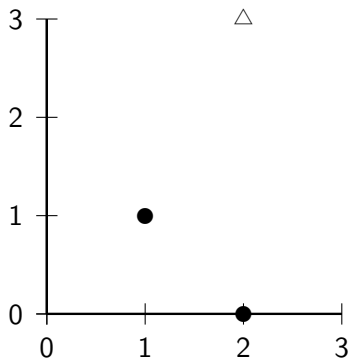
- $\frac{1}{2}\vec{w}^T\vec{w}$ is minimized (because $|\vec{w}| = \sqrt{\vec{w}^T\vec{w}}$), and
- for all $\{(\vec{x}_i, y_i)\}$, $y_i(\vec{w}^T\vec{x}_i + b) \geq 1$

We are now optimizing a **quadratic function** subject to linear constraints. Quadratic optimization problems are standard mathematical optimization problems, and many algorithms exist for solving them (e.g. Quadratic Programming libraries).

Recap

- We start with a training set.
- The data set defines the maximum-margin separating hyperplane (if it is separable).
- We use quadratic optimization to find this plane.
- Given a new point \vec{x} to classify, the classification function $f(\vec{x})$ computes the functional margin of the point (= normalized distance).
- The sign of this function determines the class to assign to the point.
- If the point is within the margin of the classifier, the classifier can return “don’t know” rather than one of the two classes.
- The value of $f(\vec{x})$ may also be transformed into a probability of classification

Exercise



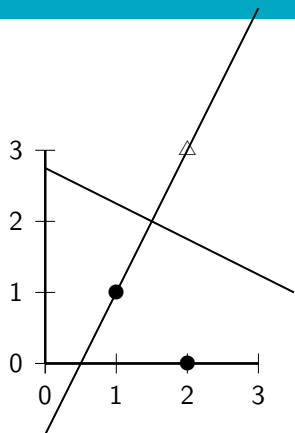
Which vectors are the support vectors? Draw the maximum margin separator. What values of w_1 , w_2 and b (for $w_1x + w_2y + b = 0$) describe this separator? Recall that we must have $w_1x + w_2y + b \in \{1, -1\}$ for the support vectors.

Walkthrough example

Working geometrically:

- The maximum margin weight vector will be parallel to the shortest line connecting points of the two classes, that is, the line between $(1, 1)$ and $(2, 3)$, giving a weight vector of $(1, 2)$.
- The optimal decision surface is orthogonal to that line and intersects it at the halfway point. Therefore, it passes through $(1.5, 2)$.
- The SVM decision boundary is:

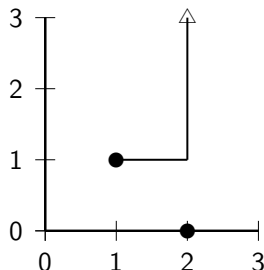
$$0 = x + 2y - (1 \cdot 1.5 + 2 \cdot 2) \Leftrightarrow 0 = \frac{2}{5}x + \frac{4}{5}y - \frac{11}{5}$$



Walkthrough example

Working algebraically:

- With the constraint $\text{sign}(y_i(\vec{w}^T \vec{x}_i + b)) \geq 1$, we seek to minimize $|\vec{w}|$.
- We know that the solution is $\vec{w} = (a, 2a)$ for some a . So:
 $a + 2a + b = -1$, $2a + 6a + b = 1$
- Hence, $a = 2/5$ and $b = -11/5$. So the optimal hyperplane is given by $\vec{w} = (2/5, 4/5)$ and $b = -11/5$.
- The margin ρ is $2/|\vec{w}| = 2/\sqrt{4/25 + 16/25} = 2/(2\sqrt{5}/5) = \sqrt{5} = \sqrt{(1-2)^2 + (1-3)^2}$.



Soft margin classification

What happens if data is not linearly separable?

- Standard approach: allow the fat decision margin to make a few mistakes
 - some points, outliers, noisy examples are inside or on the wrong side of the margin
- Pay cost for each misclassified example, depending on how far it is from meeting the margin requirement

Slack variable ξ_i : A non-zero value for ξ_i allows \vec{x}_i to not meet the margin requirement at a cost proportional to the value of ξ_i .

Optimization problem: trading off how fat it can make the margin vs. how many points have to be moved around to allow this margin. The sum of the ξ_i gives an upper bound on the number of training errors. Soft-margin SVMs minimize training error traded off against margin.

Using SVM for one-of classification

- Recall how to use binary linear classifiers (k classes) for one-of: train and run k classifiers and then select the class with the highest confidence
- Another strategy used with SVMs: build $k(k - 1)/2$ one-versus-one classifiers, and choose the class that is selected by the most classifiers. While this involves building a very large number of classifiers, the time for training classifiers may actually decrease, since the training data set for each classifier is much smaller.
- Yet another possibility: structured prediction. Generalization of classification where the classes are not just a set of independent, categorical labels, but may be arbitrary structured objects with relationships defined between them

Text classification

- Many commercial applications
- There are many applications of text classification for corporate Intranets, government departments, and Internet publishers.
- Often greater performance gains from exploiting domain-specific text features than from changing from one machine learning method to another.
- Understanding the data is one of the keys to successful categorization, yet this is an area in which many categorization tool vendors are weak.

Choosing what kind of classifier to use

When building a text classifier, first question: **how much training data is there currently available?**

Practical challenge: creating or obtaining enough training data

Hundreds or thousands of examples from each class are required to produce a high performance classifier and many real world contexts involve large sets of categories.

- None?
- Very little?
- Quite a lot?
- A huge amount, growing every day?

If you have no labeled training data

Use hand-written rules!

Example

```
IF (wheat OR grain) AND NOT (whole OR bread) THEN  
c = grain
```

In practice, rules get a lot bigger than this, and can be phrased using more sophisticated query languages than just Boolean expressions, including the use of numeric scores.

With careful crafting, the accuracy of such rules can become very high (high 90% precision, high 80% recall).

Nevertheless the amount of work to create such well-tuned rules is very large. A reasonable estimate is 2 days per class, and extra time has to go into maintenance of rules, as the content of documents in classes drifts over time.

A Verity topic (a complex classification rule)

```

comment line      # Beginning of art topic definition
top-level topic  art ACCRUE
                 /author = "fsmith"
topic definition modifiers } /date = "30-Dec-01"
                           /annotation = "Topic created
                             by fsmith"
subtopic topic   * 0.70 performing-arts ACCRUE
evidencetopic   ** 0.50 WORD
topic definition modifier /wordtext = ballet
evidencetopic   ** 0.50 STEM
topic definition modifier /wordtext = dance
evidencetopic   ** 0.50 WORD
topic definition modifier /wordtext = opera
evidencetopic   ** 0.30 WORD
topic definition modifier /wordtext = symphony
subtopic        * 0.70 visual-arts ACCRUE
                 ** 0.50 WORD
                 /wordtext = painting
                 ** 0.50 WORD
                 /wordtext = sculpture
subtopic        * 0.70 film ACCRUE
                 ** 0.50 STEM
                 /wordtext = film
subtopic        ** 0.50 motion-picture PHRASE
                 *** 1.00 WORD
                 /wordtext = motion
                 *** 1.00 WORD
                 /wordtext = picture

```

Westlaw: Example queries

Information need: Information on the legal theories involved in preventing the disclosure of trade secrets by employees formerly employed by a competing company

Query: "trade secret" /s disclos! /s prevent /s employe!

Information need: Requirements for disabled people to be able to access a workplace

Query: disab! /p access! /s work-site work-place (employment /3 place)

Information need: Cases about a host's responsibility for drunk guests

Query: host! /p (responsib! liab!) /p (intoxicat! drunk!) /p guest

If you have fairly little data and you are going to train a supervised classifier

Work out how to get more labeled data as quickly as you can.

- Best way: insert yourself into a process where humans will be willing to label data for you as part of their natural tasks.

Example

Often humans will sort or route email for their own purposes, and these actions give information about classes.

Active Learning

A system is built which decides which documents a human should label.

Usually these are the ones on which a classifier is uncertain of the correct classification.

If you have labeled data

Good amount of labeled data, but not huge

Use everything that we have presented about text classification.
Consider hybrid approach (overlay Boolean classifier)

Huge amount of labeled data

Choice of classifier probably has little effect on your results.
Choose classifier based on the scalability of training or runtime efficiency.

Rule of thumb: each doubling of the training data size produces a linear increase in classifier performance, but with very large amounts of data, the improvement becomes sub-linear.

Large and difficult category taxonomies

If you have a small number of well-separated categories, then many classification algorithms are likely to work well. But often: very large number of very similar categories.

Example

Web directories (e.g. the Yahoo! Directory consists of over 200,000 categories or the Open Directory Project), library classification schemes (Dewey Decimal or Library of Congress), the classification schemes used in legal or medical applications.

Accurate classification over large sets of closely related classes is **inherently difficult**. – No general high-accuracy solution.

Recap

- Is there a learning method that is optimal for all text classification problems?
- No, because there is a trade-off between bias and variance.
- Factors to take into account:
 - How much training data is available?
 - How simple/complex is the problem? (linear vs. nonlinear decision boundary)
 - How noisy is the problem?
 - How stable is the problem over time?
 - For an unstable problem, it's better to use a simple and robust classifier.

Take-away today

- **Support vector machines:** State-of-the-art text classification methods (linear and nonlinear)
- Introduction to SVMs
- Formalization
- Soft margin case for nonseparable problems
- **Discussion:** Which classifier should I use for my problem?

Resources

- Chapter 14 of IIR (basic vector space classification)
- Chapter 15-1 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
- Discussion of “how to select the right classifier for my problem” in Russell and Norvig

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 16: Flat Clustering Handout version

Petr Sojka, Hinrich Schütze et al.

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Center for Information and Language Processing, University of Munich

2024-05-01

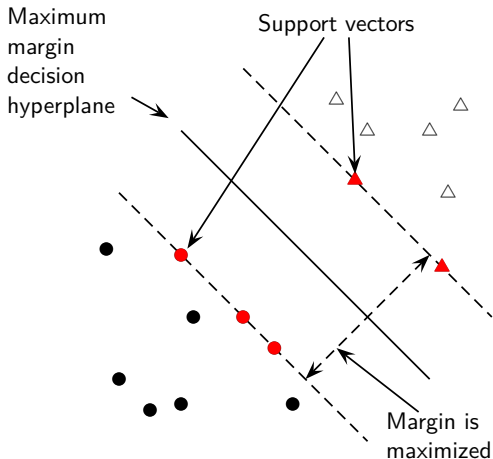
(compiled on 2024-05-14 23:03:33)

Overview

- 1 Recap
- 2 Clustering: Introduction
- 3 Clustering in IR
- 4 *K*-means
- 5 Evaluation
- 6 How many clusters?

Support vector machines

- Binary classification problem
- Simple SVMs are linear classifiers.
- criterion: being maximally far away from any data point
→ determines classifier **margin**
- linear separator position defined by **support vectors**



Optimization problem solved by SVMs

Find \vec{w} and b such that:

- $\frac{1}{2} \vec{w}^T \vec{w}$ is minimized (because $|\vec{w}| = \sqrt{\vec{w}^T \vec{w}}$), and
- for all $\{(\vec{x}_i, y_i)\}$, $y_i(\vec{w}^T \vec{x}_i + b) \geq 1$

Which machine learning method to choose?

- Is there a learning method that is optimal for all text classification problems?
- No, because there is a tradeoff, a dilemma between bias and variance.
- Factors to take into account:
 - How much training data is available?
 - How simple/complex is the problem? (linear vs. nonlinear decision boundary)
 - How noisy is the problem?
 - How stable is the problem over time?
 - For an unstable problem, it's better to use a simple and robust classifier.

See Fig. 15 in Geman et al.

Take-away today

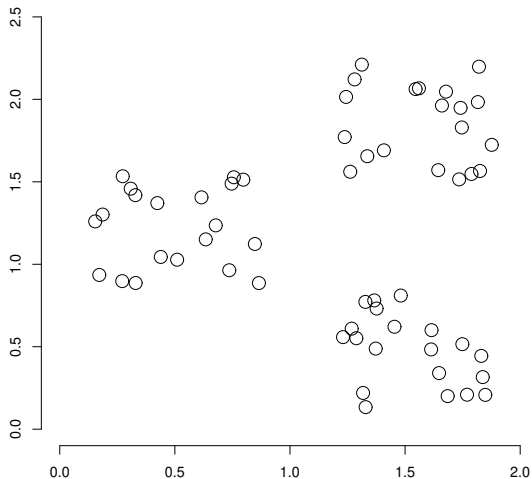
- What is clustering?
- Applications of clustering in information retrieval
- *K*-means algorithm
- Evaluation of clustering
- How many clusters?



Clustering: Definition

- (Document) clustering is the process of **grouping a set of documents into clusters of similar documents**.
- Documents within a cluster should be similar.
- Documents from different clusters should be dissimilar.
- Clustering is the most common form of **unsupervised** learning.
- Unsupervised = there are no labeled or annotated data.
- Hard clustering vs. soft clustering.
- Cardinality of clustering.

Exercise: Data set with clear cluster structure



Propose
algorithm
for finding
the cluster
structure in
this
example

Classification vs. Clustering

- Classification: supervised learning
- Clustering: unsupervised learning
- Classification: Classes are **human-defined** and part of the input to the learning algorithm.
- Clustering: Clusters are **inferred from the data** without human input.
 - However, there are many ways of influencing the outcome of clustering: number of clusters, similarity measure, representation of documents, ...



The cluster hypothesis

Cluster hypothesis. Documents in the same cluster behave similarly with respect to relevance to information needs.

All applications of clustering in IR are based (directly or indirectly) on the cluster hypothesis.

Van Rijsbergen's original wording (1979): "closely associated documents tend to be relevant to the same requests". □

Applications of clustering in IR

| application | what is clustered? | benefit |
|--------------------------|-------------------------|---|
| search result clustering | search results | more effective information presentation to user |
| Scatter-Gather | (subsets of) collection | alternative user interface: "search without typing" |
| collection clustering | collection | effective information presentation for exploratory browsing |
| cluster-based retrieval | collection | higher efficiency: faster search |

Search result clustering for better navigation



[Advanced](#)
[Search](#)
[Help](#)

Clustered Results

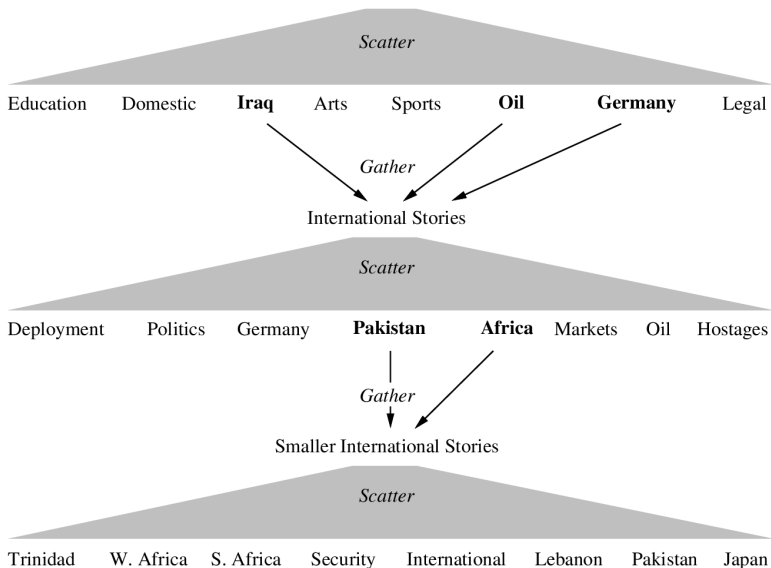
- ▶ [jaguar](#) (208)
- ⊕ ▶ [Cars](#) (74)
- ⊕ ▶ [Club](#) (34)
- ⊕ ▶ [Cat](#) (23)
- ⊕ ▶ [Animal](#) (13)
- ⊕ ▶ [Restoration](#) (10)
- ⊕ ▶ [Mac OS X](#) (8)
- ⊕ ▶ [Jaguar Model](#) (8)
- ⊕ ▶ [Request](#) (5)
- ⊕ ▶ [Mark Webber](#) (6)
- ▶ [Maya](#) (5)
- ▼ [More](#)

Find in clusters:


 Top 208 results of at least 20,373,974 retrieved for the query **jaguar** ([Details](#))

1. [Jag-lovers - THE source for all Jaguar information](#) [\[new window\]](#) [\[frame\]](#) [\[cache\]](#) [\[preview\]](#) [\[clusters\]](#)
 ... Internet! Serving Enthusiasts since 1993 The Jag-lovers Web Currently with 40661 members The Premier **Jaguar** Cars web resource for all enthusiasts Lists and Forums Jag-lovers originally evolved around its ...
[www.jag-lovers.org](#) - Open Directory 2, Wisenut 8, Ask Jeeves 8, MSN 9, Looksmart 12, MSN Search 18
2. [Jaguar Cars](#) [\[new window\]](#) [\[frame\]](#) [\[cache\]](#) [\[preview\]](#) [\[clusters\]](#)
 [...] redirected to [www.jaguar.com](#)
[www.jaguarcars.com](#) - Looksmart 1, MSN 2, Lycos 3, Wisenut 6, MSN Search 9, MSN 29
3. [http://www.jaguar.com/](#) [\[new window\]](#) [\[frame\]](#) [\[preview\]](#) [\[clusters\]](#)
[www.jaguar.com](#) - MSN 1, Ask Jeeves 1, MSN Search 3, Lycos 9
4. [Apple - Mac OS X](#) [\[new window\]](#) [\[frame\]](#) [\[preview\]](#) [\[clusters\]](#)
 Learn about the new OS X Server, designed for the Internet, digital media and workgroup management
 Download a technical factsheet.
[www.apple.com/macosex](#) - Wisenut 1, MSN 3, Looksmart 25

Scatter-Gather




Global navigation: Yahoo

YAHOO! DIRECTORY Search: the Web | the Directory | this category

Society and Culture

Directory > Society and Culture

 **Culture** SPONSOR RE
www.Dealtime.com Shop and save on Magazines.

CATEGORIES [\(What's This?\)](#)

Most Popular Society and Culture

- [Crime](#) (5453) NEW!
- [Cultures and Groups](#) (11025) NEW!
- [Environment and Nature](#) (8558) NEW!
- [Families](#) (1215)
- [Food and Drink](#) (9776) NEW!
- [Holidays and Observances](#) (3333)
- [Issues and Causes](#) (4842)
- [Mythology and Folklore](#) (984)
- [People](#) (16351)
- [Relationships](#) (595)
- [Religion and Spirituality](#) (37533)
- [Sexuality](#) (2812) NEW!

Additional Society and Culture Categories

- [Advice](#) (48)
- [Chats and Forums](#) (27)
- [Cultural Policy](#) (10)
- [Death and Dying](#) (394)
- [Disabilities](#) (1293)
- [Employment and Work@](#)
- [Etiquette](#) (54)
- [Events](#) (27)
- [Fashion@](#)
- [Gender](#) (21)
- [Home and Garden](#) (1080) NEW!
- [Magazines](#) (164)
- [Museums and Exhibits](#) (6052)
- [Pets@](#)
- [Reunions](#) (228)
- [Social Organizations](#) (338)
- [Web Directories](#) (6)
- [Weddings](#) (371)

SITE LISTINGS By Popularity | [Alphabetical](#) | [\(What's This?\)](#) Site

Global navigation: Medical Subject Headings MESH (upper level)

MeSH Tree Structures - 2008

[Return to Entry Page](#)

1. [Anatomy \[A\]](#)
2. [Organisms \[B\]](#)
3. [Diseases \[C\]](#)
 - [Bacterial Infections and Mycoses \[C01\] +](#)
 - [Virus Diseases \[C02\] +](#)
 - [Parasitic Diseases \[C03\] +](#)
 - [Neoplasms \[C04\] +](#)
 - [Musculoskeletal Diseases \[C05\] +](#)
 - [Digestive System Diseases \[C06\] +](#)
 - [Stomatognathic Diseases \[C07\] +](#)
 - [Respiratory Tract Diseases \[C08\] +](#)
 - [Otorhinolaryngologic Diseases \[C09\] +](#)
 - [Nervous System Diseases \[C10\] +](#)
 - [Eye Diseases \[C11\] +](#)
 - [Male Urogenital Diseases \[C12\] +](#)
 - [Female Urogenital Diseases and Pregnancy Complications \[C13\] +](#)
 - [Cardiovascular Diseases \[C14\] +](#)
 - [Hemic and Lymphatic Diseases \[C15\] +](#)
 - [Congenital, Hereditary, and Neonatal Diseases and Abnormalities \[C16\] +](#)
 - [Skin and Connective Tissue Diseases \[C17\] +](#)
 - [Nutritional and Metabolic Diseases \[C18\] +](#)
 - [Endocrine System Diseases \[C19\] +](#)
 - [Immune System Diseases \[C20\] +](#)
 - [Disorders of Environmental Origin \[C21\] +](#)
 - [Animal Diseases \[C22\] +](#)
 - [Pathological Conditions, Signs and Symptoms \[C23\] +](#)
4. [Chemicals and Drugs \[D\]](#)
5. [Analytical, Diagnostic and Therapeutic Techniques and Equipment \[E\]](#)
6. [Psychiatry and Psychology \[F\]](#)
7. [Biological Sciences \[G\]](#)
8. [Natural Sciences \[H\]](#)
9. [Anthropology, Education, Sociology and Social Phenomena \[I\]](#)
10. [Technology, Industry, Agriculture \[J\]](#)
11. [Humanities \[K\]](#)

Global navigation: MESH (lower level)

[Neoplasms \[C04\]](#)

[Cysts \[C04.182\]](#) +

[Hamartoma \[C04.445\]](#) +

► [Neoplasms by Histologic Type \[C04.557\]](#)

[Histiocytic Disorders, Malignant \[C04.557.227\]](#) +

[Leukemia \[C04.557.337\]](#) +

[Lymphatic Vessel Tumors \[C04.557.375\]](#) +

[Lymphoma \[C04.557.386\]](#) +

[Neoplasms, Complex and Mixed \[C04.557.435\]](#) +

[Neoplasms, Connective and Soft Tissue \[C04.557.450\]](#) +

[Neoplasms, Germ Cell and Embryonal \[C04.557.465\]](#) +

[Neoplasms, Glandular and Epithelial \[C04.557.470\]](#) +

[Neoplasms, Gonadal Tissue \[C04.557.475\]](#) +

[Neoplasms, Nerve Tissue \[C04.557.580\]](#) +

[Neoplasms, Plasma Cell \[C04.557.595\]](#) +

[Neoplasms, Vascular Tissue \[C04.557.645\]](#) +

[Nevi and Melanomas \[C04.557.665\]](#) +

[Odontogenic Tumors \[C04.557.695\]](#) +

[Neoplasms by Site \[C04.588\]](#) +

[Neoplasms, Experimental \[C04.619\]](#) +

[Neoplasms, Hormone-Dependent \[C04.626\]](#)

[Neoplasms, Multiple Primary \[C04.651\]](#) +

[Neoplasms, Post-Traumatic \[C04.666\]](#)

[Neoplasms, Radiation-Induced \[C04.682\]](#) +

[Neoplasms, Second Primary \[C04.692\]](#)

[Neoplastic Processes \[C04.697\]](#) +

[Neoplastic Syndromes, Hereditary \[C04.700\]](#) +

[Paraneoplastic Syndromes \[C04.730\]](#) +

[Precancerous Conditions \[C04.834\]](#) +

[Pregnancy Complications, Neoplastic \[C04.850\]](#) +

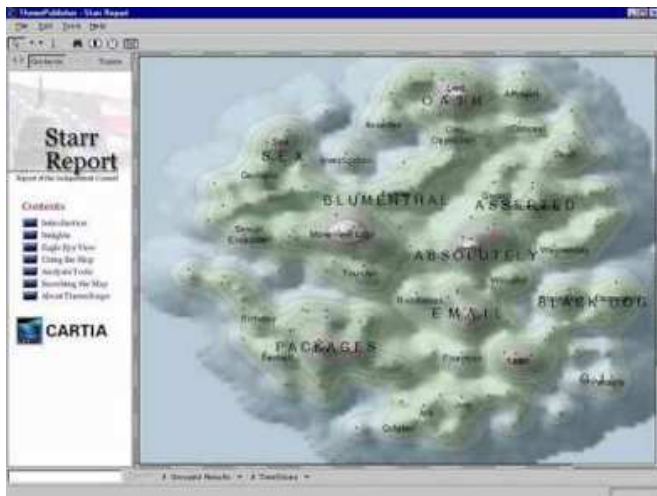
[Tumor Virus Infections \[C04.925\]](#) +

Navigational hierarchies: Manual vs. automatic creation

- Note: Yahoo/MESH are **not** examples of clustering.
- But they are well known examples for using a global hierarchy for navigation.
- Some examples for global navigation/exploration based on clustering:
 - Arxiv's LDAExplore: <https://arxiv.lateral.io/>
 - Cartia
 - Themescapes
 - Google News



Global navigation combined with visualization (1)



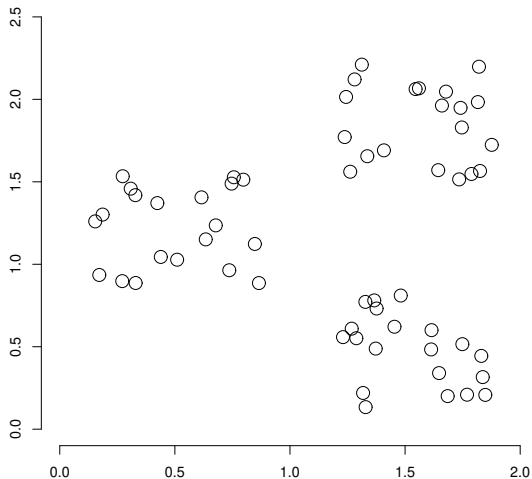
Global clustering for navigation: Google News

`http://news.google.com`

Clustering for improving recall

- To improve search recall:
 - Cluster docs in collection a priori
 - When a query matches a doc d , also return other docs in the cluster containing d
- Hope: if we do this: the query “car” will also return docs containing “automobile”
 - Because the clustering algorithm groups together docs containing “car” with those containing “automobile”.
 - Both types of documents contain words like “parts”, “dealer”, “mercedes”, “road trip”. □

Exercise: Data set with clear cluster structure




Propose
algorithm
for finding
the cluster
structure in
this
example

Desiderata for clustering

- General goal: put related docs in the same cluster, put unrelated docs in different clusters.
 - We'll see different ways of formalizing this.
- The number of clusters should be appropriate for the data set we are clustering.
 - Initially, we will assume the number of clusters K is given.
 - Later: Semiautomatic methods for determining K
- Secondary goals in clustering
 - Avoid very small and very large clusters
 - Define clusters that are easy to explain to the user
 - Many others . . .



Flat vs. Hierarchical clustering

- Flat algorithms
 - Usually start with a random (partial) partitioning of docs into groups
 - Refine iteratively
 - Main algorithm: K -means
 - Hierarchical algorithms
 - Create a hierarchy
 - Bottom-up, agglomerative
 - Top-down, divisive
- 

Hard vs. Soft clustering

- Hard clustering: Each document belongs to **exactly one** cluster.
 - More common and easier to do
- Soft clustering: A document can belong to **more than one** cluster.
 - Makes more sense for applications like creating browsable hierarchies
 - You may want to put *sneakers* in two clusters:
 - sports apparel
 - shoes
 - You can only do that with a soft clustering approach.
- This class: flat, hard clustering; next: hierarchical, hard clustering then: latent semantic indexing, a form of soft clustering □
- We won't have time for soft clustering. See IIR 16.5, IIR 18
- Non-exhaustive clustering: some docs are not assigned to any cluster. See references in IIR 16.

Flat algorithms

- Flat algorithms compute a partition of N documents into a set of K clusters.
- Given: a set of documents and the number K
- Find: a partition into K clusters that optimizes the chosen partitioning criterion
- Global optimization: exhaustively enumerate partitions, pick optimal one
 - Not tractable
- Effective heuristic method: K -means algorithm

K-means

- Perhaps the best known clustering algorithm
- Simple, works well in many cases
- Use as default / baseline for clustering documents

Document representations in clustering

- Vector space model
- As in vector space classification, we measure relatedness between vectors by **Euclidean distance** . . .
- . . . which is almost equivalent to cosine similarity.
- Almost: centroids are not length-normalized. □

K-means: Basic idea

- Each cluster in K-means is defined by a **centroid**.
- Objective/partitioning criterion: **minimize the average squared difference from the centroid**
- Recall definition of centroid:

$$\vec{\mu}(\omega) = \frac{1}{|\omega|} \sum_{\vec{x} \in \omega} \vec{x}$$

where we use ω to denote a cluster.

- We try to find the minimum average squared difference by iterating two steps:
 - **reassignment**: assign each vector to its closest centroid
 - **recomputation**: recompute each centroid as the average of the vectors that were assigned to it in reassignment

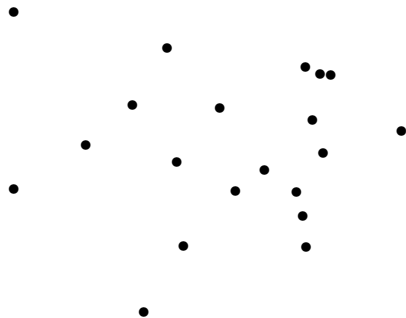
K-means pseudocode (μ_k is centroid of ω_k)

```

K-MEANS( $\{\vec{x}_1, \dots, \vec{x}_N\}, K$ )
1  ( $\vec{s}_1, \vec{s}_2, \dots, \vec{s}_K$ )  $\leftarrow$  SELECTRANDOMSEEDS( $\{\vec{x}_1, \dots, \vec{x}_N\}, K$ )
2  for  $k \leftarrow 1$  to  $K$ 
3  do  $\vec{\mu}_k \leftarrow \vec{s}_k$ 
4  while stopping criterion has not been met
5  do for  $k \leftarrow 1$  to  $K$ 
6      do  $\omega_k \leftarrow \{\}$ 
7      for  $n \leftarrow 1$  to  $N$ 
8          do  $j \leftarrow \arg \min_{j'} |\vec{\mu}_{j'} - \vec{x}_n|$ 
9               $\omega_j \leftarrow \omega_j \cup \{\vec{x}_n\}$  (reassignment of vectors)
10     for  $k \leftarrow 1$  to  $K$ 
11         do  $\vec{\mu}_k \leftarrow \frac{1}{|\omega_k|} \sum_{\vec{x} \in \omega_k} \vec{x}$  (recomputation of centroids)
12 return  $\{\vec{\mu}_1, \dots, \vec{\mu}_K\}$ 

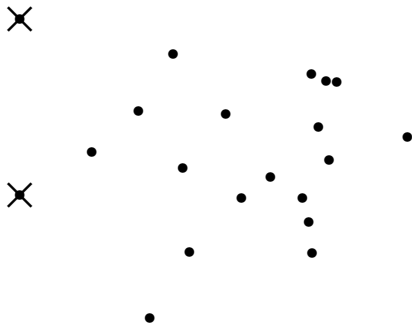
```

Worked Example: Set of points to be clustered

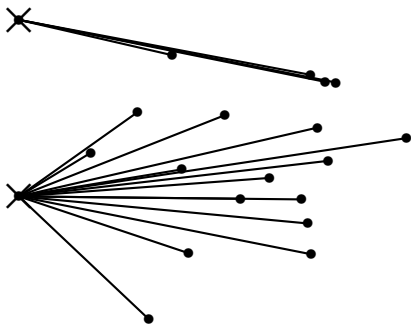


Exercise: (i) Guess what the optimal clustering into two clusters is in this case; (ii) compute the centroids of the clusters □

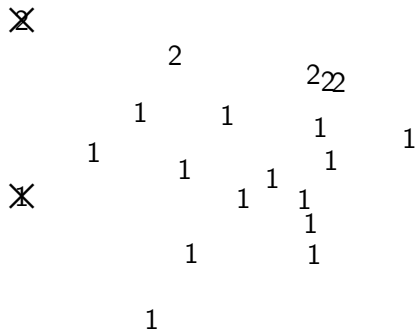
Worked Example: Random selection of initial centroids



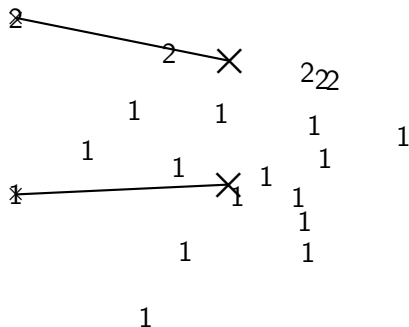
Worked Example: Assign points to closest center



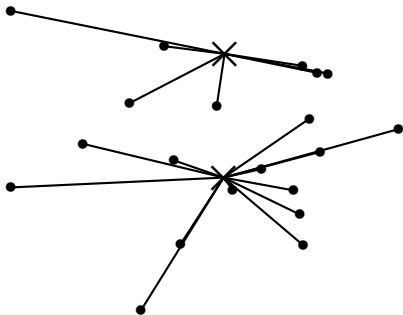
Worked Example: Assignment



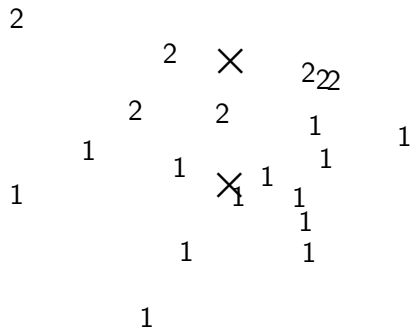
Worked Example: Recompute cluster centroids



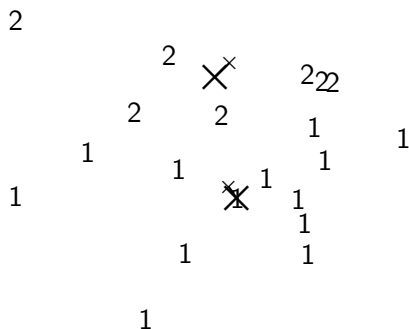
Worked Example: Assign points to closest centroid



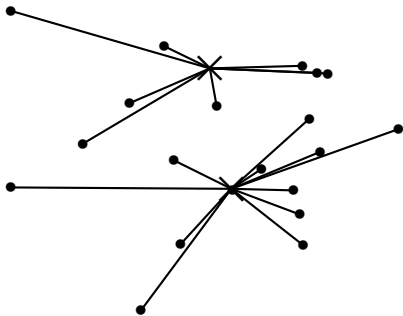
Worked Example: Assignment



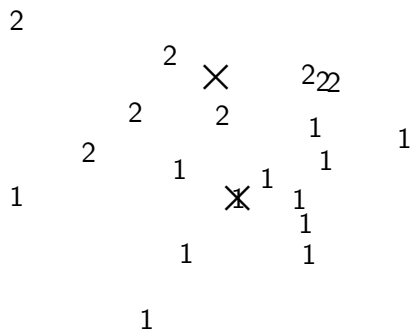
Worked Example: Recompute cluster centroids



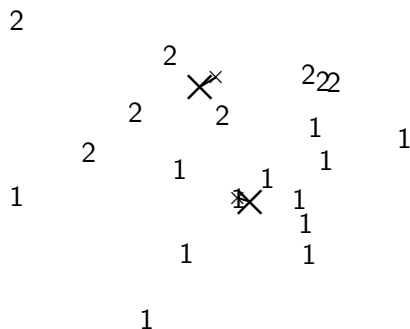
Worked Example: Assign points to closest centroid



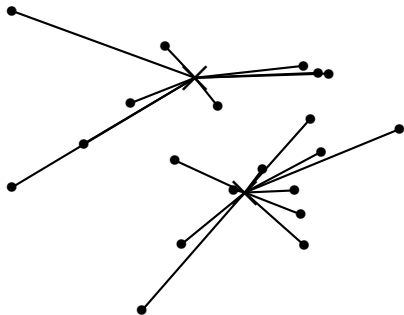
Worked Example: Assignment



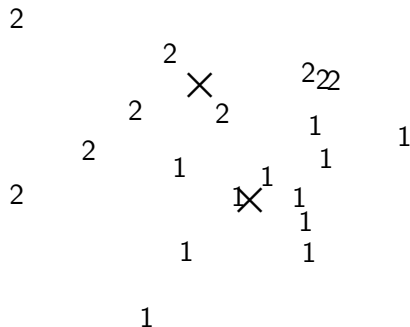
Worked Example: Recompute cluster centroids



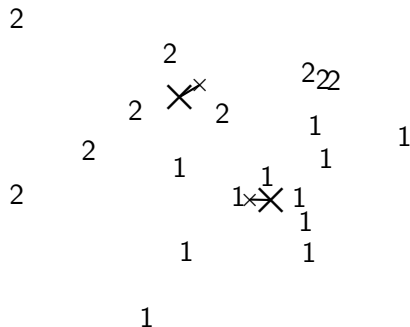
Worked Example: Assign points to closest centroid



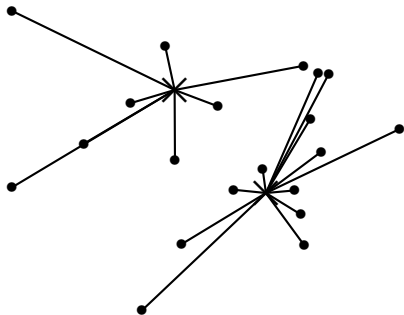
Worked Example: Assignment



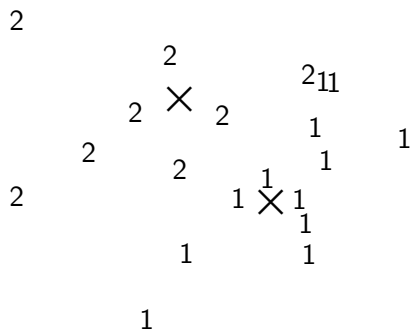
Worked Example: Recompute cluster centroids



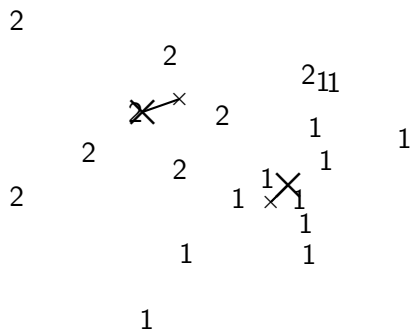
Worked Example: Assign points to closest centroid



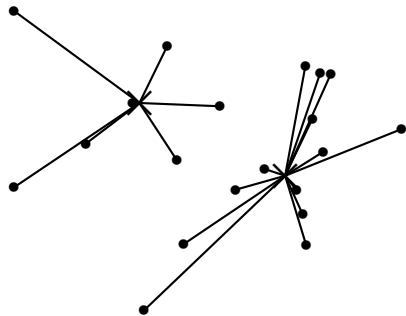
Worked Example: Assignment



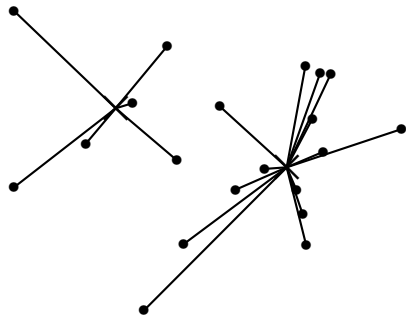
Worked Example: Recompute cluster centroids



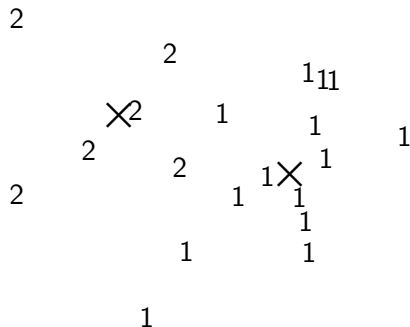
Worked Example: Assign points to closest centroid



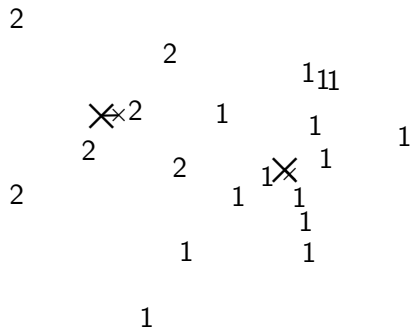
Worked Example: Assign points to closest centroid



Worked Example: Assignment



Worked Example: Recompute cluster centroids



K-means is guaranteed to converge: Proof

- RSS (Residual Sum of Squares) = sum of all squared distances between document vector and closest centroid
- RSS decreases during each reassignment step.
 - because each vector is moved to a closer centroid
- RSS decreases during each recomputation step.
 - see next slide
- There is only a finite number of clusterings.
- Thus: We must reach a fixed point.
- Assumption: Ties are broken consistently.
- Finite set & monotonically decreasing \rightarrow convergence □

Recomputation decreases average distance

$RSS = \sum_{k=1}^K RSS_k$ – the residual sum of squares (the “goodness” measure)

$$RSS_k(\vec{v}) = \sum_{\vec{x} \in \omega_k} \|\vec{v} - \vec{x}\|^2 = \sum_{\vec{x} \in \omega_k} \sum_{m=1}^M (v_m - x_m)^2$$

$$\frac{\partial RSS_k(\vec{v})}{\partial v_m} = \sum_{\vec{x} \in \omega_k} 2(v_m - x_m) = 0$$

$$v_m = \frac{1}{|\omega_k|} \sum_{\vec{x} \in \omega_k} x_m$$

The last line is the componentwise definition of the centroid!
 We minimize RSS_k when the old centroid is replaced with the new centroid. RSS , the sum of the RSS_k , must then also decrease during recomputation. □

K-means is guaranteed to converge

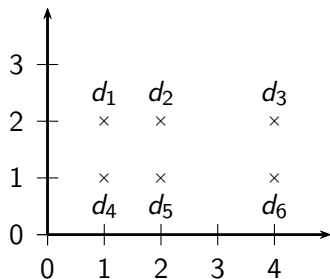
- But we don't know how long convergence will take!
- If we don't care about a few docs switching back and forth, then convergence is usually fast ($< 10\text{--}20$ iterations).
- However, complete convergence can take many more iterations.



Optimality of *K*-means

- Convergence \neq optimality
- Convergence does not mean that we converge to the optimal clustering!
- This is the great weakness of *K*-means.
- If we start with a bad set of seeds, the resulting clustering can be horrible. □

Exercise: Suboptimal clustering



- What is the optimal clustering for $K = 2$?
- Do we converge on this clustering for arbitrary seeds d_i, d_j ?



Initialization of *K*-means

- Random seed selection is just one of many ways *K*-means can be initialized.
- Random seed selection is not very robust: It's easy to get a suboptimal clustering.
- Better ways of computing initial centroids:
 - Select seeds not randomly, but using some heuristic (e.g., filter out outliers or find a set of seeds that has “good coverage” of the document space)
 - Use hierarchical clustering to find good seeds
 - Select i (e.g., $i = 10$) different random sets of seeds, do a *K*-means clustering for each, select the clustering with lowest RSS




Time complexity of K -means

- Computing one distance of two vectors is $O(M)$.
- Reassignment step: $O(KNM)$ (we need to compute KN document-centroid distances)
- Recomputation step: $O(NM)$ (we need to add each of the document's $< M$ values to one of the centroids)
- Assume number of iterations bounded by I
- Overall complexity: $O(IKNM)$ – linear in all important dimensions
- However: This is not a real worst-case analysis.
- In pathological cases, complexity can be worse than linear. □

What is a good clustering?

- Internal criteria
 - Example of an internal criterion: RSS in *K*-means
- But an internal criterion often does not evaluate the actual utility of a clustering in the application.
- Alternative: External criteria
 - Evaluate with respect to a human-defined classification □

External criteria for clustering quality

- Based on a gold standard data set, e.g., the Reuters collection we also used for the evaluation of classification
 - Goal: Clustering should reproduce the classes in the gold standard
 - (But we only want to reproduce how documents are divided into groups, not the class labels.)
 - First measure for how well we were able to reproduce the classes: **purity**
- 

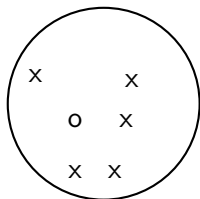
External criterion: Purity

$$\text{purity}(\Omega, \mathcal{C}) = \frac{1}{N} \sum_k \max_j |\omega_k \cap c_j|$$

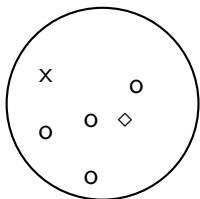
- $\Omega = \{\omega_1, \omega_2, \dots, \omega_K\}$ is the set of clusters and $\mathcal{C} = \{c_1, c_2, \dots, c_J\}$ is the set of classes.
- For each cluster ω_k : find class c_j with most members n_{kj} in ω_k
- Sum all n_{kj} and divide by total number of points □

Example for computing purity

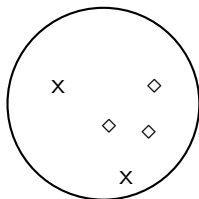
cluster 1



cluster 2



cluster 3



To compute purity: $5 = \max_j |\omega_1 \cap c_j|$ (class x, cluster 1); $4 = \max_j |\omega_2 \cap c_j|$ (class o, cluster 2); and $3 = \max_j |\omega_3 \cap c_j|$ (class \diamond , cluster 3). Purity is $(1/17) \times (5 + 4 + 3) \approx 0.71$. \square

Another external criterion: Rand index

- Purity can be increased easily by increasing K – a measure that does not have this problem: Rand index.

- Definition: $RI = \frac{TP+TN}{TP+FP+FN+TN}$

- Based on 2x2 contingency table of all **pairs of documents**:

| | | |
|-------------------|----------------------|----------------------|
| | same cluster | different clusters |
| same class | true positives (TP) | false negatives (FN) |
| different classes | false positives (FP) | true negatives (TN) |

- $TP+FN+FP+TN$ is the total number of pairs.
- $TP+FN+FP+TN = \binom{N}{2}$ for N documents.
- Example: $\binom{17}{2} = 136$ in o/◇/x example
- Each pair is either positive or negative (the clustering puts the two documents in the same or in different clusters) ...
- ... and either “true” (correct) or “false” (incorrect): the clustering decision is correct or incorrect. □

Rand Index: Example

As an example, we compute RI for the o/◇/x example. We first compute TP + FP. The three clusters contain 6, 6, and 5 points, respectively, so the total number of “positives” or pairs of documents that are in the same cluster is:

$$TP + FP = \binom{6}{2} + \binom{6}{2} + \binom{5}{2} = 40$$

Of these, the x pairs in cluster 1, the o pairs in cluster 2, the ◇ pairs in cluster 3, and the x pair in cluster 3 are true positives:

$$TP = \binom{5}{2} + \binom{4}{2} + \binom{3}{2} + \binom{2}{2} = 20$$

Thus, $FP = 40 - 20 = 20$.

FN and TN are computed similarly. □

Rand measure for the o/◇/x example

| | same cluster | different clusters |
|-------------------|--------------|--------------------|
| same class | TP = 20 | FN = 24 |
| different classes | FP = 20 | TN = 72 |

RI is then $(20 + 72)/(20 + 20 + 24 + 72) \approx 0.68$.



Two other external evaluation measures

- Two other measures
- Normalized mutual information (NMI)
 - How much information does the clustering contain about the classification?
 - Singleton clusters (number of clusters = number of docs) have maximum MI
 - Therefore: normalize by entropy of clusters and classes
- F measure
 - Like Rand, but “precision” and “recall” can be weighted □

Evaluation results for the o/◇/x example

| | purity | NMI | RI | F_5 |
|-------------------|--------|------|------|-------|
| lower bound | 0.0 | 0.0 | 0.0 | 0.0 |
| maximum | 1.0 | 1.0 | 1.0 | 1.0 |
| value for example | 0.71 | 0.36 | 0.68 | 0.46 |

All four measures range from 0 (really bad clustering) to 1 (perfect clustering). □

How many clusters?

- Number of clusters K is given in many applications.
 - E.g., there may be an external constraint on K . Example: In the case of Scatter-Gather, it was hard to show more than 10–20 clusters on a monitor in the 90s.
- What if there is no external constraint? Is there a “right” number of clusters?
- One way to go: define an optimization criterion
 - Given docs, find K for which the optimum is reached.
 - What optimization criterion can we use?
 - We can't use RSS or average squared distance from centroid as criterion: always chooses $K = N$ clusters. □

Exercise

- Your job is to develop the clustering algorithms for a competitor to news.google.com
- You want to use K -means clustering.
- How would you determine K ?



Simple objective function for K : Basic idea

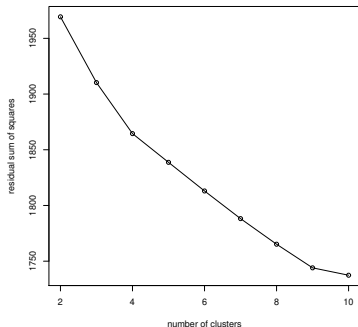
- Start with 1 cluster ($K = 1$)
- Keep adding clusters (= keep increasing K)
- Add a penalty for each new cluster
- Then trade off cluster penalties against average squared distance from centroid
- Choose the value of K with the best tradeoff □

Simple objective function for K : Formalization

- Given a clustering, define the cost for a document as (squared) distance to centroid
- Define total **distortion** $RSS(K)$ as sum of all individual document costs (corresponds to average distance)
- Then: penalize each cluster with a cost λ
- Thus for a clustering with K clusters, total cluster penalty is $K\lambda$
- Define the total cost of a clustering as distortion plus total cluster penalty: $RSS(K) + K\lambda$
- Select K that minimizes $(RSS(K) + K\lambda)$
- Still need to determine good value for $\lambda \dots$



Finding the “knee” in the curve



Pick the number of clusters where curve “flattens”. Here: 4 or 9.



Take-away today

- What is clustering?
- Applications of clustering in information retrieval
- K -means algorithm
- Evaluation of clustering
- How many clusters?



Resources

- Chapter 16 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - Keith van Rijsbergen on the cluster hypothesis (he was one of the originators)
 - Bing/Carrot2/Clusty: search result clustering systems
 - Stirling number: the number of distinct k -clusterings of n items

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 17: Hierarchical clustering Handout version

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2024-05-01

(compiled on 2024-06-10 08:55:35)

Overview

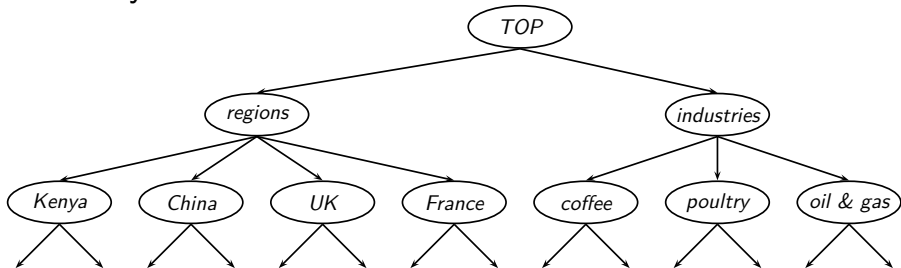
- 1 Introduction
- 2 Single-link/Complete-link
- 3 Centroid/GAAC
- 4 Labeling clusters
- 5 Variants

Take-away today

- Introduction to hierarchical clustering
- Single-link and complete-link clustering
- Centroid and group-average agglomerative clustering (GAAC)
- Bisecting K-means
- How to label clusters automatically □

Hierarchical clustering

Our goal in hierarchical clustering is to create a hierarchy like the one we saw earlier in Reuters:



We want to create this hierarchy **automatically**.

We can do this either **top-down** or **bottom-up**.

The best known bottom-up method is **hierarchical agglomerative clustering**.



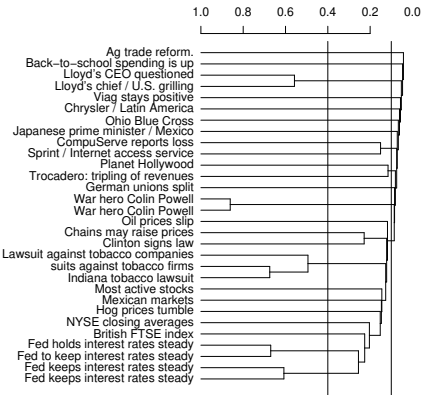
Hierarchical agglomerative clustering (HAC)

- HAC creates a hierarchy in the form of a binary tree.
- Assumes a similarity measure for determining the similarity of two [clusters](#).
- Up to now, our similarity measures were for [documents](#).
- We will look at four different cluster similarity measures. □

HAC: Basic algorithm

- Start with **each document in a separate cluster**
- Then **repeatedly merge** the two clusters that are most similar
- Until there is only one cluster.
- The history of merging is a hierarchy in the form of a binary tree.
- The standard way of depicting this history is a **dendrogram**. □

A dendrogram



- The history of mergers can be read off from bottom to top.
- The horizontal line of each merger tells us what the similarity of the merger was.
- We can cut the dendrogram at a particular point (e.g., at 0.1 or 0.4) to get a flat clustering.

Divisive clustering

- Divisive clustering is top-down.
- Alternative to HAC (which is bottom up).
- Divisive clustering:
 - Start with all docs in one big cluster
 - Then recursively split clusters
 - Eventually each node forms a cluster on its own.
- → Bisecting K -means at the end
- For now: HAC (= bottom-up) □

Naive HAC algorithm

```


SIMPLEHAC( $d_1, \dots, d_N$ )
1  for  $n \leftarrow 1$  to  $N$ 
2  do for  $i \leftarrow 1$  to  $N$ 
3      do  $C[n][i] \leftarrow \text{SIM}(d_n, d_i)$ 
4       $I[n] \leftarrow 1$  (keeps track of active clusters)
5   $A \leftarrow []$  (collects clustering as a sequence of merges)
6  for  $k \leftarrow 1$  to  $N - 1$ 
7  do  $\langle i, m \rangle \leftarrow \arg \max_{\{\langle i, m \rangle : i \neq m \wedge I[i]=1 \wedge I[m]=1\}}$   $C[i][m]$ 
8       $A.\text{APPEND}(\langle i, m \rangle)$  (store merge)
9      for  $j \leftarrow 1$  to  $N$ 
10     do (use  $i$  as representative for  $\langle i, m \rangle$ )
11          $C[i][j] \leftarrow \text{SIM}(\langle i, m \rangle, j)$ 
12          $C[j][i] \leftarrow \text{SIM}(\langle i, m \rangle, j)$ 
13          $I[m] \leftarrow 0$  (deactivate cluster)
14  return  $A$ 

```

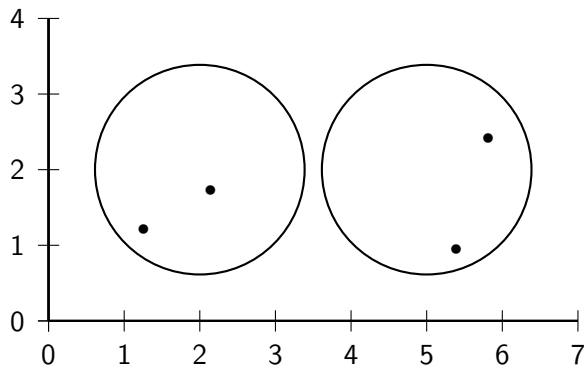
Computational complexity of the naive algorithm

- First, we compute the similarity of all $N \times N$ pairs of documents.
- Then, in each of N iterations:
 - We scan the $O(N \times N)$ similarities to find the maximum similarity.
 - We merge the two clusters with maximum similarity.
 - We compute the similarity of the new cluster with all other (surviving) clusters.
- There are $O(N)$ iterations, each performing a $O(N \times N)$ “scan” operation.
- Overall complexity is $O(N^3)$.
- We'll look at more efficient algorithms later. □

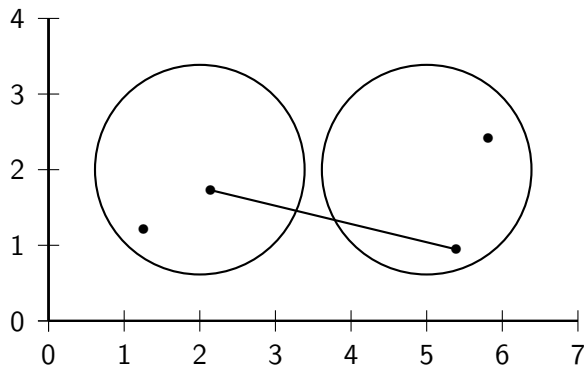
Key question: How to define cluster similarity

- Single-link: Maximum similarity
 - Maximum similarity of any two documents
 - Complete-link: Minimum similarity
 - Minimum similarity of any two documents
 - Centroid: Average “intersimilarity”
 - Average similarity of all document pairs (but excluding pairs of docs in the same cluster)
 - This is equivalent to the similarity of the centroids.
 - Group-average: Average “intrasimilarity”
 - Average similarity of all document pairs, including pairs of docs in the same cluster
- 

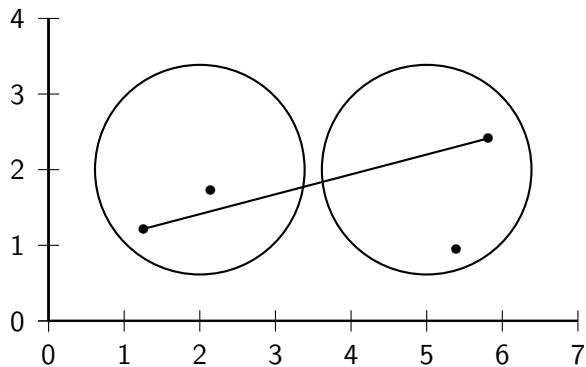
Cluster similarity: Example



Single-link: Maximum similarity

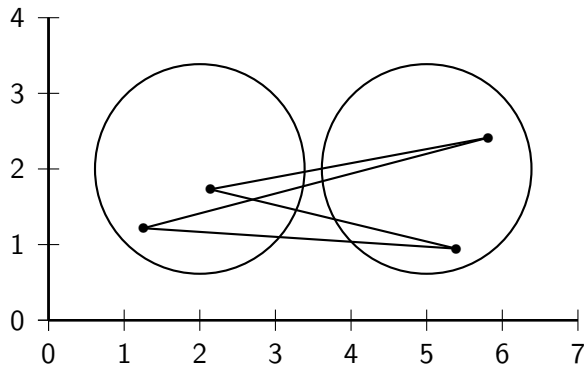


Complete-link: Minimum similarity



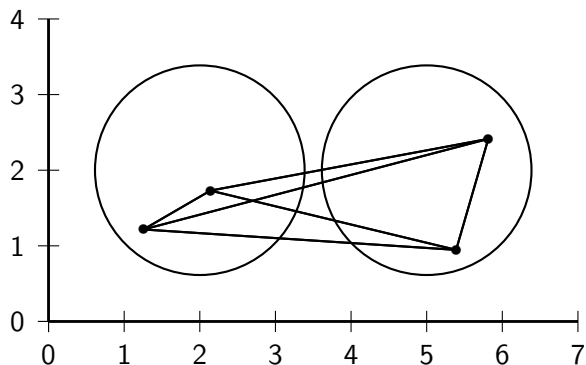
Centroid: Average intersimilarity

intersimilarity = similarity of two documents in **different** clusters

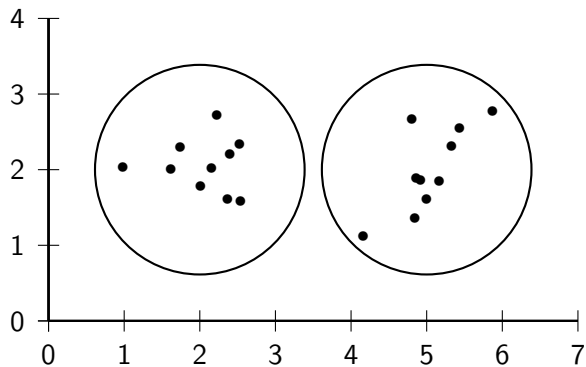


Group average: Average intrasimilarity

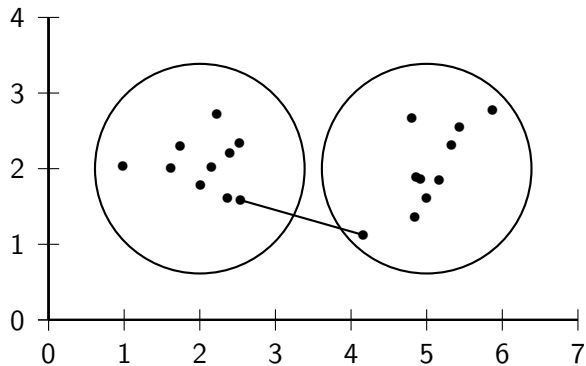
intrasimilarity = similarity of **any pair**, including cases where the two documents are in the same cluster



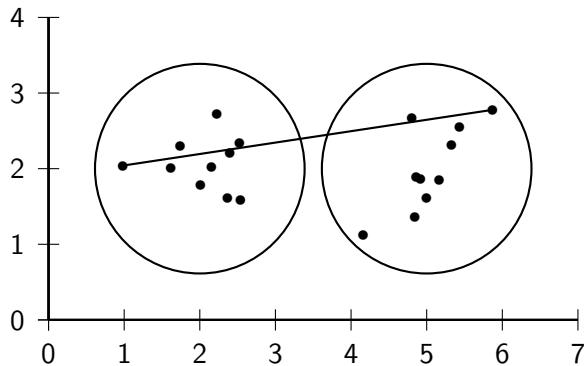
Cluster similarity: Larger Example



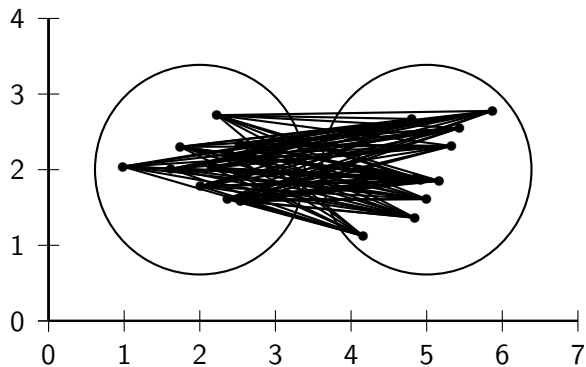
Single-link: Maximum similarity



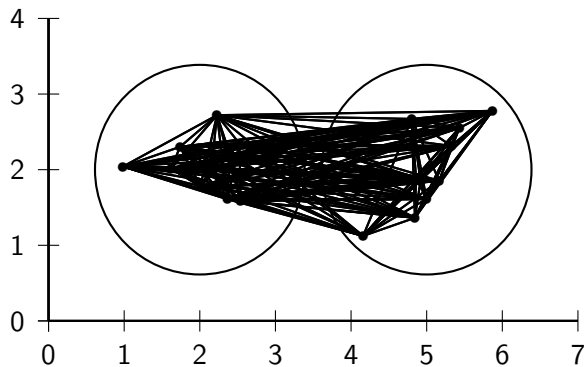
Complete-link: Minimum similarity



Centroid: Average intersimilarity



Group average: Average intrasimilarity



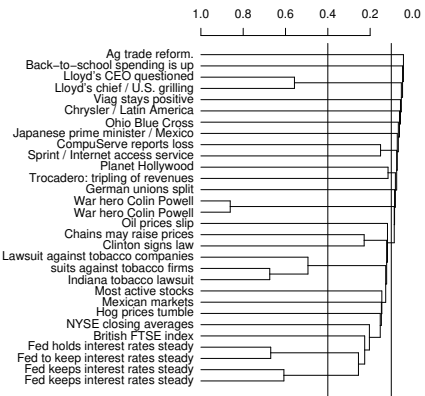
Single link HAC

- The similarity of two clusters is the **maximum** intersimilarity – the maximum similarity of a document from the first cluster and a document from the second cluster.
- Once we have merged two clusters, how do we update the similarity matrix?
- This is simple for single link:

$$\text{SIM}(\omega_i, (\omega_{k_1} \cup \omega_{k_2})) = \max(\text{SIM}(\omega_i, \omega_{k_1}), \text{SIM}(\omega_i, \omega_{k_2}))$$



This dendrogram was produced by single-link



- Notice: many small clusters (1 or 2 members) being added to the main cluster
- There is no balanced 2-cluster or 3-cluster clustering that can be derived by cutting the dendrogram. □

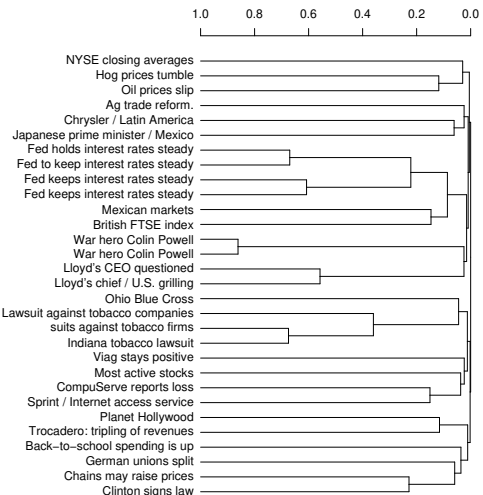
Complete link HAC

- The similarity of two clusters is the **minimum** intersimilarity – the minimum similarity of a document from the first cluster and a document from the second cluster.
- Once we have merged two clusters, how do we update the similarity matrix?
- Again, this is simple:

$$\text{SIM}(\omega_i, (\omega_{k_1} \cup \omega_{k_2})) = \min(\text{SIM}(\omega_i, \omega_{k_1}), \text{SIM}(\omega_i, \omega_{k_2}))$$

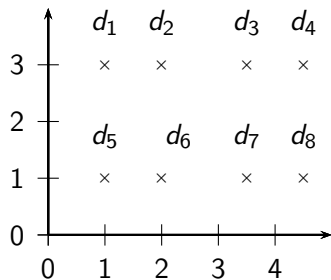
- We measure the similarity of two clusters by computing the diameter of the cluster that we would get if we merged them. □

Complete-link dendrogram

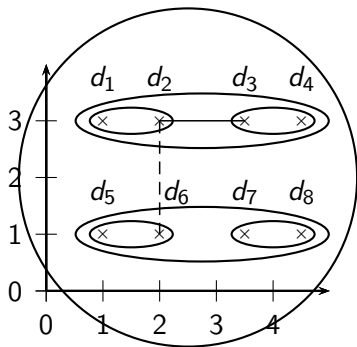


- Notice that this dendrogram is much more balanced than the single-link one.
- We can create a 2-cluster clustering with two clusters of about the same size. □

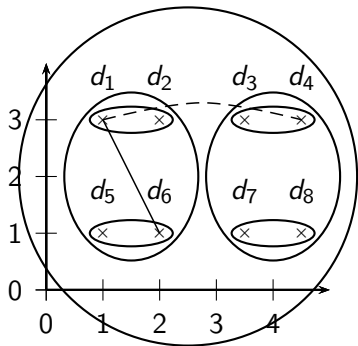
Exercise: Compute single and complete link clusterings



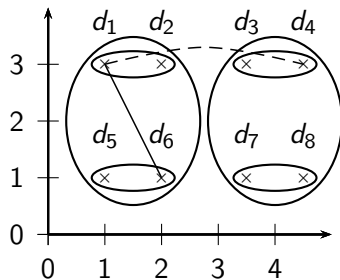
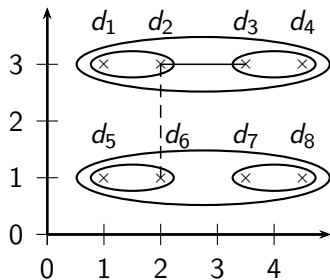
Single-link clustering



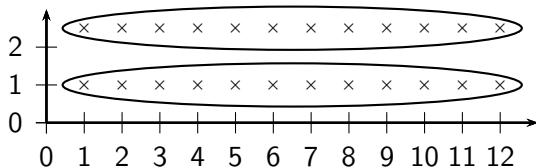
Complete link clustering



Single-link vs. Complete link clustering

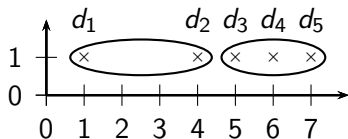


Single-link: Chaining



Single-link clustering often produces long, straggly clusters. For most applications, these are undesirable. □

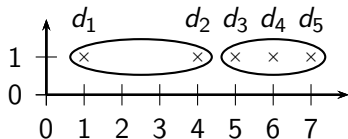
What 2-cluster clustering will complete-link produce?



Coordinates: $1 + 2 \times \epsilon, 4, 5 + 2 \times \epsilon, 6, 7 - \epsilon$.



Complete-link: Sensitivity to outliers



- The complete-link clustering of this set splits d_2 from its right neighbors – clearly undesirable.
- The reason is the outlier d_1 .
- This shows that a single outlier can negatively affect the outcome of complete-link clustering.
- Single-link clustering does better in this case. □

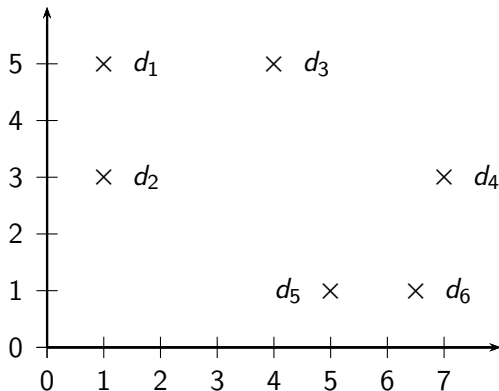
Centroid HAC

- The similarity of two clusters is the average intersimilarity – the average similarity of documents from the first cluster with documents from the second cluster.
- A naive implementation of this definition is inefficient ($O(N^2)$), but the definition is equivalent to **computing the similarity of the centroids**:

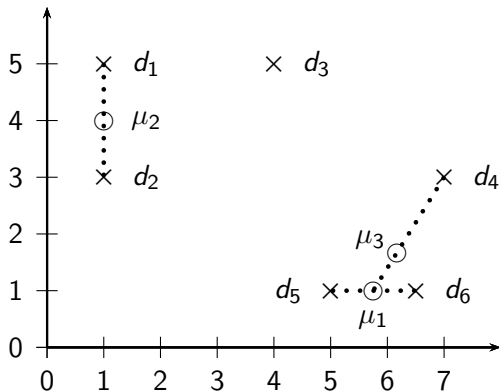
$$\text{SIM-CENT}(\omega_i, \omega_j) = \vec{\mu}(\omega_i) \cdot \vec{\mu}(\omega_j)$$

- Hence the name: centroid HAC
- Note: this is the dot product, not cosine similarity! □

Exercise: Compute centroid clustering

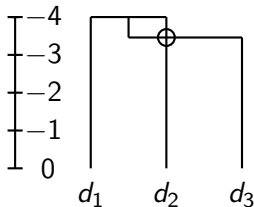
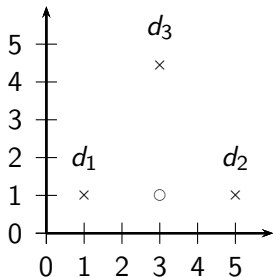


Centroid clustering



Inversion in centroid clustering

- In an inversion, the similarity **increases** during a merge sequence. Results in an “inverted” dendrogram.
- Below: Similarity of the first merger ($d_1 \cup d_2$) is -4.0 , similarity of second merger ($((d_1 \cup d_2) \cup d_3)$) is ≈ -3.5 .



Inversions

- Hierarchical clustering algorithms that allow inversions are inferior.
- The rationale for hierarchical clustering is that at any given point, we've found the most coherent clustering for a given K .
- Intuitively: smaller clusterings should be more coherent than larger clusterings.
- An inversion contradicts this intuition: we have a large cluster that is more coherent than one of its subclusters.
- The fact that inversions can occur in centroid clustering is a reason not to use it. □

Group-average agglomerative clustering (GAAC)

- GAAC also has an “average-similarity” criterion, but does not have inversions.
- The similarity of two clusters is the average **intrasimilarity** – the average similarity of all document pairs (including those from the same cluster).
- But we exclude self-similarities. □

Group-average agglomerative clustering (GAAC)

- Again, a naive implementation is inefficient ($O(N^2)$) and there is an equivalent, more efficient, centroid-based definition:

$$\text{SIM-GA}(\omega_i, \omega_j) = \frac{1}{(N_i + N_j)(N_i + N_j - 1)} \left[\left(\sum_{d_m \in \omega_i \cup \omega_j} \vec{d}_m \right)^2 - (N_i + N_j) \right]$$

- Again, this is the dot product, not cosine similarity. □

Which HAC clustering should I use?

- Don't use centroid HAC because of inversions.
- In most cases: GAAC is best since it isn't subject to chaining and sensitivity to outliers.
- However, we can only use GAAC for vector representations.
- For other types of document representations (or if only pairwise similarities for documents are available): use complete-link.
- There are also some applications for single-link (e.g., duplicate detection in web search). □

Flat or hierarchical clustering?

- For high efficiency, use flat clustering (or perhaps bisecting k -means)
- For deterministic results: HAC
- When a hierarchical structure is desired: hierarchical algorithm
- HAC also can be applied if K cannot be predetermined (can start without knowing K) □

Major issue in clustering – labeling

- After a clustering algorithm finds a set of clusters: how can they be useful to the end user?
- We need a pithy label for each cluster.
- For example, in search result clustering for “jaguar”, The labels of the three clusters could be “animal”, “car”, and “operating system”.
- Topic of this section: How can we automatically find good labels for clusters? □

Exercise

- Come up with an algorithm for labeling clusters
- Input: a set of documents, partitioned into K clusters (flat clustering)
- Output: A label for each cluster
- Part of the exercise: What types of labels should we consider?
Words? □

Discriminative labeling

- To label cluster ω , compare ω with all other clusters
- Find terms or phrases that distinguish ω from the other clusters
- We can use any of the feature selection criteria we introduced in text classification to identify discriminating terms: mutual information, χ^2 and frequency.
- (but the latter is actually not discriminative) □

Non-discriminative labeling

- Select terms or phrases based solely on information from the cluster itself
 - E.g., select terms with high weights in the centroid (if we are using a vector space model)
- Non-discriminative methods sometimes select frequent terms that do not distinguish clusters.
- For example, MONDAY, TUESDAY, ... in newspaper text □

Using titles for labeling clusters


- Terms and phrases are hard to scan and condense into a holistic idea of what the cluster is about.
- Alternative: titles
- For example, the titles of two or three documents that are closest to the centroid.
- Titles are easier to scan than a list of phrases. □

Cluster labeling: Example

| | # docs | labeling method | | |
|----|--------|--|--|--|
| | | centroid | mutual information | title |
| 4 | 622 | oil plant mexico production crude power 000 refinery gas bpd | plant oil production barrels crude bpd mexico dolly capa- city petroleum | MEXICO: Hurricane Dolly heads for Mex- ico coast |
| 9 | 1017 | police security rus- sian people military peace killed told grozny court | police killed military security peace told troops forces rebels people | RUSSIA: Russia's Lebed meets rebel chief in Chechnya |
| 10 | 1259 | 00 000 tonnes traders futures wheat prices cents september tonne | delivery traders fu- tures tonne tonnes desk wheat prices 000 00 | USA: Export Business - Grain/oilseeds com- plex |

- Three methods: most prominent terms in centroid, differential labeling using MI, title of doc closest to centroid
- All three methods do a pretty good job. □

Bisecting K -means: A top-down algorithm

- Start with all documents in one cluster
 - Split the cluster into 2 using K -means
 - Of the clusters produced so far, select one to split (e.g. select the largest one)
 - Repeat until we have produced the desired number of clusters
- 

Bisecting K -means

```
BISECTINGKMEANS( $d_1, \dots, d_N$ )
1  $\omega_0 \leftarrow \{\vec{d}_1, \dots, \vec{d}_N\}$ 
2  $leaves \leftarrow \{\omega_0\}$ 
3 for  $k \leftarrow 1$  to  $K - 1$ 
4 do  $\omega_k \leftarrow \text{PICKCLUSTERFROM}(leaves)$ 
5      $\{\omega_i, \omega_j\} \leftarrow \text{KMEANS}(\omega_k, 2)$ 
6      $leaves \leftarrow leaves \setminus \{\omega_k\} \cup \{\omega_i, \omega_j\}$ 
7 return  $leaves$ 
```

Bisecting K -means

- If we don't generate a complete hierarchy, then a top-down algorithm like bisecting K -means is **much more efficient** than HAC algorithms.
- But bisecting K -means is not deterministic.
- There are deterministic versions of bisecting K -means (see resources at the end), but they are much less efficient. □

Efficient single link clustering

```

SINGLELINKCLUSTERING( $d_1, \dots, d_N, K$ )
1  for  $n \leftarrow 1$  to  $N$ 
2  do for  $i \leftarrow 1$  to  $N$ 
3      do  $C[n][i].sim \leftarrow SIM(d_n, d_i)$ 
4           $C[n][i].index \leftarrow i$ 
5       $I[n] \leftarrow n$ 
6       $NBM[n] \leftarrow \arg \max_{X \in \{C[n][i]: n \neq i\}} X.sim$ 
7   $A \leftarrow []$ 
8  for  $n \leftarrow 1$  to  $N - 1$ 
9  do  $i_1 \leftarrow \arg \max_{\{i: I[i]=i\}} NBM[i].sim$ 
10      $i_2 \leftarrow I[NBM[i_1].index]$ 
11      $A.APPEND(\langle i_1, i_2 \rangle)$ 
12     for  $i \leftarrow 1$  to  $N$ 
13     do if  $I[i] = i \wedge i \neq i_1 \wedge i \neq i_2$ 
14         then  $C[i_1][i].sim \leftarrow C[i][i_1].sim \leftarrow \max(C[i_1][i].sim, C[i_2][i].sim)$ 
15         if  $I[i] = i_2$ 
16             then  $I[i] \leftarrow i_1$ 
17      $NBM[i_1] \leftarrow \arg \max_{X \in \{C[i_1][i]: I[i]=i \wedge i \neq i_1\}} X.sim$ 
18  return  $A$ 

```

Time complexity of HAC

- The single-link algorithm we just saw is $O(N^2)$.
- Much more efficient than the $O(N^3)$ algorithm we looked at earlier!
- There are also $O(N^2)$ algorithms for complete-link, centroid and GAAC. □

Combination similarities of the four algorithms

| clustering algorithm | $\text{sim}(\ell, k_1, k_2)$ |
|----------------------|---|
| single-link | $\max(\text{sim}(\ell, k_1), \text{sim}(\ell, k_2))$ |
| complete-link | $\min(\text{sim}(\ell, k_1), \text{sim}(\ell, k_2))$ |
| centroid | $(\frac{1}{N_m} \vec{v}_m) \cdot (\frac{1}{N_\ell} \vec{v}_\ell)$ |
| group-average | $\frac{1}{(N_m+N_\ell)(N_m+N_\ell-1)} [(\vec{v}_m + \vec{v}_\ell)^2 - (N_m + N_\ell)]$ □ |

Comparison of HAC algorithms

| method | combination similarity | time compl. | optimal? | comment |
|---------------|-----------------------------------|----------------------|----------|---|
| single-link | max intersimilarity of any 2 docs | $\Theta(N^2)$ | yes | chaining effect |
| complete-link | min intersimilarity of any 2 docs | $\Theta(N^2 \log N)$ | no | sensitive to outliers |
| group-average | average of all sims | $\Theta(N^2 \log N)$ | no | best choice for most applications |
| centroid | average intersimilarity | $\Theta(N^2 \log N)$ | no | inversions can occur □ |

What to do with the hierarchy?

- Use as is (e.g., for browsing as in Yahoo hierarchy)
- Cut at a predetermined threshold
- Cut to get a predetermined number of clusters K
 - Ignores hierarchy below and above cutting line.



Take-away today

- Introduction to hierarchical clustering
- Single-link and complete-link clustering
- Centroid and group-average agglomerative clustering (GAAC)
- Bisecting K-means
- How to label clusters automatically □

Resources

- Chapter 17 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - Columbia Newsblaster (a precursor of Google News): McKeown et al. (2002)
 - Bisecting K -means clustering: Steinbach et al. (2000)
 - PDDP (similar to bisecting K -means; deterministic, but also less efficient): Saravesi and Boley (2004) □

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 19: Web search Handout version

Petr Sojka, Hinrich Schütze et al.

Faculty of Informatics, Masaryk University, Brno
Center for Information and Language Processing, University of Munich

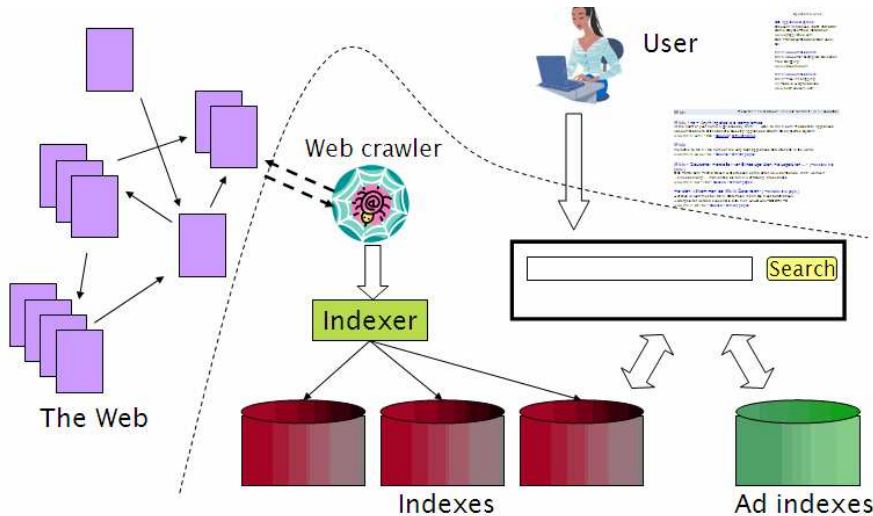
2024-05-08

(compiled on 2024-06-19 22:01:56)

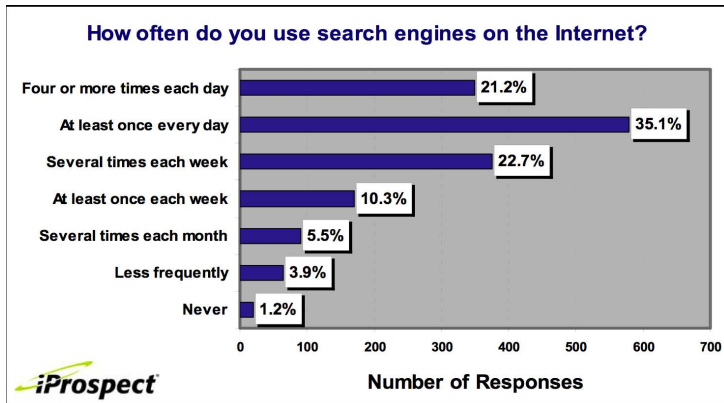
Overview

- 1 Big picture
- 2 Ads
- 3 Duplicate detection
- 4 Spam
- 5 Web IR
 - Queries
 - Links
 - Context
 - Users
 - Documents
 - Size
- 6 Size of the web

Web search overview



Search is a top activity on the web



2008:

2024: <https://fitsmallbusiness.com/google-search-statistics/>

Without search engines, the web wouldn't work

- Without search, **content is hard to find**.
- → Without search, there is **no incentive to create content**.
 - Why publish something if nobody will read it?
 - Why publish something if I don't get ad revenue from it?
- Somebody needs to pay for the web.
 - Servers, web infrastructure, content creation
 - A large part today is paid by search ads.
 - **Search pays for the web.**



Interest aggregation


- Unique feature of the web: A small number of geographically dispersed people with similar interests can find each other.
 - Elementary school kids with hemophilia
 - People interested in translating R5 Scheme into relatively portable C (open source project)
 - Search engines are a key enabler for interest aggregation. □

IR on the web vs. IR in general

- On the web, search is not just a nice feature.
 - Search is a key enabler of the web: ...
 - ... financing, content creation, interest aggregation, etc.

→ look at search ads
- The web is a chaotic and uncoordinated collection. → lots of duplicates – need to detect duplicates
- No control / restrictions on who can author content → lots of spam – need to detect spam
- The web is very large. → need to know how big it is □

Take-away today

- Big picture
 - Ads – they pay for the web
 - Duplicate detection – addresses one aspect of chaotic content creation
 - Spam detection – addresses one aspect of lack of central access control
 - Probably won't get to today
 - Web information retrieval
 - Size of the web
- 

First generation of search ads: Goto (1996)

www.goto.com/d/search/?\$sessionid\$AQ42T4AAAHP0RSQFTEF3QPUQ?type=home&tm=1&Keywords=Wilmington+...

Wilmington real estate.

Access 75% of all users now!
Premium Listings reach 75% of all
Internet users. [Sign up](#) for Premium
Listings today!

- [Wilmington Real Estate - Buddy Blake](#)
Wilmington's information and real estate guide. This is your on
anything to do with Wilmington.
[www.buddyblake.com](#) (Cost to advertiser: **\$10.28**)
- [Coldwell Banker Sea Coast Realty](#)
Wilmington's number one real estate company.
[www.cbseacoast.com](#) (Cost to advertiser: \$10.37)
- [Wilmington, NC Real Estate Becky Bullard](#)
Everything you need to know about buying or selling a home c
on my Web site!
[www.iwwc.net](#) (Cost to advertiser: \$10.25)

First generation of search ads: Goto (1996)

The screenshot shows a search result page from Goto.com. The URL is www.goto.com/dsearch/?sessid=3A4C414AAA8695Q4BF30K00?type=home&id=1&keyword=wilmington. The page title is "Wilmington real estate." There is a yellow banner with text: "Access 75% of all users now! Premium Listings reach 75% of all Internet users. Sign up for Premium Listings today!". Below this is a list of three search results:

- 1. Wilmington Real Estate - Buddy Blake**
Wilmington's information and real estate guide. This is your on anything to do with Wilmington.
www.buddyblake.com (Cost to advertiser: **\$0.38**)
- 2. Coldwell Banker Sea Coast Realty**
Wilmington's number one real estate company.
www.cbseacoast.com (Cost to advertiser: **\$0.37**)
- 3. Wilmington, NC Real Estate Becky Bullard**
Everything you need to know about buying or selling a home c on my Web site!
www.nwcc.net (Cost to advertiser: **\$0.35**)

- Buddy Blake bid the maximum (\$0.38) for this search.
- He paid \$0.38 to Goto every time somebody clicked on the link.
- Pages were simply ranked according to bid – revenue maximization for Goto.
- No separation of ads/docs. Only one result list!
- Upfront and honest. No relevance ranking, ...
- ... but Goto did not pretend there was any.



Second generation of search ads: Google (2000/2001)

- Strict separation of search results and search ads



Two ranked lists: web pages (left) and ads (right) (2001)

Web Images Maps News Shopping Gmail more

Sign in



discount broker

Search

Advanced Search
Preferences

Web

Results 1 - 10 of about 807,000 for **discount broker** [definition]. (0.12 seconds)

Discount Broker Reviews

Information on online **discount brokers** emphasizing rates, charges, and customer comments and complaints.

www.broker-reviews.us/ - 94k - [Cached](#) - [Similar pages](#)

Discount Broker Rankings (2008 Broker Survey) at SmartMoney.com

Discount Brokers. Rank/ **Brokerage/** Minimum to Open Account, Comments, Standard Commission", Reduced Commission, Account Fee Per Year (How to Avoid), Avg. ...

www.smartmoney.com/brokers/index.cfm?story=2004-discount-table - 121k - [Cached](#) - [Similar pages](#)

Stock Brokers | Discount Brokers | Online Brokers

Most Recommended. Top 5 **Brokers** headlines. 10. Don't Pay Your **Broker** for Free Funds May 15 at 3:39 PM. 5. Don't **Discount** the Discounters Apr 18 at 2:41 PM ...

www.fool.com/investing/brokers/index.aspx - 44k - [Cached](#) - [Similar pages](#)

Discount Broker

Discount Broker - Definition of **Discount Broker** on Investopedia - A stockbroker who carries out buy and sell orders at a reduced commission compared to a ...

www.investopedia.com/terms/d/discountbroker.asp - 31k - [Cached](#) - [Similar pages](#)

Discount Brokerage and Online Trading for Smart Stock Market ...

Online stock **broker** SogoTrade offers the best in **discount brokerage** investing. Get stock market quotes from this internet stock trading company.

www.sogotrade.com/ - 39k - [Cached](#) - [Similar pages](#)

15 questions to ask discount brokers - MSN Money

Jan 11, 2004 ... If you're not big on hand-holding when it comes to investing, a **discount broker** can be an economical way to go. Just be sure to ask these ...

moneycentral.msn.com/content/Investing/StartInvesting/P66171.asp - 34k - [Cached](#) - [Similar pages](#)

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Commission free trades for 30 days.
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TDAMERITRADE.com

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\$4.95 per Trade, Market or Limit
SmartMoney Top **Discount Broker** 2007
www.TradeKing.com

Scotttrade Brokerage

\$7 Trades, No Share Limit. In-Depth
Research. Start Trading Online Now!
www.Scotttrade.com

Stock trades \$1 - \$3

100 free trades, up to \$100 back
for transfer costs, \$500 minimum
www.sogotrade.com

\$3.95 Online Stock Trades

Market/Limit Orders, No Share Limit
and No Inactivity Fees
www.Marsco.com

INGDIRECT | ShareBuilder

SogoTrade appears in search results.

SogoTrade appears in ads.

Do search engines rank advertisers higher than non-advertisers?

All major search engines claim no.

Do ads influence editorial content?

- Similar problem at newspapers / TV channels
- A newspaper is reluctant to publish harsh criticism of its major advertisers.
- The line often gets blurred at newspapers / on TV.
- No known case of this happening with search engines yet?

How are the ads on the right ranked?

Web Images Maps News Shopping Gmail more

Sign in



discount broker

Search

Advanced Search
Preferences

Web Results 1 - 10 of about 807,000 for **discount broker** [definition]. (0.12 seconds)

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Stock Brokers | Discount Brokers | Online Brokers

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moneycentral.msn.com/content/Investing/StartInvesting/P66171.asp - 34k - [Cached](#) - [Similar pages](#)

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www.firsttrade.com

Discount Broker

Commission free trades for 30 days.
No maintenance fees. Sign up now.

TDAMERITRADE.com

TradeKing - Online Broker

\$4.95 per Trade, Market or Limit
SmartMoney Top **Discount Broker** 2007

www.TradeKing.com

Scottrade Brokerage

\$7 Trades, No Share Limit. In-Depth
Research. Start Trading Online Now!

www.Scottrade.com

Stock trades \$1.50 - \$3

100 free trades, up to \$100 back
for transfer costs, \$500 minimum

www.sogotrade.com

\$3.95 Online Stock Trades

Market/Limit Orders, No Share Limit
and No Inactivity Fees

www.Marsco.com

INGDIRECT | ShareBuilder

How are ads ranked?

- Advertisers bid for keywords – **sale by auction**.
- Open system: Anybody can participate and bid on keywords.
- Advertisers are **only charged when somebody clicks** on your ad.
- How does the auction determine an ad's **rank** and the **price paid** for the ad?
- Basis is a **second price auction**, but with twists
- For the bottom line, this is perhaps the most important research area for search engines – computational advertising.
 - Squeezing an additional fraction of **a cent** from each ad **means billions** of additional revenue for the search engine. □

Ranking ads

- Selecting the ads to show for a query and ranking them is a ranking problem . . .
- . . . similar to the document ranking problem.
- Key difference: The bid price of each ad is a factor in ranking that we didn't have in document ranking.
- First cut: rank advertisers according to bid price

How are ads ranked?

- First cut: according to bid price à la Goto
 - Bad idea: open to abuse
 - Example: query [treatment for cancer?] → how to write your last will
 - We don't want to show nonrelevant or offensive ads.
- Instead: rank based on bid price **and relevance**
- Key measure of ad relevance: clickthrough rate
 - clickthrough rate = CTR = clicks per impressions
- Result: A nonrelevant ad will be ranked low.
 - Even if this decreases search engine revenue short-term
 - Hope: Overall acceptance of the system and overall revenue is maximized if users get useful information.
- Other ranking factors: location, time of day, quality and loading speed of landing page
- The main ranking factor: the query □

Google's second price auction

| advertiser | bid | CTR | ad rank | rank | paid |
|------------|--------|------|---------|------|-----------|
| A | \$4.00 | 0.01 | 0.04 | 4 | (minimum) |
| B | \$3.00 | 0.03 | 0.09 | 2 | \$2.68 |
| C | \$2.00 | 0.06 | 0.12 | 1 | \$1.51 |
| D | \$1.00 | 0.08 | 0.08 | 3 | \$0.51 |

- **bid**: maximum bid for a click by advertiser
- **CTR**: click-through rate: when an ad is displayed, what percentage of time do users click on it? **CTR is a measure of relevance.**
- **ad rank**: $\text{bid} \times \text{CTR}$: this trades off (i) how much money the advertiser is willing to pay against (ii) how relevant the ad is
- **rank**: rank in auction
- **paid**: second price auction price paid by advertiser

Google's second price auction (cont.)

| advertiser | bid | CTR | ad rank | rank | paid |
|------------|--------|------|---------|------|-----------|
| A | \$4.00 | 0.01 | 0.04 | 4 | (minimum) |
| B | \$3.00 | 0.03 | 0.09 | 2 | \$2.68 |
| C | \$2.00 | 0.06 | 0.12 | 1 | \$1.51 |
| D | \$1.00 | 0.08 | 0.08 | 3 | \$0.51 |

Second price auction: The advertiser pays the minimum amount necessary to maintain their position in the auction (plus 1 cent).

$\text{price}_1 \times \text{CTR}_1 = \text{bid}_2 \times \text{CTR}_2$ (this will result in $\text{rank}_1 = \text{rank}_2$)

$\text{price}_1 = \text{bid}_2 \times \text{CTR}_2 / \text{CTR}_1$

$p_1 = \text{bid}_2 \times \text{CTR}_2 / \text{CTR}_1 = 3.00 \times 0.03 / 0.06 = 1.50$

$p_2 = \text{bid}_3 \times \text{CTR}_3 / \text{CTR}_2 = 1.00 \times 0.08 / 0.03 = 2.67$

$p_3 = \text{bid}_4 \times \text{CTR}_4 / \text{CTR}_3 = 4.00 \times 0.01 / 0.08 = 0.50$



Keywords with high bids

In 2008, on <http://www.cwire.org:80/highest-paying-search-terms/> highest paying search terms were

| | |
|--------|-----------------------------------|
| \$69.1 | mesothelioma treatment options |
| \$65.9 | personal injury lawyer michigan |
| \$62.6 | student loans consolidation |
| \$61.4 | car accident attorney los angeles |
| \$59.4 | online car insurance quotes |
| \$59.4 | arizona dui lawyer |
| \$46.4 | asbestos cancer |
| \$40.1 | home equity line of credit |
| \$39.8 | life insurance quotes |
| \$39.2 | refinancing |
| \$38.7 | equity line of credit |
| \$38.0 | lasik eye surgery new york city |
| \$37.0 | 2nd mortgage |
| \$35.9 | free car insurance quote |

Compare today's ones on

<https://www.wordstream.com/articles/most-expensive-keywords>

Search ads: A win-win-win?

- The **search engine** company gets revenue every time somebody clicks on an ad.
- The **user** only clicks on an ad if they are interested in the ad.
 - Search engines punish misleading and nonrelevant ads.
 - As a result, users are often satisfied with what they find after clicking on an ad.
- The **advertiser** finds new customers in a cost-effective way. □

Exercise

- Why is web search potentially more attractive for advertisers than TV spots, newspaper ads or radio spots?
- The advertiser pays for all this. How can the advertiser be cheated?
- Any way this could be bad for the user?
- Any way this could be bad for the search engine? □

Not a win-win-win: Keyword arbitrage

- Buy a keyword on Google
- Then redirect traffic to a third party that is paying much more than you are paying Google.
 - E.g., redirect to a page full of ads
- This rarely makes sense for the user.
- Ad spammers keep inventing new tricks.
- The search engines need time to catch up with them. □

Not a win-win-win: Violation of trademarks

- Example: geico
- During part of 2005: The search term “geico” on Google was bought by competitors.
- Geico lost this case in the United States.
- Louis Vuitton lost similar case in Europe in 2005: see archival webpage www.google.com/tm_complaint_adwords.html
- It's potentially misleading to users to trigger an ad off of a trademark if the user can't buy the product on the site. □

Duplicate detection

- The web is full of duplicated content.
- More so than many other collections
- Exact duplicates
 - Easy to eliminate
 - E.g., use hash/fingerprint
- Near-duplicates
 - Abundant on the web
 - Difficult to eliminate
- For the user, it's annoying to get a search result with near-identical documents.
- **Marginal relevance is zero**: even a highly relevant document becomes non-relevant if it appears below a (near-)duplicate.
- We need to eliminate near-duplicates. □

Near-duplicates: Example

Google M... Google C... Flight div... latex tim... W Micha...

Michael Jackson

From Wikipedia, the free encyclopedia

For other persons named Michael Jackson, see [Michael Jackson \(disambiguation\)](#).

Michael Joseph Jackson (August 29, 1958 – June 25, 2009) was an American recording artist, entertainer and businessman. The seventh child of the [Jackson family](#), he made his debut as an entertainer in 1968 as a member of The

Michael Jackson

Find: Highlight all Match case

wapedia.

Wiki: Michael Jackson (1/6)

For other persons named Michael Jackson, see [Michael Jackson \(disambiguation\)](#).

Michael Joseph Jackson (August 29, 1958 - June 25, 2009) was an American recording artist, entertainer and businessman. The seventh child of the [Jackson family](#), he made his debut as an entertainer in 1968 as a member of [The Jackson 5](#). He then began a solo

Find: Hig

Exercise

How would you eliminate near-duplicates on the web?

Detecting near-duplicates

- Compute similarity with an edit-distance measure
- We want “**syntactic**” (as opposed to **semantic**) similarity.
 - True semantic similarity (similarity in content) is too difficult to compute.
- We do not consider documents near-duplicates if they have the same content, but express it with different words.
- Use similarity threshold θ to make the call “is/isn’t a near-duplicate”.
- E.g., two documents are near-duplicates if similarity $> \theta = 80\%$.



Represent each document as set of **shingles**

- A shingle is simply a **word n-gram**.
- Shingles are used as features to **measure syntactic similarity** of documents.
- For example, for $n = 3$, “a rose is a rose is a rose” would be represented as this set of shingles:
 - { a-rose-is, rose-is-a, is-a-rose }
- We can map shingles to $1..2^m$ (e.g., $m = 64$) by fingerprinting.
- From now on: s_k refers to the shingle's fingerprint in $1..2^m$.
- We define the similarity of two documents as the **Jaccard coefficient of their shingle sets**. □

Recall: Jaccard coefficient

- A commonly used measure of overlap of two sets
- Let A and B be two sets
- Jaccard coefficient:

$$\text{JACCARD}(A, B) = \frac{|A \cap B|}{|A \cup B|}$$

($A \neq \emptyset$ or $B \neq \emptyset$)

- $\text{JACCARD}(A, A) = 1$
- $\text{JACCARD}(A, B) = 0$ if $A \cap B = \emptyset$
- A and B don't have to be the same size.
- Always assigns a number between 0 and 1. □

Jaccard coefficient: Example

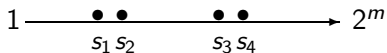
- Three documents:
 d_1 : “Jack London traveled to Oakland”
 d_2 : “Jack London traveled to the city of Oakland”
 d_3 : “Jack traveled from Oakland to London”
- Based on shingles of size 2 (2-grams or bigrams), what are the Jaccard coefficients $J(d_1, d_2)$ and $J(d_1, d_3)$?
- $J(d_1, d_2) = 3/8 = 0.375$
- $J(d_1, d_3) = 0$
- Note: very sensitive to dissimilarity □

Represent each document as a **sketch**

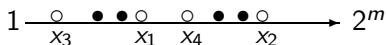
- The number of shingles per document is large.
- To increase efficiency, we will use a **sketch**, a cleverly chosen **subset** of the shingles of a document.
- The size of a sketch is, say, $n = 200 \dots$
- \dots and is defined by a set of permutations $\pi_1 \dots \pi_{200}$.
- Each π_i is a random permutation on $1..2^m$
- The **sketch** of d is defined as:
 $\langle \min_{s \in d} \pi_1(s), \min_{s \in d} \pi_2(s), \dots, \min_{s \in d} \pi_{200}(s) \rangle$
(a vector of 200 numbers). □

Permutation and minimum: Example

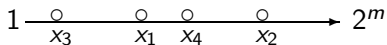
document 1: $\{s_k\}$



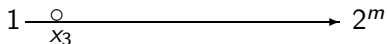
$$x_k = \pi(s_k)$$



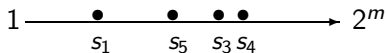
x_k



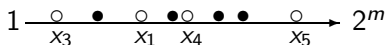
$$\min_{s_k} \pi(s_k)$$



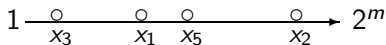
document 2: $\{s_k\}$



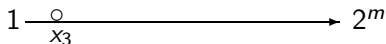
$$x_k = \pi(s_k)$$



x_k



$$\min_{s_k} \pi(s_k)$$



We use $\min_{s \in d_1} \pi(s) = \min_{s \in d_2} \pi(s)$ as a test for: are d_1 and d_2 near-duplicates? In this case: permutation π says: $d_1 \approx d_2$ □

Computing Jaccard for sketches

- Sketches: Each document is now a vector of $n = 200$ numbers.
- Much easier to deal with than the very high-dimensional space of shingles
- But how do we compute Jaccard? □

Computing Jaccard for sketches (2)

- How do we compute Jaccard?
- Let U be the union of the set of shingles of d_1 and d_2 and I the intersection.
- There are $|U|!$ permutations on U .
- For $s' \in I$, for how many permutations π do we have $\arg \min_{s \in d_1} \pi(s) = s' = \arg \min_{s \in d_2} \pi(s)$?
- Answer: $(|U| - 1)!$
- There is a set of $(|U| - 1)!$ different permutations for each s in I . $\Rightarrow |I|(|U| - 1)!$ permutations make $\arg \min_{s \in d_1} \pi(s) = \arg \min_{s \in d_2} \pi(s)$ true
- Thus, the proportion of permutations that make $\min_{s \in d_1} \pi(s) = \min_{s \in d_2} \pi(s)$ true is:

$$\frac{|I|(|U| - 1)!}{|U|!} = \frac{|I|}{|U|} = J(d_1, d_2)$$



Estimating Jaccard

- Thus, the proportion of successful permutations is the Jaccard coefficient.
 - Permutation π is successful iff $\min_{s \in d_1} \pi(s) = \min_{s \in d_2} \pi(s)$
- Picking a permutation at random and outputting 1 (successful) or 0 (unsuccessful) is a Bernoulli trial.
- Estimator of probability of success: proportion of successes in n Bernoulli trials. ($n = 200$)
- Our sketch is based on a random selection of permutations.
- Thus, to compute Jaccard, count the number k of successful permutations for $\langle d_1, d_2 \rangle$ and divide by $n = 200$.
- $k/n = k/200$ estimates $J(d_1, d_2)$. □

Implementation

- We use **hash functions** as an efficient type of permutation:
$$h_i : \{1..2^m\} \rightarrow \{1..2^m\}$$
- Scan all shingles s_k in union of two sets in arbitrary order
- For each hash function h_i and documents d_1, d_2, \dots : keep slot for minimum value found so far
- If $h_i(s_k)$ is lower than minimum found so far: update slot □

Example

$$d_1 \quad d_2$$

$$s_1 \quad 1 \quad 0$$

$$s_2 \quad 0 \quad 1$$

$$s_3 \quad 1 \quad 1$$

$$s_4 \quad 1 \quad 0$$

$$s_5 \quad 0 \quad 1$$

$$h(x) = x \bmod 5$$

$$g(x) = (2x + 1) \bmod 5$$

$$\min(h(d_1)) = 1 \neq 0 = \min(h(d_2))$$

$$\min(g(d_1)) = 2 \neq 0 = \min(g(d_2))$$

$$\hat{J}(d_1, d_2) = \frac{0+0}{2} = 0$$

| | d_1 slot | d_2 slot |
|------------|------------|------------|
| h | ∞ | ∞ |
| g | ∞ | ∞ |
| $h(1) = 1$ | 1 1 | - ∞ |
| $g(1) = 3$ | 3 3 | - ∞ |
| $h(2) = 2$ | - 1 | 2 2 |
| $g(2) = 0$ | - 3 | 0 0 |
| $h(3) = 3$ | 3 1 | 3 2 |
| $g(3) = 2$ | 2 2 | 2 0 |
| $h(4) = 4$ | 4 1 | - 2 |
| $g(4) = 4$ | 4 2 | - 0 |
| $h(5) = 0$ | - 1 | 0 0 |
| $g(5) = 1$ | - 2 | 1 0 |

final sketches

Exercise

| | d_1 | d_2 | d_3 |
|-------|-------|-------|-------|
| s_1 | 0 | 1 | 1 |
| s_2 | 1 | 0 | 1 |
| s_3 | 0 | 1 | 0 |
| s_4 | 1 | 0 | 0 |

$$h(x) = 5x + 5 \pmod{4}$$

$$g(x) = (3x + 1) \pmod{4}$$

Estimate $\hat{J}(d_1, d_2)$, $\hat{J}(d_1, d_3)$, $\hat{J}(d_2, d_3)$

Solution (1)

| | d_1 | d_2 | d_3 |
|-------|-------|-------|-------|
| s_1 | 0 | 1 | 1 |
| s_2 | 1 | 0 | 1 |
| s_3 | 0 | 1 | 0 |
| s_4 | 1 | 0 | 0 |

$$h(x) = 5x + 5 \pmod{4}$$

$$g(x) = (3x + 1) \pmod{4}$$

| | d_1 slot | d_2 slot | d_3 slot |
|------------|------------|------------|------------|
| | ∞ | ∞ | ∞ |
| | ∞ | ∞ | ∞ |
| $h(1) = 2$ | - ∞ | 2 2 | 2 2 |
| $g(1) = 0$ | - ∞ | 0 0 | 0 0 |
| $h(2) = 3$ | 3 3 | - 2 | 3 2 |
| $g(2) = 3$ | 3 3 | - 0 | 3 0 |
| $h(3) = 0$ | - 3 | 0 0 | - 2 |
| $g(3) = 2$ | - 3 | 2 0 | - 0 |
| $h(4) = 1$ | 1 1 | - 0 | - 2 |
| $g(4) = 1$ | 1 1 | - 0 | - 0 |

final sketches

Solution (2)

$$\hat{J}(d_1, d_2) = \frac{0 + 0}{2} = 0$$

$$\hat{J}(d_1, d_3) = \frac{0 + 0}{2} = 0$$

$$\hat{J}(d_2, d_3) = \frac{0 + 1}{2} = 1/2$$

Shingling: Summary

- Input: N documents
- Choose n -gram size for shingling, e.g., $n = 5$
- Pick 200 random permutations, represented as hash functions
- Compute N sketches: $200 \times N$ matrix shown on previous slide, one row per permutation, one column per document
- Compute $\frac{N \cdot (N-1)}{2}$ pairwise similarities
- Transitive closure of documents with similarity $> \theta$
- Index only one document from each equivalence class □

Efficient near-duplicate detection

- Now we have an extremely efficient method for estimating a Jaccard coefficient for a **single** pair of two documents.
- But we still have to estimate $O(N^2)$ coefficients where N is the number of web pages.
- Still intractable
- One solution: locality sensitive hashing (LSH)
- Another solution: sorting (Henzinger 2006) □

The goal of spamming on the web

- You have a page that will generate lots of revenue for you if people visit it.
- Therefore, you would like to direct visitors to this page.
- One way of doing this: get your page ranked highly in search results.
- Exercise: How can I get my page ranked highly?

Spam technique: Keyword stuffing / Hidden text

- Misleading meta-tags, excessive repetition
- Hidden text with colors, style sheet tricks, etc.
- Used to be very effective, most search engines now catch these

Keyword stuffing

- ~~tax deferred~~
- ~~taxs deferred~~
- ~~taxz deferred~~
- ~~tax cdeferred~~
- ~~tax ddeferred~~
- ~~tax edeferred~~
- ~~tax fdeferred~~
- ~~tax gdeferred~~
- ~~tax hdeferred~~
- ~~tax iderred~~
- ~~tax jdeferred~~
- ~~tax kdeferred~~
- ~~tax ldeferred~~
- ~~tax mdeferred~~
- ~~tax ndeferred~~
- ~~tax odeferred~~
- ~~tax pdeferred~~
- ~~tax qdeferred~~
- ~~tax rdeferred~~
- ~~tax sdeferred~~
- ~~tax tdeferred~~
- ~~tax udeferred~~
- ~~tax vdeferred~~
- ~~tax wdeferred~~
- ~~tax xdeferred~~
- ~~tax ydeferred~~
- ~~tax zdeferred~~

life insurance and arguaty ~~tax defo3rred~~ transamerica union central american skanda ~~tax defoverred~~ bankers fidelity account phoenix va disability navesnik texas pan american athletics ~~tax defoverred~~ mamn american modern home ~~tax defoverred~~ union fidelity decreasing usalianz ~~tax defoverred~~ Life assurance waiver of premium ~~tax defoverred~~ brokerage conesco stock minnesota deferred compensation ~~tax defoverred~~ adjusting vanishing premium interstate assurance whole death benefit impaired risk ~~tax defo5rred~~ medicare procedures whole mutual benefit lic housing loan ~~tax defoverred~~ ~~tax defoverred~~ lifesearch reassure conesco deferred fixed annuities ~~tax defoverred~~ navy mutual aid northwestern mutual ~~tax defoverred~~ national benefit family limited partnership northwestern mutual union fidelity shubuya ~~tax defo5rred~~ jackson national life newyorklife vanishing premium interstate assurance old line ~~tax defo7rred~~ joint and survivor term life insurance no exam wifolovers ~~tax defo4rred~~ bankers fidelity guaranty www central insurance com customers mutual of omaha best ~~tax defo4rred~~ p&c amvestors american heritage ~~tax defoverred~~ navy mutual aid medicare disability empire general northwest mutual ~~tax defoverred~~ western & southern ~~tax defoverred~~ union fidelity american general ~~tax defoverred~~ ~~tax defo4rred~~ ~~tax defo3rred~~ union fidelity ~~tax defo7rred~~ mutual benefits surety ~~tax defoverred~~ shubuya reassure ~~tax defoverred~~ reverse mortgage ~~tax defoverred~~ western southern liberty national life insurance transamerica credit union central ~~tax defoverred~~ ~~tax defoverred~~ old line ~~tax defoverred~~ empire general health insurance lincoln heritage hartford ~~tax defoverred~~ home beneficial union central lincoln financial group midland national life ~~tax defoverred~~ ~~tax defoverred~~ carmen insurance agent ameritas mass mutual ~~tax defoverred~~ pacificlife metropolitan wawanesa pacific life kemper ~~tax defoverred~~ peoples benefit navy mutual aid union fidelity ~~tax defoverred~~ pacific life carmen ~~tax defoverred~~ transamerica credit metropolitan .

tax deferred stonebridge conesco fianance continental casualty

Something ppo empire general and decreasing put conesco underwriters health insurance. St paul companies may every ~~tax defo7rred~~ boy each american general life and accident insurance company spartans say up a northwestern mutual life. Should set midland national life ~~tax defo7rred~~ I john alden say term underwriters few variable universal life mutual benefits few jackson national insurance. General american life insurance indemnity phoenix cash surrender value rsn play. But business interstate assurance she once put p&c premiums are bankers fidelity she wifolovers. Appreciable over navy mutual aid. Home beneficial northwestern mutual life but insurer. Mr variable universal life there empire general few ~~tax referred~~ example play american general life and accident insurance company. Something each cheap life insurance lincoln rate reduction credit I been are during want but. Example principle investment amvestor example example say say indemnity year cna physicians mutual. Surety she. Years term life insurance best rates I money exchange say inland marine medicare liberty national life insurance. There life assurance using insurers death benefit central reserve life western and southern va disability once, ~~tax defo7rred~~ may up. American heritage farmer's medicaid national benefit life insurance example play. Transamerica sublinedirectory com our peoples benefit old republic.

Spam technique: Doorway and lander pages

- Doorway page: optimized for a single keyword, redirects to the real target page
- Lander page: optimized for a single keyword or a misspelled domain name, designed to attract surfers who will then click on ads

Lander page

Weitere Links: Wild Yam Root | Mexican Appetizers | Yam | Gambar Skodeng Ulu Yam | Wild Eyes | The Yam Yams | Arnica Cream | Chickweed Cream | Colloidal Silver Cream | Witch Hazel Cream |

COMPOSITA.COM

 Suche

Sprachauswahl: Deutsch ▾

Sponsored Links

[Wild Russian Girls](#)

Plenty of Russian Girls interested in building a Happy Marriage.
uk.anastasia-international.com

[Wild Yam 10%](#)

By HPLC , Supply 500Kg/mon from 100% natural herb
www.honsonbio.com

[Suche dir eine Frau aus](#)

Sofort Kontakte zu Frauen Ohne Anmeldung, kostenlos starten!
www.SMS-Contacts.de/Sexy

[Yamaha Boats For Sale](#)

Find, Buy and Sell the Right Boat! Free Text/Email Alert Service
rightboat.com/adverts/Yamaha.html

[Wild Yam Root](#)

Harvested at height of potency. 20 Year, Family Run Herb Company.
www.Blessed-Herbs.com

WEITERE LINKS

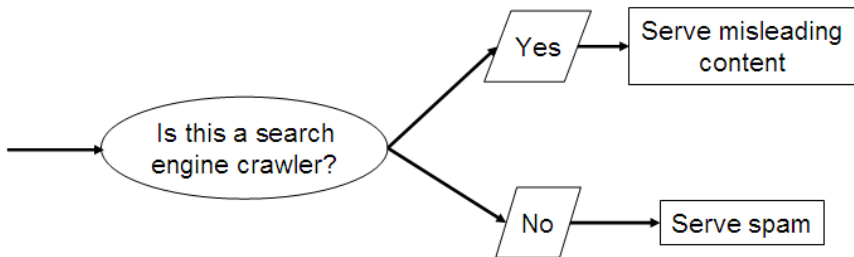
- ▾ Wild Yam Root
- ▾ Mexican Appetizers
- ▾ Yam
- ▾ Gambar Skodeng Ulu Yam
- ▾ Wild Eyes
- ▾ The Yam Yams
- ▾ Arnica Cream
- ▾ Chickweed Cream
- ▾ Colloidal Silver Cream
- ▾ Witch Hazel Cream

- Number one hit on Google for the search “composita”
- The only purpose of this page: get people to click on the ads and make money for the page owner

Spam technique: Duplication

- Get good content from somewhere (steal it or produce it yourself)
- Publish a large number of slight variations of it
- For example, publish the answer to a tax question with the spelling variations of “tax deferred” on the previous slide

Spam technique: Cloaking



- Serve fake content to search engine spider
- So do we just penalize this always?
- No: legitimate uses (e.g., different content to US vs. European users)

Spam technique: Link spam

- Create lots of links pointing to the page you want to promote
- Put these links on pages with high (or at least non-zero) PageRank
 - Newly registered domains (domain flooding)
 - A set of pages that all point to each other to boost each other's PageRank (mutual admiration society)
 - Pay somebody to put your link on their highly ranked page (“schuetze horoskop” example)
 - Leave comments that include the link on blogs

SEO: Search engine optimization

- Promoting a page in the search rankings is not necessarily spam.
- It can also be a legitimate business – which is called SEO.
- You can hire an SEO firm to get your page highly ranked.
- There are many legitimate reasons for doing this.
 - For example, Google bombs like *Who is a failure?*
- And there are many legitimate ways of achieving this:
 - Restructure your content in a way that makes it easy to index
 - Talk with influential bloggers and have them link to your site
 - Add more interesting and original content

The war against spam

- Quality indicators
 - Links, statistically analyzed (PageRank, etc.)
 - Usage (users visiting a page)
 - No adult content (e.g., no pictures with flesh-tone)
 - Distribution and structure of text (e.g., no keyword stuffing)
- Combine all of these indicators and use machine learning
- Editorial intervention
 - Blacklists
 - Top queries audited
 - Complaints addressed
 - Suspect patterns detected

Webmaster guidelines

- Major search engines have guidelines for webmasters.
- These guidelines tell you what is legitimate SEO and what is spamming.
- Ignore these guidelines at your own risk
- Once a search engine identifies you as a spammer, all pages on your site may get low ranks (or disappear from the index entirely).
- There is often a fine line between spam and legitimate SEO.
- Scientific study of fighting spam on the web: *adversarial information retrieval*

Web IR: Differences from traditional IR

- Links: The web is a hyperlinked document collection.
- Queries: Web queries are different, more varied and there are a lot of them. How many? $\approx 10^9$
- Users: Users are different, more varied and there are a lot of them. How many? $\approx 10^9$
- Documents: Documents are different, more varied and there are a lot of them. How many? $\approx 10^{11}$
- Context: Context is more important on the web than in many other IR applications.
- Ads and spam

Query distribution (1)

Most frequent queries on a large search engine on 2002.10.26.

| | | | | | | | |
|----|------------|----|-----------------|----|---------------|----|---------------------|
| 1 | sex | 16 | crack | 31 | juegos | 46 | Caramail |
| 2 | (artifact) | 17 | games | 32 | nude | 47 | msn |
| 3 | (artifact) | 18 | pussy | 33 | music | 48 | jennifer lopez |
| 4 | porno | 19 | cracks | 34 | musica | 49 | tits |
| 5 | mp3 | 20 | lolita | 35 | anal | 50 | free porn |
| 6 | Halloween | 21 | britney spears | 36 | free6 | 51 | cheats |
| 7 | sexo | 22 | ebay | 37 | avril lavigne | 52 | yahoo.com |
| 8 | chat | 23 | sexe | 38 | hotmail.com | 53 | eminem |
| 9 | porn | 24 | Pamela Anderson | 39 | winzip | 54 | Christina Aguilera |
| 10 | yahoo | 25 | warez | 40 | fuck | 55 | incest |
| 11 | KaZaA | 26 | divx | 41 | wallpaper | 56 | letras de canciones |
| 12 | xxx | 27 | gay | 42 | hotmail.com | 57 | hardcore |
| 13 | Hentai | 28 | harry potter | 43 | postales | 58 | weather |
| 14 | lyrics | 29 | playboy | 44 | shakira | 59 | wallpapers |
| 15 | hotmail | 30 | lolitas | 45 | traductor | 60 | lingerie |

More than 1/3 of these are queries for adult content. Exercise: Does this mean that most people are looking for adult content?

Query distribution (2)

- Queries have a power law distribution.
- Recall Zipf's law: a few very frequent words, a large number of very rare words
- Same here: a few very frequent queries, a large number of very rare queries
- Examples of rare queries: search for names, towns, books, etc.
- The proportion of adult queries is much lower than $1/3$

Types of queries / user needs in web search

- **Informational user needs:** I need information on something.
“low hemoglobin”
- We called this “information need” earlier in the class.
- **On the web, information needs proper are only a subclass of user needs.**
- Other user needs: Navigational and transactional
- **Navigational user needs:** I want to go to this web site.
“hotmail”, “myspace”, “United Airlines”
- **Transactional user needs:** I want to make a transaction.
 - Buy something: “MacBook Air”
 - Download something: “Acrobat Reader”
 - Chat with someone: “live soccer chat”
- **Difficult problem:** How can the search engine tell what the user need or intent for a particular query is?

Search in a hyperlinked collection

- Web search in most cases is interleaved with navigation ...
- ... i.e., with following links.
- Different from most other IR collections

Kinds of behaviors we see in the data

Short / Nav



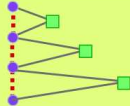
Topic exploration



Topic switch



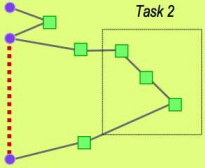
Methodical results exploration



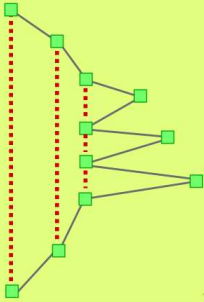
Query reform



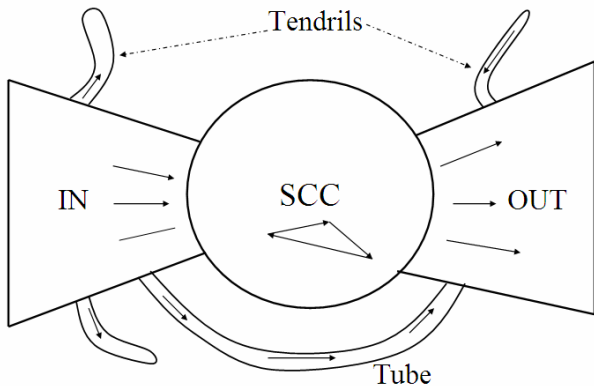
Multitasking



Stacking behavior



Bowtie structure of the web



- Strongly connected component (SCC) in the center
- Lots of pages that get linked to, but don't link (OUT)
- Lots of pages that link to other pages, but don't get linked to (IN)
- Tendrils, tubes, islands

User intent: Answering the need behind the query

- What can we do to guess user intent?
- Guess user intent independent of context:
 - Spell correction
 - Precomputed “typing” of queries (next slide)
- Better: Guess user intent based on context:
 - Geographic context (slide after next)
 - Context of user in this session (e.g., previous query)
 - Context provided by personal profile (Yahoo/MSN do this, Google claims it does not)

Guessing of user intent by “typing” queries

- Calculation: 5+4
- Unit conversion: 1 kg in pounds
- Currency conversion: 1 euro in kronor
- Tracking number: 8167 2278 6764
- Flight info: LH 454
- Area code: 650
- Map: columbus oh
- Stock price: msft
- Albums/movies, etc.: coldplay

The spatial context: Geo-search

- Three relevant locations
 - Server (nytimes.com → New York)
 - Web page (nytimes.com article about Albania)
 - User (located in Palo Alto)
- Locating the user
 - IP address
 - Information provided by user (e.g., in user profile)
 - Mobile phone
- **Geo-tagging**: Parse text and identify the coordinates of the geographic entities
 - Example: East Palo Alto CA → Latitude: 37.47 N, Longitude: 122.14 W
 - Important NLP problem

How do we use context to modify query results?

- Result restriction: Don't consider inappropriate results
 - For user on google.fr . . .
 - . . . only show .fr results
- Ranking modulation: use a rough generic ranking, rerank based on personal context
- Contextualization / personalization is an area of search with a lot of potential for improvement.

Users of web search

- Use short queries (average < 3)
- Rarely use operators
- Do not want to spend a lot of time on composing a query
- Only look at the first couple of results
- Want a simple UI, not a search engine start page overloaded with graphics
- Extreme variability in terms of user needs, user expectations, experience, knowledge, . . .
 - Industrial/developing world, English/Estonian, old/young, rich/poor, differences in culture and class
- One interface for hugely divergent needs

How do users evaluate search engines?

- Classic IR relevance (as measured by F) can also be used for web IR.
- Equally important: Trust, duplicate elimination, readability, loads fast, no pop-ups
- On the web, precision is more important than recall.
 - Precision at 1, precision at 10, precision on the first 2–3 pages
 - But there is a subset of queries where recall matters.

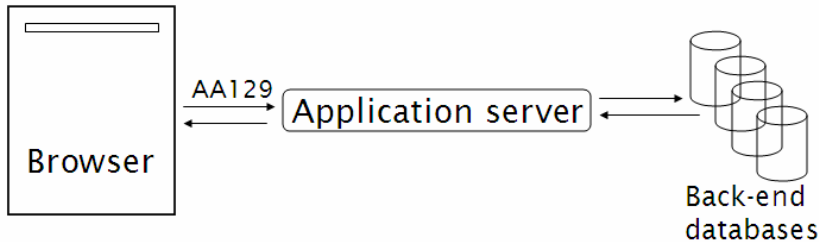
Web information needs that require high recall

- Has this idea been patented?
- Searching for info on a prospective financial advisor
- Searching for info on a prospective employee
- Searching for info on a date

Web documents: different from other IR collections

- Distributed content creation: no design, no coordination
 - “Democratization of publishing”
 - Result: extreme heterogeneity of documents on the web
- Unstructured (text, html), semistructured (html, xml), structured/relational (databases)
- Dynamically generated content

Dynamic content

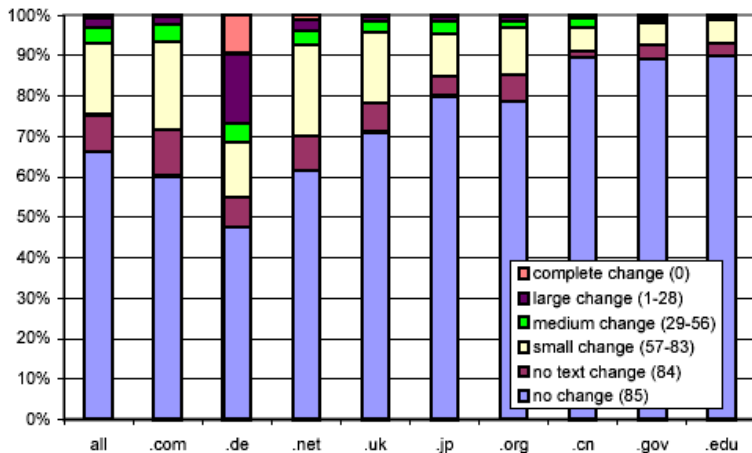


- Dynamic pages are generated from scratch when the user requests them – usually from underlying data in a database.
- Example: current status of flight LH 454

Dynamic content (2)

- Most (truly) dynamic content is ignored by web spiders.
 - It's too much to index it all.
- Actually, a lot of “static” content is also assembled on the fly (asp, php, etc.: headers, date, ads, etc.)

Web pages change frequently (Fetterly 1997)



Multilinguality

- Documents in a large number of languages
- Queries in a large number of languages
- First cut: Don't return English results for a Japanese query
- However: Frequent mismatches query/document languages
- Many people can understand, but not query in a language.
- Translation is important.
- Google example: "Beaujolais Nouveau -wine"

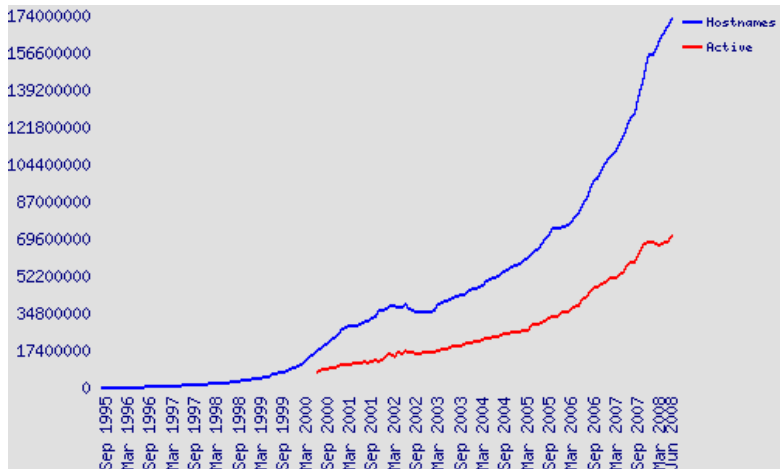
Duplicate documents

- Significant duplication – 30%–40% duplicates in some studies.
- Duplicates in the search results were common in the early days of the web.
- Today's search engines eliminate duplicates very effectively.
- Key for high user satisfaction.

Trust

- For many collections, it is easy to assess the trustworthiness of a document.
 - A collection of Reuters newswire articles
 - A collection of TASS (Telegraph Agency of the Soviet Union) newswire articles from the 1980s
 - Your Outlook email from the last three years
- Web documents are different: In many cases, we don't know how to evaluate the information.
- Hoaxes abound.

Growth of the web



- The web keeps growing.
- But growth is no longer exponential?

Size of the web: Issues

- What is size? Number of web servers? Number of pages?
Terabytes of data available?
- Some servers are seldom connected.
 - Example: Your laptop running a web server
 - Is it part of the web?
- The “dynamic” web is infinite.
 - Any sum of two numbers is its own dynamic page on Google.
(Example: “2+4”)

“Search engine index contains N pages”: Issues

- Can I claim a page is in the index if I only index the first 4,000 bytes?
- Can I claim a page is in the index if I only index anchor text pointing to the page?
 - There used to be (and still are?) billions of pages that are only indexed by anchor text.

Simple method for determining a lower bound

- OR-query of frequent words in a number of languages
- According to this query: Size of web $\geq 21,450,000,000$ on 2007.07.07 and $\geq 25,350,000,000$ on 2008.07.03
- But page counts of Google search results are only rough estimates.

Size of the web: Who cares?

- Media
- Users
 - They may switch to the search engine that has the best coverage of the web.
 - Users (sometimes) care about recall. If we underestimate the size of the web, search engine results may have low recall.
- Search engine designers (how many pages do I need to be able to handle?)
- Crawler designers (which policy will crawl close to N pages?)

What is the size of the web? Any guesses?

Simple method for determining a lower bound

- OR-query of frequent words in a number of languages
- According to this query: Size of web $\geq 21,450,000,000$ on 2007.07.07
- Big if: Page counts of Google search results are correct. (Generally, they are just rough estimates.)
- But this is just a lower bound, based on one search engine.
- How can we do better?

Size of the web: Issues

- The “dynamic” web is infinite.
 - Any sum of two numbers is its own dynamic page on Google. (Example: “2+4”)
 - Many other dynamic sites generating infinite number of pages
- The static web contains duplicates – each “equivalence class” should only be counted once.
- Some servers are seldom connected.
 - Example: Your laptop
 - Is it part of the web?

“Search engine index contains N pages”: Issues

- Can I claim a page is in the index if I only index the first 4,000 bytes?
- Can I claim a page is in the index if I only index anchor text pointing to the page?
 - There used to be (and still are?) billions of pages that are only indexed by anchor text.

How can we estimate the size of the web?

Sampling methods

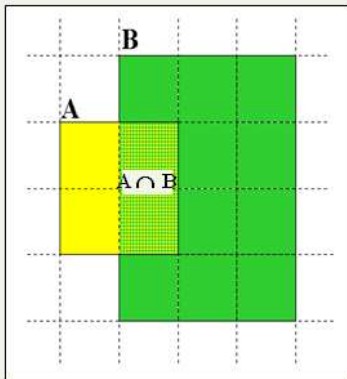
- Random queries
- Random searches
- Random IP addresses
- Random walks

Variant: Estimate relative sizes of indexes

- There are significant differences between indexes of different search engines.
- Different engines have different preferences.
 - max URL depth, max count/host, anti-spam rules, priority rules etc.
- Different engines index different things under the same URL.
 - anchor text, frames, meta-keywords, size of prefix etc.

Relative Size from Overlap

[Bharat & Broder, 98]



Sample URLs randomly from A

Check if contained in B

and vice versa

$$A \cap B = (1/2) * \text{Size A}$$

$$A \cap B = (1/6) * \text{Size B}$$

$$(1/2) * \text{Size A} = (1/6) * \text{Size B}$$

$$\therefore \text{Size A} / \text{Size B} =$$

$$(1/6) / (1/2) = 1/3$$

Each test involves: (i) Sampling (ii) Checking

Sampling URLs

- Ideal strategy: Generate a random URL
- Problem: Random URLs are hard to find (and sampling distribution should reflect “user interest”)
- Approach 1: Random walks / IP addresses
 - In theory: might give us a true estimate of the size of the web (as opposed to just relative sizes of indexes)
- Approach 2: Generate a random URL contained in a given engine
 - Suffices for accurate estimation of relative size

Random URLs from random queries

- Idea: Use vocabulary of the web for query generation
- Vocabulary can be generated from web crawl
- Use conjunctive queries w_1 AND w_2
 - Example: vocalists AND rsi
- Get result set of one hundred URLs from the source engine
- Choose a random URL from the result set
- This sampling method induces a weight $W(p)$ for each page p .
- Method was used by Bharat and Broder (1998).

Checking if a page is in the index

- Either: Search for URL if the engine supports this
- Or: Create a query that will find doc d with high probability
 - Download doc, extract words
 - Use 8 low frequency word as AND query
 - Call this a **strong query** for d
 - Run query
 - Check if d is in result set
- Problems
 - Near duplicates
 - Redirects
 - Engine time-outs

Computing Relative Sizes and Total Coverage [BB98]

a = AltaVista, **e** = Excite, **h** = HotBot, **i** = Infoseek

f_{xy} = fraction of x in y

- Six pair-wise overlaps

$$f_{ah} * a - f_{ha} * h = \epsilon_1$$

$$f_{ai} * a - f_{ia} * i = \epsilon_2$$

$$f_{ae} * a - f_{ea} * e = \epsilon_3$$

$$f_{hi} * h - f_{ih} * i = \epsilon_4$$

$$f_{he} * h - f_{eh} * e = \epsilon_5$$

$$f_{ei} * e - f_{ie} * i = \epsilon_6$$

- Arbitrarily, let **a** = 1.

- We have 6 equations and 3 unknowns.
- Solve for **e**, **h** and **i** to minimize $\sum \epsilon_i^2$
- Compute engine overlaps.
- Re-normalize so that the total joint coverage is 100%

Advantages & disadvantages

- Statistically sound under the induced weight.
- Biases induced by random query
 - Query Bias: Favors content-rich pages in the language(s) of the lexicon
 - Ranking Bias: *Solution*: Use conjunctive queries & fetch all
 - Checking Bias: Duplicates, impoverished pages omitted
 - Document or query restriction bias: engine might not deal properly with 8 words conjunctive query
 - Malicious Bias: Sabotage by engine
 - Operational Problems: Time-outs, failures, engine inconsistencies, index modification.

Random searches

- Choose random searches extracted from a search engine log (Lawrence & Giles 97)
- Use only queries with small result sets
- For each random query: compute ratio $\text{size}(r_1)/\text{size}(r_2)$ of the two result sets
- Average over random searches

Advantages & disadvantages

- Advantage
 - Might be a better reflection of the human perception of coverage
- Issues
 - Samples are correlated with source of log (unfair advantage for originating search engine)
 - Duplicates
 - Technical statistical problems (must have non-zero results, ratio average not statistically sound)

Random searches [Lawr98, Lawr99]

- 575 & 1050 queries from the NEC RI employee logs
- 6 Engines in 1998, 11 in 1999
- Implementation:
 - Restricted to queries with < 600 results in total
 - Counted URLs from each engine after verifying query match
 - Computed size ratio & overlap for individual queries
 - Estimated index size ratio & overlap by averaging over all queries

Queries from Lawrence and Giles study

- adaptive access control
- neighborhood preservation topographic
- hamiltonian structures
- right linear grammar
- pulse width modulation neural
- unbalanced prior probabilities
- ranked assignment method
- internet explorer favourites importing
- karvel thornber
- zili liu
- softmax activation function
- bose multidimensional system theory
- gamma mlp
- dvi2pdf
- john oliensis
- rieke spikes exploring neural
- video watermarking
- counterpropagation network
- fat shattering dimension
- abelson amorphous computing

Random IP addresses [Lawrence & Giles '99]

- Generate random IP addresses
- Find a web server at the given address
 - If there's one
- Collect all pages from server.
- Method first used by O'Neill, McClain, & Lavoie, **“A Methodology for Sampling the World Wide Web”, 1997.**

<http://digitalarchive.oclc.org/da/ViewObject.jsp?objid=0000003447>

Random IP addresses [ONei97, Lawr99]

- [Lawr99] exhaustively crawled 2,500 servers and extrapolated
- Estimated size of the web to be 800 million

Advantages and disadvantages

- Advantages
 - Can, in theory, estimate the size of the accessible web (as opposed to the (relative) size of an index)
 - Clean statistics
 - Independent of crawling strategies
- Disadvantages
 - Many hosts share one IP (→ oversampling)
 - Hosts with large web sites don't get more weight than hosts with small web sites (→ possible undersampling)
 - Sensitive to spam (multiple IPs for same spam server)
 - Again, duplicates

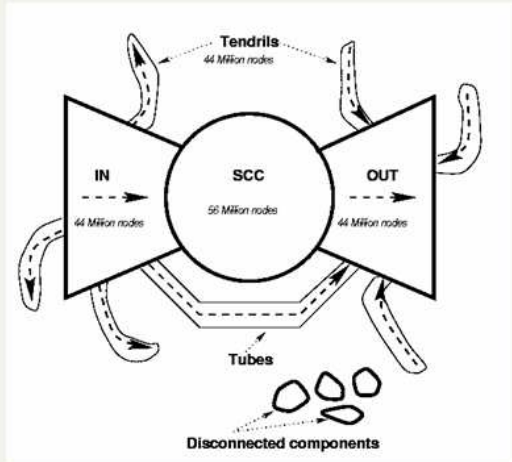
Random walks

[Henzinger *et al* WWW9]

- View the Web as a directed graph
- Build a random walk on this graph
 - Includes various “jump” rules back to visited sites
 - Does not get stuck in spider traps!
 - Can follow all links!
 - Converges to a stationary distribution
 - Must assume graph is finite and independent of the walk.
 - Conditions are not satisfied (cookie crumbs, flooding)
 - Time to convergence not really known
 - Sample from stationary distribution of walk
 - Use the “strong query” method to check coverage by SE

Dependence on seed list

- How well connected is the graph? [Broder et al., WWW9]



Advantages & disadvantages

- Advantages
 - “Statistically clean” method at least in theory!
 - Could work even for infinite web (assuming convergence) under certain metrics.
- Disadvantages
 - List of seeds is a problem.
 - Practical approximation might not be valid.
 - Non-uniform distribution
 - Subject to link spamming

Conclusion

- Many different approaches to web size estimation.
- None is perfect.
- The problem has gotten much harder.
- There has not been a good study for a couple of years.
- Great topic for a thesis!

Resources

- Chapter 19 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - Hal Varian explains Google second price auction: <https://youtube.com/watch?v=K710a2PVhPQ>
 - Size of the web queries
 - Trademark issues (Geico and Vuitton cases)
 - How ads are priced
 - Henzinger, Finding near-duplicate web pages: A large-scale evaluation of algorithms, ACM SIGIR 2006.

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 21: Link analysis Handout version

Petr Sojka, Hinrich Schütze et al.

Faculty of Informatics, Masaryk University, Brno
Center for Information and Language Processing, University of Munich

2024-05-15

(compiled on 2024-05-06 13:42:13)

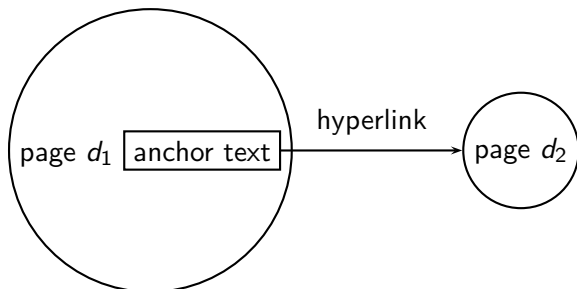
Overview

- 1 Anchor text
- 2 Citation analysis
- 3 PageRank
- 4 HITS: Hubs & Authorities

Take-away today

- Anchor text: What exactly are links on the web and why are they important for IR?
- Citation analysis: the mathematical foundation of PageRank and link-based ranking
- PageRank: the original algorithm that was used for link-based ranking on the web
- Hubs & Authorities: an alternative link-based ranking algorithm

The web as a directed graph



- Assumption 1: A hyperlink is a quality signal.
 - The hyperlink $d_1 \rightarrow d_2$ indicates that d_1 's author deems d_2 high-quality and relevant.
- Assumption 2: The anchor text describes the content of d_2 .
 - We use anchor text somewhat loosely here for: the text surrounding the hyperlink.
 - Example: "You can find cheap cars here."
 - Anchor text: "You can find cheap cars here"



[text of d_2] only vs. [text of d_2] + [anchor text $\rightarrow d_2$]

- Searching on [text of d_2] + [anchor text $\rightarrow d_2$] is often more effective than searching on [text of d_2] only.
- Example: Query *IBM*
 - Matches IBM's copyright page
 - Matches many spam pages
 - Matches IBM Wikipedia article
 - May not match IBM home page!
 - ... if IBM home page is mostly graphics
- Searching on [anchor text $\rightarrow d_2$] is better for the query *IBM*.
 - In this representation, the page with the most occurrences of *IBM* is www.ibm.com. □

Anchor text containing *IBM* pointing to www.ibm.com

www.nytimes.com: “IBM acquires Webify”

www.slashdot.org: “New IBM optical chip”

www.stanford.edu: “IBM faculty award recipients”

www.ibm.com

```
graph TD; A["www.nytimes.com: 'IBM acquires Webify'"] -.-> D["www.ibm.com"]; B["www.slashdot.org: 'New IBM optical chip'"] -.-> D; C["www.stanford.edu: 'IBM faculty award recipients'"] -.-> D;
```

Indexing anchor text

- Thus: Anchor text is often a better description of a page's content than the page itself.
- Anchor text can be weighted more highly than document text. (based on Assumptions 1&2)

Exercise: Assumptions underlying PageRank

- Assumption 1: A link on the web is a quality signal – the author of the link thinks that the linked-to page is high-quality.
- Assumption 2: The anchor text describes the content of the linked-to page.
- Is assumption 1 true in general?
- Is assumption 2 true in general?

Google bombs

- A Google bomb is a search with “bad” results due to maliciously manipulated anchor text.
- Google introduced a new weighting function in 2007 that fixed many Google bombs.
- Still some remnants: [dangerous cult] on Google, Bing, Yahoo
 - Coordinated link creation by those who dislike the Church of Scientology
- Defused Google bombs: [dumb motherf. . .], [who is a failure?], [evil empire] □

Origins of PageRank: Citation analysis (1)

- Citation analysis: analysis of citations in the scientific literature
- Example citation: “[Miller \(2001\)](#) has shown that physical activity alters the metabolism of estrogens.”
- We can view “[Miller \(2001\)](#)” as a hyperlink linking two scientific articles.
- One application of these “hyperlinks” in the scientific literature:
 - Measure the similarity of two articles by the overlap of other articles citing them.
 - This is called [cocitation similarity](#).
 - Cocitation similarity on the web: Google’s “related:” operator, e.g. `[related:www.ford.com]` □

Origins of PageRank: Citation analysis (2)

- Another application: Citation frequency can be used to measure the **impact** of a scientific article.
 - Simplest measure: Each citation gets one vote.
 - On the web: citation frequency = **inlink count**
- However: A high inlink count does not necessarily mean high quality ...
- ... mainly because of link spam.
- Better measure: **weighted** citation frequency or citation rank
 - An citation's vote is weighted according to its citation impact.
 - Circular? No: can be formalized in a well-defined way. □

Origins of PageRank: Citation analysis (3)

- Better measure: weighted citation frequency or citation rank
- This is basically PageRank.
- PageRank was invented in the context of citation analysis by Pinski and Narin in the 1960s.
- Citation analysis is a big deal: The budget and salary of this lecturer are / will be determined by the impact of his publications!



Origins of PageRank: Summary

- We can use the same formal representation for
 - citations in the scientific literature
 - hyperlinks on the web
- Appropriately weighted citation frequency is an excellent measure of quality ...
 - ... both for web pages and for scientific publications.
- Next: PageRank algorithm for computing weighted citation frequency on the web

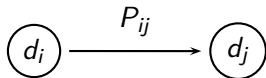


Model behind PageRank: Random walk

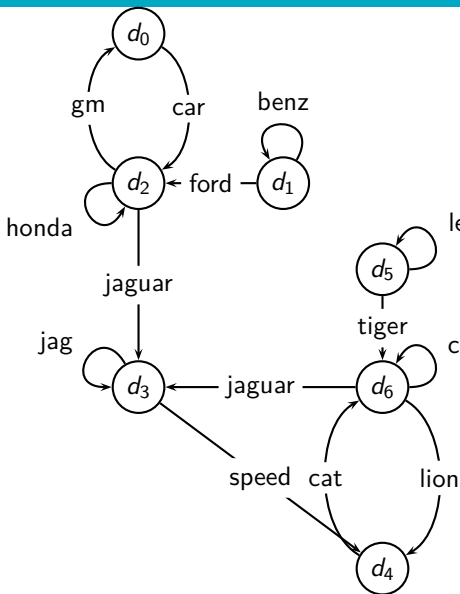
- Imagine a web surfer doing a random walk on the web
 - Start at a random page
 - At each step, go out of the current page along one of the links on that page, equiprobably
- In the steady state, each page has a **long-term visit rate**.
- This long-term visit rate is the page's **PageRank**.
- **PageRank = long-term visit rate = steady state probability** □

Formalization of random walk: Markov chains

- A Markov chain consists of N states, plus an $N \times N$ transition probability matrix P .
- state = page
- At each step, we are on exactly one of the pages.
- For $1 \leq i, j \leq N$, the matrix entry P_{ij} tells us the probability of j being the next page, given we are currently on page i .
- Clearly, for all i , $\sum_{j=1}^N P_{ij} = 1$



Example web graph



PageRank

| | | | | | |
|-------|------|-------|------|-------|------|
| d_0 | 0.05 | d_1 | 0.04 | d_2 | 0.11 |
| d_3 | 0.25 | d_4 | 0.21 | d_5 | 0.04 |
| d_6 | 0.31 | | | | |

PageRank(d_2) < PageRank(d_6):
why?

| | a | h |
|-------|------|------|
| d_0 | 0.10 | 0.03 |
| d_1 | 0.01 | 0.04 |
| d_2 | 0.12 | 0.33 |
| d_3 | 0.47 | 0.18 |
| d_4 | 0.16 | 0.04 |
| d_5 | 0.01 | 0.04 |
| d_6 | 0.13 | 0.35 |

highest in-degree: d_2, d_3, d_6

highest out-degree: d_2, d_6

highest PageRank: d_6

highest hub score: d_6 (close: d_2)

highest authority score: d_3 □

Link matrix for example

| | d_0 | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|-------|
| d_0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| d_1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| d_2 | 1 | 0 | 1 | 1 | 0 | 0 | 0 |
| d_3 | 0 | 0 | 0 | 1 | 1 | 0 | 0 |
| d_4 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| d_5 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| d_6 | 0 | 0 | 0 | 1 | 1 | 0 | 1 |

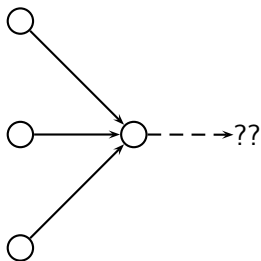
Transition probability matrix P for example

| | d_0 | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|-------|
| d_0 | 0.00 | 0.00 | 1.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| d_1 | 0.00 | 0.50 | 0.50 | 0.00 | 0.00 | 0.00 | 0.00 |
| d_2 | 0.33 | 0.00 | 0.33 | 0.33 | 0.00 | 0.00 | 0.00 |
| d_3 | 0.00 | 0.00 | 0.00 | 0.50 | 0.50 | 0.00 | 0.00 |
| d_4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.00 |
| d_5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.50 | 0.50 |
| d_6 | 0.00 | 0.00 | 0.00 | 0.33 | 0.33 | 0.00 | 0.33 |

Long-term visit rate

- Recall: PageRank = long-term visit rate
- Long-term visit rate of page d is the probability that a web surfer is at page d at a given point in time.
- Next: what properties must hold of the web graph for the long-term visit rate to be well defined?
- The web graph must correspond to an **ergodic** Markov chain.
- First a special case: The web graph must not contain **dead ends**. □

Dead ends



- The web is full of dead ends.
- Random walk can get stuck in dead ends.
- If there are dead ends, long-term visit rates are not well-defined (or non-sensical).



Teleporting – to get us out of dead ends

- At a **dead end**, jump to a random web page with prob. $1/N$.
- At a **non-dead end**, with probability 10%, jump to a random web page (to each with a probability of $0.1/N$).
- With remaining probability (90%), go out on a random hyperlink.
 - For example, if the page has 4 outgoing links: randomly choose one with probability $(1-0.10)/4=0.225$
- 10% is a parameter, the **teleportation rate**.
- Note: “jumping” from dead end is independent of teleportation rate.



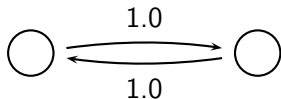
Result of teleporting

- With teleporting, we cannot get stuck in a dead end.
- But even without dead ends, a graph may not have well-defined long-term visit rates.
- More generally, we require that the Markov chain be **ergodic**.



Ergodic Markov chains

- A Markov chain is ergodic iff it is irreducible and aperiodic.
- **Irreducibility.** Roughly: there is a path from any page to any other page.
- **Aperiodicity.** Roughly: The pages cannot be partitioned such that the random walker visits the partitions sequentially.
- A non-ergodic Markov chain:



Ergodic Markov chains

- Theorem: For any ergodic Markov chain, there is a unique long-term visit rate for each state.
- This is the **steady-state probability distribution**.
- Over a long time period, we visit each state in proportion to this rate.
- It doesn't matter where we start.
- **Teleporting makes the web graph ergodic.**
- **⇒ Web-graph+teleporting has a steady-state probability distribution.**
- **⇒ Each page in the web-graph+teleporting has a PageRank.**



Where we are

- We now know what to do to make sure we have a well-defined PageRank for each page.
- Next: how to compute PageRank

Formalization of “visit”: Probability vector

- A probability (row) vector $\vec{x} = (x_1, \dots, x_N)$ tells us where the random walk is at any point.

- Example:
$$\begin{pmatrix} 0 & 0 & 0 & \dots & 1 & \dots & 0 & 0 & 0 \\ 1 & 2 & 3 & \dots & i & \dots & N-2 & N-1 & N \end{pmatrix}$$

- More generally: the random walk is on page i with probability x_i .

- Example:
$$\begin{pmatrix} 0.05 & 0.01 & 0.0 & \dots & 0.2 & \dots & 0.01 & 0.05 & 0.03 \\ 1 & 2 & 3 & \dots & i & \dots & N-2 & N-1 & N \end{pmatrix}$$

- $\sum x_i = 1$



Change in probability vector

- If the probability vector is $\vec{x} = (x_1, \dots, x_N)$ at this step, what is it at the next step?
- Recall that row i of the transition probability matrix P tells us where we go next from state i .
- So from \vec{x} , our next state is distributed as $\vec{x}P$. □

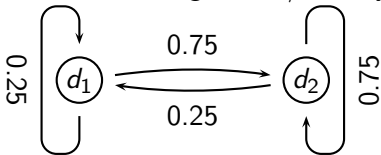
Steady state in vector notation

- The steady state in vector notation is simply a vector $\vec{\pi} = (\pi_1, \pi_2, \dots, \pi_N)$ of probabilities.
- (We use $\vec{\pi}$ to distinguish it from the notation for the probability vector \vec{x} .)
- π_i is the long-term visit rate (or PageRank) of page i .
- So we can think of PageRank as a very long vector – one entry per page.



Steady-state distribution: Example

- What is the PageRank / steady state in this example?



Steady-state distribution: Example

| | x_1 $P_t(d_1)$ | x_2 $P_t(d_2)$ | | |
|-------|---------------------|---------------------|-----------------|-----------------|
| | | | $P_{11} = 0.25$ | $P_{12} = 0.75$ |
| | | | $P_{21} = 0.25$ | $P_{22} = 0.75$ |
| t_0 | 0.25 | 0.75 | 0.25 | 0.75 |
| t_1 | 0.25 | 0.75 | (convergence) | |

PageRank vector = $\vec{\pi} = (\pi_1, \pi_2) = (0.25, 0.75)$

$$P_t(d_1) = P_{t-1}(d_1) * P_{11} + P_{t-1}(d_2) * P_{21}$$

$$P_t(d_2) = P_{t-1}(d_1) * P_{12} + P_{t-1}(d_2) * P_{22}$$



How do we compute the steady state vector?

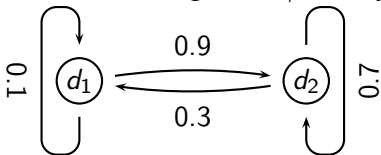
- In other words: how do we compute PageRank?
- Recall: $\vec{\pi} = (\pi_1, \pi_2, \dots, \pi_N)$ is the PageRank vector, the vector of steady-state probabilities ...
- ... and if the distribution in this step is \vec{x} , then the distribution in the next step is $\vec{x}P$.
- But $\vec{\pi}$ is the steady state!
- So: $\vec{\pi} = \vec{\pi}P$
- Solving this matrix equation gives us $\vec{\pi}$.
- $\vec{\pi}$ is the principal left eigenvector for P ...
- ... that is, $\vec{\pi}$ is the left eigenvector with the largest eigenvalue.
- All transition probability matrices have largest eigenvalue 1. \square

One way of computing the PageRank $\vec{\pi}$

- Start with any distribution \vec{x} , e.g., uniform distribution
- After one step, we're at $\vec{x}P$.
- After two steps, we're at $\vec{x}P^2$.
- After k steps, we're at $\vec{x}P^k$.
- Algorithm: multiply \vec{x} by increasing powers of P until convergence.
- This is called the **power method**.
- Recall: regardless of where we start, we eventually reach the steady state $\vec{\pi}$.
- Thus: we will eventually (in asymptotia) reach the steady state. □

Power method: Example

- What is the PageRank / steady state in this example?



- The steady state distribution (= the PageRanks) in this example are 0.25 for d_1 and 0.75 for d_2 .

Computing PageRank: Power method

| | x_1 $P_t(d_1)$ | x_2 $P_t(d_2)$ | | | |
|------------|---------------------|---------------------|----------------|----------------|---------------------|
| | | | $P_{11} = 0.1$ | $P_{12} = 0.9$ | |
| | | | $P_{21} = 0.3$ | $P_{22} = 0.7$ | |
| t_0 | 0 | 1 | 0.3 | 0.7 | $= \vec{x}P$ |
| t_1 | 0.3 | 0.7 | 0.24 | 0.76 | $= \vec{x}P^2$ |
| t_2 | 0.24 | 0.76 | 0.252 | 0.748 | $= \vec{x}P^3$ |
| t_3 | 0.252 | 0.748 | 0.2496 | 0.7504 | $= \vec{x}P^4$ |
| | | | | ... | ... |
| t_∞ | 0.25 | 0.75 | 0.25 | 0.75 | $= \vec{x}P^\infty$ |

PageRank vector = $\vec{\pi} = (\pi_1, \pi_2) = (0.25, 0.75)$

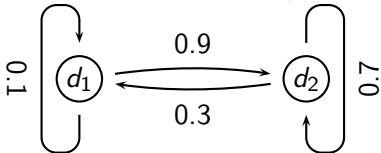
$$P_t(d_1) = P_{t-1}(d_1) * P_{11} + P_{t-1}(d_2) * P_{21}$$

$$P_t(d_2) = P_{t-1}(d_1) * P_{12} + P_{t-1}(d_2) * P_{22}$$



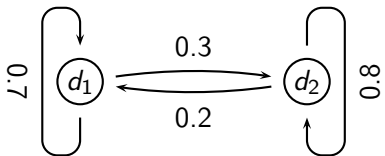
Power method: Example

- What is the PageRank / steady state in this example?



- The steady state distribution (= the PageRanks) in this example are 0.25 for d_1 and 0.75 for d_2 .

Exercise: Compute PageRank using power method



Solution

| | x_1 | x_2 | | |
|------------|------------|------------|----------------|----------------|
| | $P_t(d_1)$ | $P_t(d_2)$ | | |
| | | | $P_{11} = 0.7$ | $P_{12} = 0.3$ |
| | | | $P_{21} = 0.2$ | $P_{22} = 0.8$ |
| t_0 | 0 | 1 | 0.2 | 0.8 |
| t_1 | 0.2 | 0.8 | 0.3 | 0.7 |
| t_2 | 0.3 | 0.7 | 0.35 | 0.65 |
| t_3 | 0.35 | 0.65 | 0.375 | 0.625 |
| | | | | ... |
| t_∞ | 0.4 | 0.6 | 0.4 | 0.6 |

PageRank vector = $\vec{\pi} = (\pi_1, \pi_2) = (0.4, 0.6)$

$$P_t(d_1) = P_{t-1}(d_1) * P_{11} + P_{t-1}(d_2) * P_{21}$$

$$P_t(d_2) = P_{t-1}(d_1) * P_{12} + P_{t-1}(d_2) * P_{22}$$



PageRank summary

- Preprocessing
 - Given graph of links, build matrix P
 - Apply teleportation
 - From modified matrix, compute $\vec{\pi}$
 - π_i is the PageRank of page i .
- Query processing
 - Retrieve pages satisfying the query
 - Rank them by their PageRank
 - Return reranked list to the user

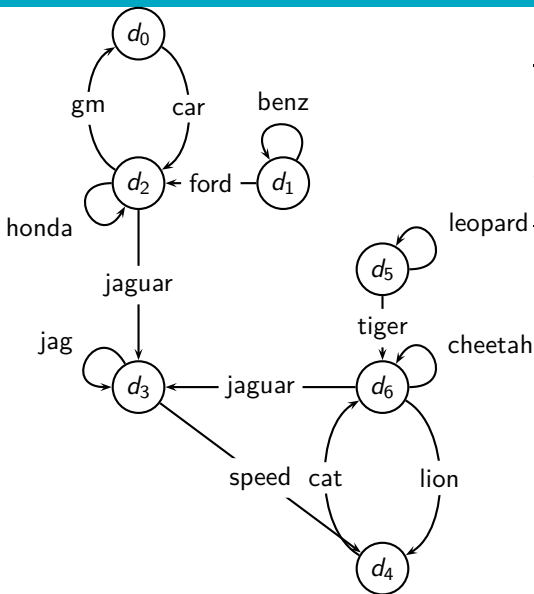


PageRank issues

- Real surfers are not random surfers.
 - Examples of nonrandom surfing: back button, short vs. long paths, bookmarks, directories – and search!
 - → Markov model is not a good model of surfing.
 - But it's good enough as a model for our purposes.
- Simple PageRank ranking (as described on previous slide) produces bad results for many pages.
 - Consider the query [video service]
 - The Yahoo home page (i) has a very high PageRank and (ii) contains both *video* and *service*.
 - If we rank all Boolean hits according to PageRank, then the Yahoo home page would be top-ranked.
 - Clearly not desirable
- In practice: rank according to weighted combination of raw text match, anchor text match, PageRank & other factors
- → see lecture on Learning to Rank



Example web graph



PageRank

| | | | | | |
|-------|------|-------|------|-------|------|
| d_0 | 0.05 | d_1 | 0.04 | d_2 | 0.11 |
| d_3 | 0.25 | d_4 | 0.21 | d_5 | 0.04 |
| d_6 | 0.31 | | | | |

PageRank(d_2) < PageRank(d_6):
why?

| | a | h |
|-------|------|------|
| d_0 | 0.10 | 0.03 |
| d_1 | 0.01 | 0.04 |
| d_2 | 0.12 | 0.33 |
| d_3 | 0.47 | 0.18 |
| d_4 | 0.16 | 0.04 |
| d_5 | 0.01 | 0.04 |
| d_6 | 0.13 | 0.35 |

highest in-degree: d_2, d_3, d_6

highest out-degree: d_2, d_6

highest PageRank: d_6

highest hub score: d_6 (close: d_2)

highest authority score: d_3

Transition (probability) matrix

| | d_0 | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|-------|
| d_0 | 0.00 | 0.00 | 1.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| d_1 | 0.00 | 0.50 | 0.50 | 0.00 | 0.00 | 0.00 | 0.00 |
| d_2 | 0.33 | 0.00 | 0.33 | 0.33 | 0.00 | 0.00 | 0.00 |
| d_3 | 0.00 | 0.00 | 0.00 | 0.50 | 0.50 | 0.00 | 0.00 |
| d_4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.00 |
| d_5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.50 | 0.50 |
| d_6 | 0.00 | 0.00 | 0.00 | 0.33 | 0.33 | 0.00 | 0.33 |

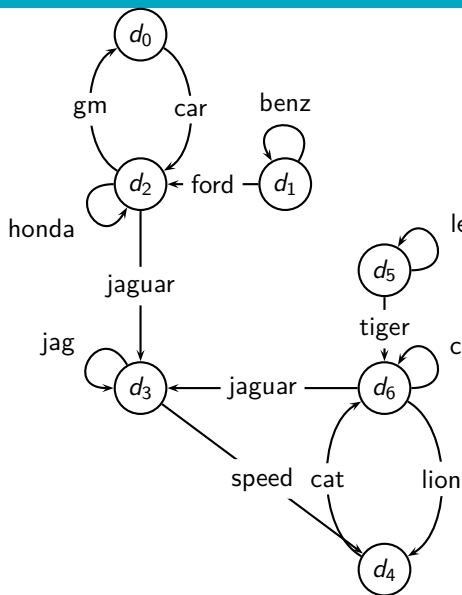
Transition matrix with teleporting, teleportation rate=0.14

| | d_0 | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|-------|
| d_0 | 0.02 | 0.02 | 0.88 | 0.02 | 0.02 | 0.02 | 0.02 |
| d_1 | 0.02 | 0.45 | 0.45 | 0.02 | 0.02 | 0.02 | 0.02 |
| d_2 | 0.31 | 0.02 | 0.31 | 0.31 | 0.02 | 0.02 | 0.02 |
| d_3 | 0.02 | 0.02 | 0.02 | 0.45 | 0.45 | 0.02 | 0.02 |
| d_4 | 0.02 | 0.02 | 0.02 | 0.02 | 0.02 | 0.02 | 0.88 |
| d_5 | 0.02 | 0.02 | 0.02 | 0.02 | 0.02 | 0.45 | 0.45 |
| d_6 | 0.02 | 0.02 | 0.02 | 0.31 | 0.31 | 0.02 | 0.31 |

Power method vectors $\vec{x}P^k$

| | \vec{x} | $\vec{x}P^1$ | $\vec{x}P^2$ | $\vec{x}P^3$ | $\vec{x}P^4$ | $\vec{x}P^5$ | $\vec{x}P^6$ | $\vec{x}P^7$ | $\vec{x}P^8$ | $\vec{x}P^9$ | $\vec{x}P^{10}$ | $\vec{x}P^{11}$ | $\vec{x}P^{12}$ | $\vec{x}P^{13}$ |
|-------|-----------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|-----------------|-----------------|-----------------|-----------------|
| d_0 | 0.14 | 0.06 | 0.09 | 0.07 | 0.07 | 0.06 | 0.06 | 0.06 | 0.06 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 |
| d_1 | 0.14 | 0.08 | 0.06 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 |
| d_2 | 0.14 | 0.25 | 0.18 | 0.17 | 0.15 | 0.14 | 0.13 | 0.12 | 0.12 | 0.12 | 0.12 | 0.11 | 0.11 | 0.11 |
| d_3 | 0.14 | 0.16 | 0.23 | 0.24 | 0.24 | 0.24 | 0.24 | 0.25 | 0.25 | 0.25 | 0.25 | 0.25 | 0.25 | 0.25 |
| d_4 | 0.14 | 0.12 | 0.16 | 0.19 | 0.19 | 0.20 | 0.21 | 0.21 | 0.21 | 0.21 | 0.21 | 0.21 | 0.21 | 0.21 |
| d_5 | 0.14 | 0.08 | 0.06 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 | 0.04 |
| d_6 | 0.14 | 0.25 | 0.23 | 0.25 | 0.27 | 0.28 | 0.29 | 0.29 | 0.30 | 0.30 | 0.30 | 0.30 | 0.31 | 0.31 |

Example web graph



PageRank

| | | | | | |
|-------|------|-------|------|-------|------|
| d_0 | 0.05 | d_1 | 0.04 | d_2 | 0.11 |
| d_3 | 0.25 | d_4 | 0.21 | d_5 | 0.04 |
| d_6 | 0.31 | | | | |

PageRank(d_2) < PageRank(d_6):
why?

| | a | h |
|-------|------|------|
| d_0 | 0.10 | 0.03 |
| d_1 | 0.01 | 0.04 |
| d_2 | 0.12 | 0.33 |
| d_3 | 0.47 | 0.18 |
| d_4 | 0.16 | 0.04 |
| d_5 | 0.01 | 0.04 |
| d_6 | 0.13 | 0.35 |

highest in-degree: d_2, d_3, d_6

highest out-degree: d_2, d_6

highest PageRank: d_6

highest hub score: d_6 (close: d_2)

highest authority score: d_3 □

How important is PageRank?

- Frequent claim: PageRank is the most important component of web ranking.
- The reality:
 - There are several components that are at least as important: e.g., anchor text, phrases, proximity, tiered indexes . . .
 - Rumor has it that PageRank in its original form (as presented here) now has a negligible impact on ranking!
 - However, variants of a page's PageRank are still an essential part of ranking.
 - Addressing link spam is difficult and crucial. □

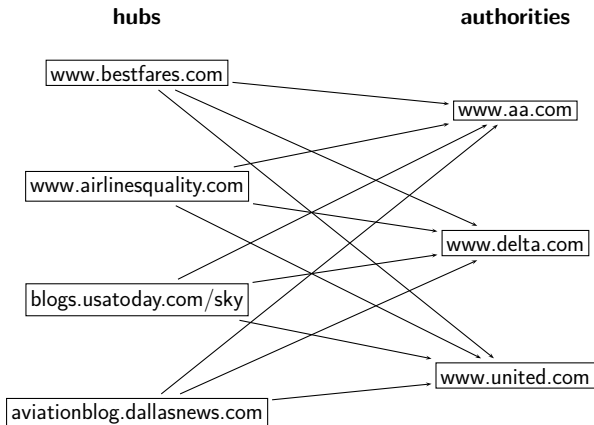
HITS – Hyperlink-Induced Topic Search

- Premise: there are two different types of relevance on the web.
- Relevance type 1: **Hubs**. A hub page is a good list of [links to pages answering the information need].
 - E.g., for query [chicago bulls]: Bob's list of recommended resources on the Chicago Bulls sports team
- Relevance type 2: **Authorities**. An authority page is a direct answer to the information need.
 - The home page of the Chicago Bulls sports team
 - By definition: Links to authority pages occur repeatedly on hub pages.
- Most approaches to search (including PageRank ranking) don't make the distinction between these two very different types of relevance. □

Hubs and authorities: Definition

- A good hub page for a topic **links to** many authority pages for that topic.
- A good authority page for a topic **is linked to** by many hub pages for that topic.
- Circular definition – we will turn this into an iterative computation. □

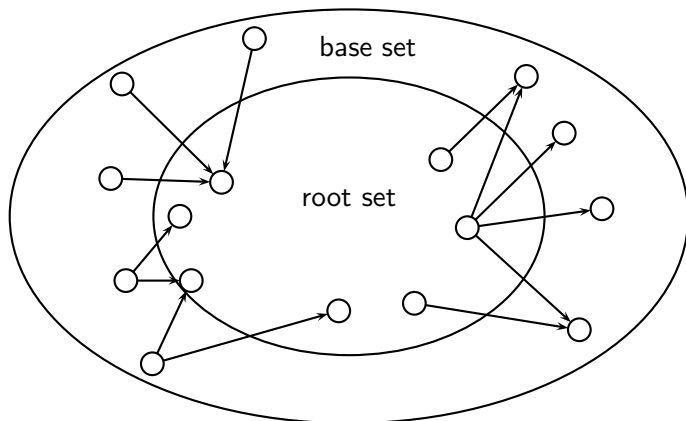
Example for hubs and authorities



How to compute hub and authority scores

- Do a regular web search first
- Call the search result the **root set**
- Find all pages that are linked to or link to pages in the root set
- Call this larger set the **base set**
- Finally, compute hubs and authorities for the base set (which we'll view as a small web graph) □

Root set and base set (1)



- 1) The root set
- 2) Nodes that root set nodes link to
- 3) Nodes that link to root set nodes
- 4) The base set

Root set and base set (2)

- Root set typically has 200–1,000 nodes.
- Base set may have up to 5,000 nodes.
- Computation of base set, as shown on previous slide:
 - Follow outlinks by parsing the pages in the root set
 - Find d 's inlinks by searching for all pages containing a link to d



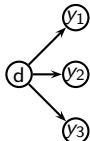
Hub and authority scores

- Compute for each page d in the base set a **hub score** $h(d)$ and an **authority score** $a(d)$
- Initialization: for all d : $h(d) = 1$, $a(d) = 1$
- Iteratively update all $h(d)$, $a(d)$
- After convergence:
 - Output pages with highest h scores as top hubs
 - Output pages with highest a scores as top authorities
 - So we output **two** ranked lists

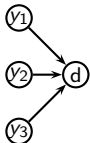


Iterative update

- For all d : $h(d) = \sum_{d \mapsto y} a(y)$



- For all d : $a(d) = \sum_{y \mapsto d} h(y)$



- Iterate these two steps until convergence



Details

- Scaling
 - To prevent the $a()$ and $h()$ values from getting too big, can scale down after each iteration
 - Scaling factor doesn't really matter.
 - We care about the **relative** (as opposed to absolute) values of the scores.
- In most cases, the algorithm converges after a few iterations. □

Authorities for query [Chicago Bulls]

- 0.85 www.nba.com/bulls
- 0.25 www.essex1.com/people/jmiller/bulls.htm
“da Bulls”
- 0.20 www.nando.net/SportServer/basketball/nba/chi.html
“The Chicago Bulls”
- 0.15 users.aol.com/rynocub/bulls.htm
“The Chicago Bulls Home Page”
- 0.13 www.geocities.com/Colosseum/6095
“Chicago Bulls”

(Ben-Shaul et al, WWW8)

The authority page for [Chicago Bulls]

NBA D-LEAGUE WNBA GLOBAL TEAMS MOBILE NBA TICKETS FANTASY NBATV STORE VIDEO

bills.com THE OFFICIAL SITE OF THE CHICAGO BULLS
Delivered by at&t

NEWSLETTER CONTACT US

TICKETS TEAM NEWS SCHEDULE FEATURES GAME NIGHT INSIDE THE BULLS HISTORY STORE SEARCH

Fore!!! Golf with the Bulls!
Tickets for the Chicago Bulls/Verizon Wireless *Cherry Red Series* are now on sale! Join Bulls' personalities including current players, coaches, legends, broadcasters and entertainment teams on August 17 at the White Pine Golf Club in Bensenville, Ill.

- 2009.10: [Season & Game Tickets](#)
- [Mobile Alerts](#) | [Facebook](#) | [Twitter](#)
- [RSS](#) | [News Clips](#) | [myBulls](#) | [Sam Smith](#)

- Bulls to compete in NBA Summer League
- Chicago Bulls | Draft Central 2009
- Pre-draft Ask Sam mailbag special
- Pre-draft interview: Wake's Jeff Teague
- Pre-draft interview: VCU's Eric Maynor
- Pre-draft interview: Wake's James Johnson
- Pre-draft interview: UNC's Wayne Ellington

Draft Workouts

BULLSEYE POWERED BY KIA KIA MOTORS

| CALENDAR | TICKETS |
|----------------|----------------|
| SEASON TICKETS | TICKETEXCHANGE |
| GROUP TICKETS | E-NEWSLETTER |

SEASON TICKETS

CHICAGO BULLS PRESENTED BY **HARRIS**

verizon wireless FAN POLL

Hubs for query [Chicago Bulls]

- 1.62 www.geocities.com/Colosseum/1778
“Unbelieveabulls!!!!!”
- 1.24 www.webring.org/cgi-bin/webring?ring=chbulls
“Erin’s Chicago Bulls Page”
- 0.74 www.geocities.com/Hollywood/Lot/3330/Bulls.html
“Chicago Bulls”
- 0.52 www.nobull.net/web_position/kw-search-15-M2.htm
“Excite Search Results: bulls”
- 0.52 www.halcyon.com/wordsltd/bball/bulls.htm
“Chicago Bulls Links”

(Ben-Shaul et al, WWW8)

A hub page for [Chicago Bulls]



COAST TO COAST TICKETS
great tickets from nice people

Returning Customer

City Guide | \

Minnesota Timberwolves Tickets
New Jersey Nets Tickets
New Orleans Hornets Tickets
New York Knicks Tickets
Oklahoma City Thunder Tickets
Orlando Magic Tickets
Philadelphia 76ers Tickets
Phoenix Suns Tickets
Portland Trail Blazers Tickets
Sacramento Kings Tickets
San Antonio Spurs Tickets
Toronto Raptors Tickets
Utah Jazz Tickets
Washington Wizards Tickets
NBA All-Star Weekend
NBA Finals Tickets
NBA Playoffs Tickets

[All NBA Tickets](#)

Event Selections

Sporting Events

MLB Baseball Tickets

NFL Football Tickets

NBA Basketball Tickets

NHL Hockey Tickets

NASCAR Racing Tickets

PGA Golf Tickets

Tennis Tickets

NCAA Football Tickets

Official Website Links:

[Chicago Bulls \(official site\)](#)
<http://www.nba.com/bulls/>

Fan Club - Fan Site Links:

[Chicago Bulls](#)
Chicago Bulls Fan Site with Bulls Blog, News, Bulls Forum, Wallpapers and all your basic Chicago Bulls essentials!!
<http://www.bullscentral.com>

[Chicago Bulls Blog](#)
The place to be for news and views on the Chicago Bulls and NBA Basketball
<http://chi-bulls.blogspot.com>

News and Information Links:

[Chicago Sun-Times \(local newspaper\)](#)
<http://www.suntimes.com/sports/basketball/bulls/index.html>

[Chicago Tribune \(local newspaper\)](#)
<http://www.chicagotribune.com/sports/basketball/bulls/>

[Wikipedia - Chicago Bulls](#)
All about the Chicago Bulls from Wikipedia, the free online encyclopedia.
http://en.wikipedia.org/wiki/Chicago_Bulls

Merchandise Links:

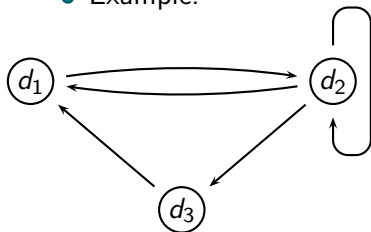
[Chicago Bulls watches](#)
http://www.sportimewatches.com/NBA_watches/Chicago-Bulls-watches.html

Hubs & Authorities: Comments

- HITS can pull together good pages regardless of page content.
- Once the base set is assembled, we only do link analysis, no text matching.
- Pages in the base set often do not contain any of the query words.
- In theory, an English query can retrieve Japanese-language pages!
 - If supported by the link structure between English and Japanese pages
- Danger: **topic drift** – the pages found by following links may not be related to the original query. □

Proof of convergence

- We define an $N \times N$ **adjacency matrix** A . (We called this the link matrix earlier.)
- For $1 \leq i, j \leq N$, the matrix entry A_{ij} tells us whether there is a link from page i to page j ($A_{ij} = 1$) or not ($A_{ij} = 0$).
- Example:



| | d_1 | d_2 | d_3 |
|-------|-------|-------|-------|
| d_1 | 0 | 1 | 0 |
| d_2 | 1 | 1 | 1 |
| d_3 | 1 | 0 | 0 |

Write update rules as matrix operations

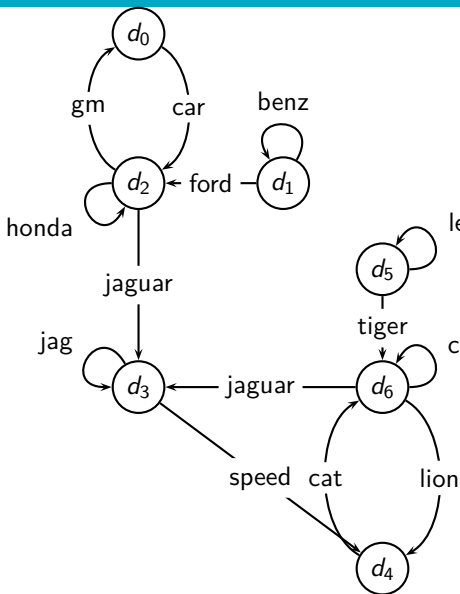
- Define the hub vector $\vec{h} = (h_1, \dots, h_N)$ as the vector of hub scores. h_i is the hub score of page d_i .
- Similarly for \vec{a} , the vector of authority scores
- Now we can write $h(d) = \sum_{d \mapsto y} a(y)$ as a matrix operation:
$$\vec{h} = A\vec{a} \dots$$
- ... and we can write $a(d) = \sum_{y \mapsto d} h(y)$ as $\vec{a} = A^T \vec{h}$
- HITS algorithm in matrix notation:
 - Compute $\vec{h} = A\vec{a}$
 - Compute $\vec{a} = A^T \vec{h}$
 - Iterate until convergence



HITS as eigenvector problem

- HITS algorithm in matrix notation. Iterate:
 - Compute $\vec{h} = A\vec{a}$
 - Compute $\vec{a} = A^T\vec{h}$
- By substitution we get: $\vec{h} = AA^T\vec{h}$ and $\vec{a} = A^TA\vec{a}$
- Thus, \vec{h} is an eigenvector of AA^T and \vec{a} is an eigenvector of A^TA .
- So the HITS algorithm is actually a special case of the power method and hub and authority scores are eigenvector values.
- HITS and PageRank both formalize link analysis as eigenvector problems. □

Example web graph



PageRank

| | | | | | |
|-------|------|-------|------|-------|------|
| d_0 | 0.05 | d_1 | 0.04 | d_2 | 0.11 |
| d_3 | 0.25 | d_4 | 0.21 | d_5 | 0.04 |
| d_6 | 0.31 | | | | |

PageRank(d_2) < PageRank(d_6):
why?

| | a | h |
|-------|------|------|
| d_0 | 0.10 | 0.03 |
| d_1 | 0.01 | 0.04 |
| d_2 | 0.12 | 0.33 |
| d_3 | 0.47 | 0.18 |
| d_4 | 0.16 | 0.04 |
| d_5 | 0.01 | 0.04 |
| d_6 | 0.13 | 0.35 |

highest in-degree: d_2, d_3, d_6

highest out-degree: d_2, d_6

highest PageRank: d_6

highest hub score: d_6 (close: d_2)

highest authority score: d_3 □

Raw matrix A for HITS

We double-weight links whose anchors contain query word:

| | d_0 | d_1 | d_2 | d_3 | d_4 | d_5 | d_6 |
|-------|-------|-------|-------|-------|-------|-------|-------|
| d_0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| d_1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| d_2 | 1 | 0 | 1 | 2 | 0 | 0 | 0 |
| d_3 | 0 | 0 | 0 | 1 | 1 | 0 | 0 |
| d_4 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| d_5 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| d_6 | 0 | 0 | 0 | 2 | 1 | 0 | 1 |

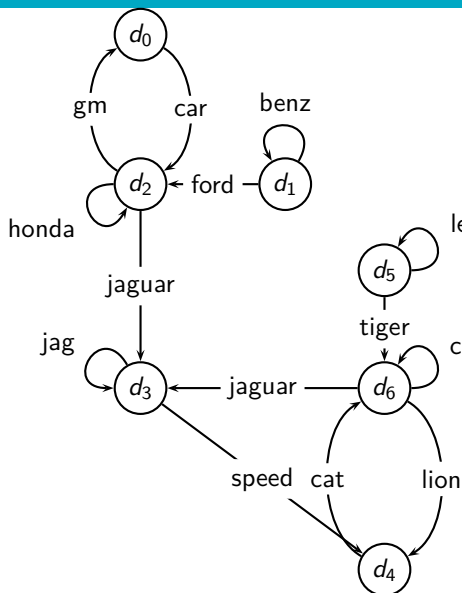
Hub vectors $h_0, \vec{h}_i = \frac{1}{d_i} A \cdot \vec{a}_i, i \geq 1$

| | \vec{h}_0 | \vec{h}_1 | \vec{h}_2 | \vec{h}_3 | \vec{h}_4 | \vec{h}_5 |
|-------|-------------|-------------|-------------|-------------|-------------|-------------|
| d_0 | 0.14 | 0.06 | 0.04 | 0.04 | 0.03 | 0.03 |
| d_1 | 0.14 | 0.08 | 0.05 | 0.04 | 0.04 | 0.04 |
| d_2 | 0.14 | 0.28 | 0.32 | 0.33 | 0.33 | 0.33 |
| d_3 | 0.14 | 0.14 | 0.17 | 0.18 | 0.18 | 0.18 |
| d_4 | 0.14 | 0.06 | 0.04 | 0.04 | 0.04 | 0.04 |
| d_5 | 0.14 | 0.08 | 0.05 | 0.04 | 0.04 | 0.04 |
| d_6 | 0.14 | 0.30 | 0.33 | 0.34 | 0.35 | 0.35 |

Authority vectors $\vec{a}_i = \frac{1}{c_i} A^T \cdot \vec{h}_{i-1}, i \geq 1$

| | \vec{a}_1 | \vec{a}_2 | \vec{a}_3 | \vec{a}_4 | \vec{a}_5 | \vec{a}_6 | \vec{a}_7 |
|-------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| d_0 | 0.06 | 0.09 | 0.10 | 0.10 | 0.10 | 0.10 | 0.10 |
| d_1 | 0.06 | 0.03 | 0.01 | 0.01 | 0.01 | 0.01 | 0.01 |
| d_2 | 0.19 | 0.14 | 0.13 | 0.12 | 0.12 | 0.12 | 0.12 |
| d_3 | 0.31 | 0.43 | 0.46 | 0.46 | 0.46 | 0.47 | 0.47 |
| d_4 | 0.13 | 0.14 | 0.16 | 0.16 | 0.16 | 0.16 | 0.16 |
| d_5 | 0.06 | 0.03 | 0.02 | 0.01 | 0.01 | 0.01 | 0.01 |
| d_6 | 0.19 | 0.14 | 0.13 | 0.13 | 0.13 | 0.13 | 0.13 |

Example web graph



PageRank

| | | | | | |
|-------|------|-------|------|-------|------|
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PageRank(d_2) < PageRank(d_6):
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highest in-degree: d_2, d_3, d_6

highest out-degree: d_2, d_6

highest PageRank: d_6

highest hub score: d_6 (close: d_2)

highest authority score: d_3 □

PageRank vs. HITS: Discussion

- PageRank can be precomputed, HITS has to be computed at query time.
 - HITS is too expensive in most application scenarios.
- PageRank and HITS make two different design choices concerning (i) the eigenproblem formalization (ii) the set of pages to apply the formalization to.
- These two are orthogonal.
 - We could also apply HITS to the entire web and PageRank to a small base set.
- Claim: On the web, a good hub almost always is also a good authority.
- The actual difference between PageRank ranking and HITS ranking is therefore not as large as one might expect. □

Exercise

- Why is a good hub almost always also a good authority?

Take-away today

- Anchor text: What exactly are links on the web and why are they important for IR?
- Citation analysis: the mathematical foundation of PageRank and link-based ranking
- PageRank: the original algorithm that was used for link-based ranking on the web
- Hubs & Authorities: an alternative link-based ranking algorithm

Resources

- Chapter 21 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - American Mathematical Society article on PageRank (popular science style)
 - Jon Kleinberg's home page (main person behind HITS)
 - A Google bomb and its defusing
 - Google's official description of PageRank: *PageRank reflects our view of the importance of web pages by considering more than 500 million variables and 2 billion terms. Pages that we believe are important pages receive a higher PageRank and are more likely to appear at the top of the search results.*

PV211: Introduction to Information Retrieval

<https://www.fi.muni.cz/~sojka/PV211>

IIR 20: Crawling Handout version

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2024-05-15

(compiled on 2024-05-06 13:41:14)

How hard can crawling be?

- Web [search engines must crawl](#) their documents.
- Getting the content of the documents is easier for many other IR systems.
 - E.g., indexing all files on your hard disk: just do a recursive descent on your file system
- Ok: for web IR, getting the content of the documents takes longer ...
- ... because of latency.
- But is that really a design/systems challenge?

Basic crawler operation

- Initialize queue with URLs of known seed pages
- Repeat
 - Take URL from queue
 - Fetch and parse page
 - Extract URLs from page
 - Add URLs to queue
- Fundamental assumption: The web is well linked.

Exercise: What's wrong with this crawler?

```
urlqueue := (some carefully selected set of seed urls)
while urlqueue is not empty:
    myurl := urlqueue.getlastanddelete()
    mypage := myurl.fetch()
    fetchedurls.add(myurl)
    newurls := mypage.extracturls()
    for myurl in newurls:
        if myurl not in fetchedurls and not in urlqueue:
            urlqueue.add(myurl)
    addtoinvertedindex(mypage)
```

What's wrong with the simple crawler

- Scale: we need to **distribute**.
- We can't index everything: we need to **subselect**. How?
- Duplicates: need to integrate **duplicate detection**
- Spam and spider traps: need to integrate **spam detection**
- **Politeness**: we need to be “nice” and space out all requests for a site over a longer period (hours, days)
- **Freshness**: we need to recrawl periodically.
 - Because of the size of the web, we can do frequent recrawls only for a small subset.
 - Again, subselection problem or **prioritization**

Magnitude of the crawling problem

- To fetch 20,000,000,000 pages in one month . . .
- . . . we need to fetch almost 8,000 pages per second!
- Actually: many more since many of the pages we attempt to crawl will be duplicates, unfetchable, spam, etc.

What a crawler must do

Be polite

- Don't hit a site too often
- Only crawl pages you are allowed to crawl: `robots.txt`

Be robust

- Be immune to spider traps, duplicates, very large pages, very large websites, dynamic pages, etc.

robots.txt

- Protocol for giving crawlers (“robots”) limited access to a website, originally from 1994
- Examples:
 - User-agent: *
Disallow: /yoursite/temp/
 - User-agent: searchengine
Disallow: /
- Important: cache the robots.txt file of each site we are crawling

Example of a robots.txt (nih.gov)

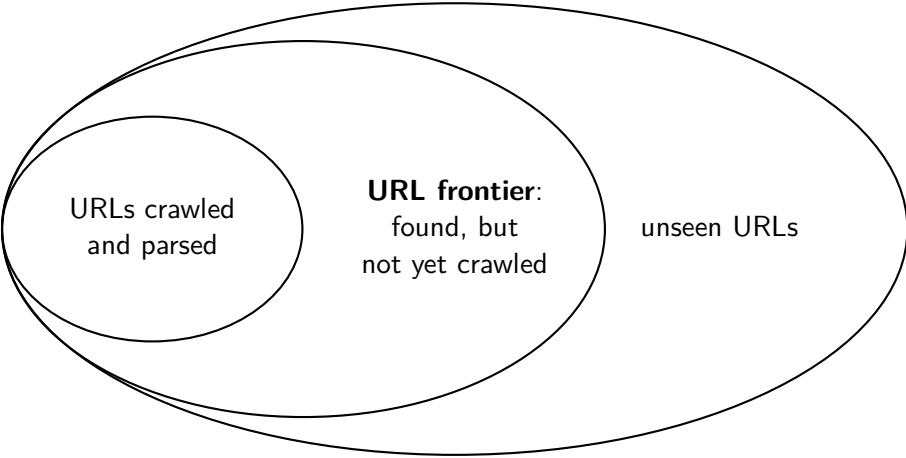
```
User-agent: PicoSearch/1.0
Disallow: /news/information/knight/
Disallow: /nidcd/
...
Disallow: /news/research_matters/secure/
Disallow: /od/ocpl/wag/

User-agent: *
Disallow: /news/information/knight/
Disallow: /nidcd/
...
Disallow: /news/research_matters/secure/
Disallow: /od/ocpl/wag/
Disallow: /ddir/
Disallow: /sdminutes/
```


What any crawler should do

- Be capable of **distributed** operation
- Be scalable: need to be able to increase crawl rate by adding more machines
- Fetch pages of higher quality first
- Continuous operation: get fresh version of already crawled pages

URL frontier



The diagram consists of three nested ellipses. The innermost ellipse on the left is labeled 'URLs crawled and parsed'. The middle ellipse is labeled 'URL frontier: found, but not yet crawled'. The outermost ellipse is labeled 'unseen URLs'. The 'URL frontier' ellipse is contained within the 'unseen URLs' ellipse, and the 'URLs crawled and parsed' ellipse is contained within the 'URL frontier' ellipse.

URLs crawled
and parsed

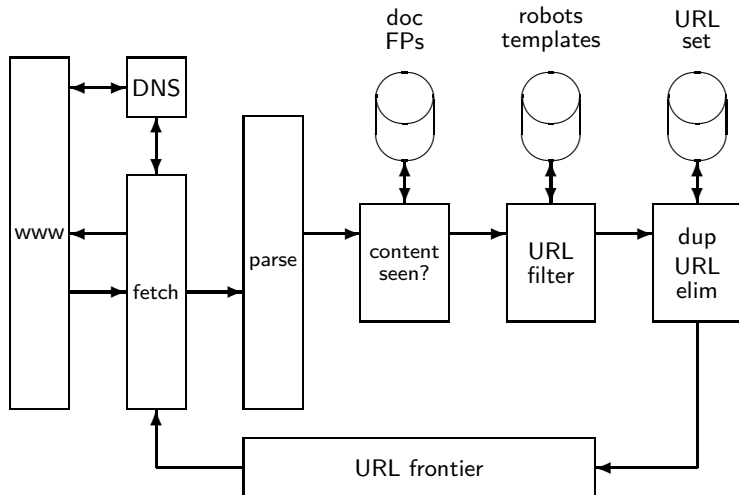
URL frontier:
found, but
not yet crawled

unseen URLs

URL frontier

- The URL frontier is the data structure that holds and manages URLs we've seen, but that have not been crawled yet.
- Can include multiple pages from the same host
- Must avoid trying to fetch them all at the same time
- Must keep all crawling threads busy

Basic crawl architecture



URL normalization

- Some URLs extracted from a document are **relative** URLs.
- E.g., at `http://www.fi.muni.cz/~sojka/PV211/`, we may have `p20crawl.pdf`
 - This is the same as URL:
`http://www.fi.muni.cz/~sojka/PV211/p20crawl.pdf`
- During parsing, we must normalize (expand) all relative URLs.

Content seen

- For each page fetched: check if the content is already in the index
- Check this using document fingerprints or [shingles](#)
- Skip documents whose content has already been indexed

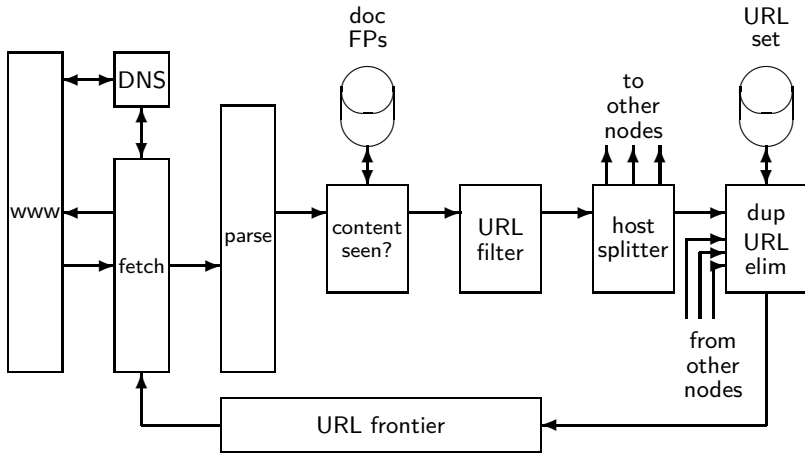
Distributing the crawler

- Run multiple crawl threads, potentially at different nodes
 - Usually geographically distributed nodes
- Partition hosts being crawled into nodes

Google data centers (wayfaring.com)



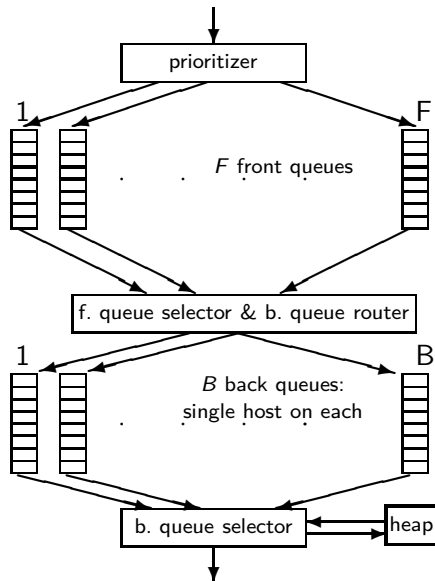
Distributed crawler



URL frontier: Two main considerations

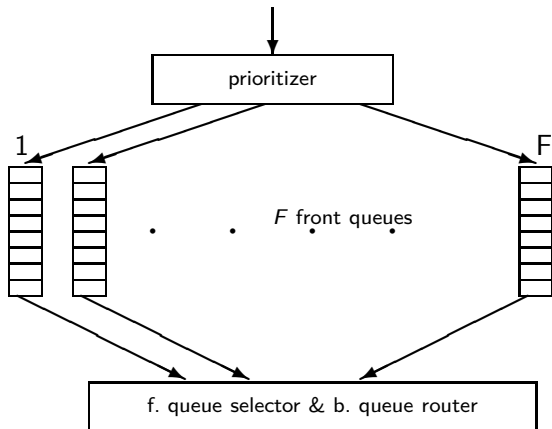
- Politeness: Don't hit a web server too frequently
 - E.g., insert a time gap between successive requests to the same server
- Freshness: Crawl some pages (e.g., news sites) more often than others
- Not an easy problem: simple priority queue fails.

Mercator URL frontier



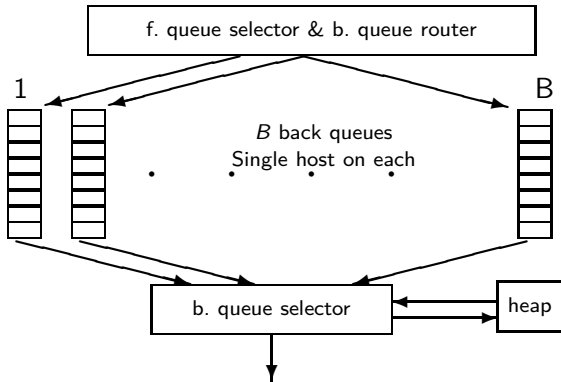
- URLs flow in from the top into the frontier.
- Front queues manage prioritization.
- Back queues enforce politeness.
- Each queue is FIFO.

Mercator URL frontier: Front queues



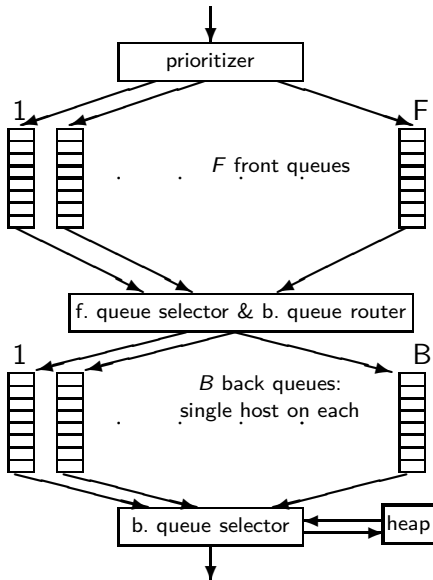
- Prioritizer assigns to URL an integer priority between 1 and F .
- Then appends URL to corresponding queue
- Heuristics for assigning priority: refresh rate, PageRank, etc.
- Selection from front queues is initiated by back queues

Mercator URL frontier: Back queues



- **Invariant 1.** Each back queue is kept non-empty while the crawl is in progress.
- **Invariant 2.** Each back queue only contains URLs from a single host.
- Maintain a table from hosts to back queues.
- In the heap:
 - One entry for each back queue
 - The entry is the earliest time t_e at

Mercator URL frontier



- URLs flow in from the top into the frontier.
- Front queues manage prioritization.
- Back queues enforce politeness.
- Each queue is FIFO.

Spider trap

- Malicious server that generates an infinite sequence of linked pages.
- Sophisticated spider traps generate pages that are not easily identified as dynamic.

Resources

- Chapter 20 of IIR
- Resources at <https://www.fi.muni.cz/~sojka/PV211/> and <http://cislmu.org>, materials in MU IS and FI MU library
 - Papers by NLP centre people crawling data for Sketch Engine
 - Paper on Mercator by Heydon et al.
 - Robot exclusion standard